

# Electric Fields

## & Potential Mapping

### 1) Electric Fields

— a field in physics is a quantity that has a value at every point in space or some specified region of space

— a scalar field is one where there the field just has a value at every point in space

e.g., density, temperature, pressure

→ The value can be positive or

2) negative — so it's not just a magnitude, (e.g., Celsius temperature)

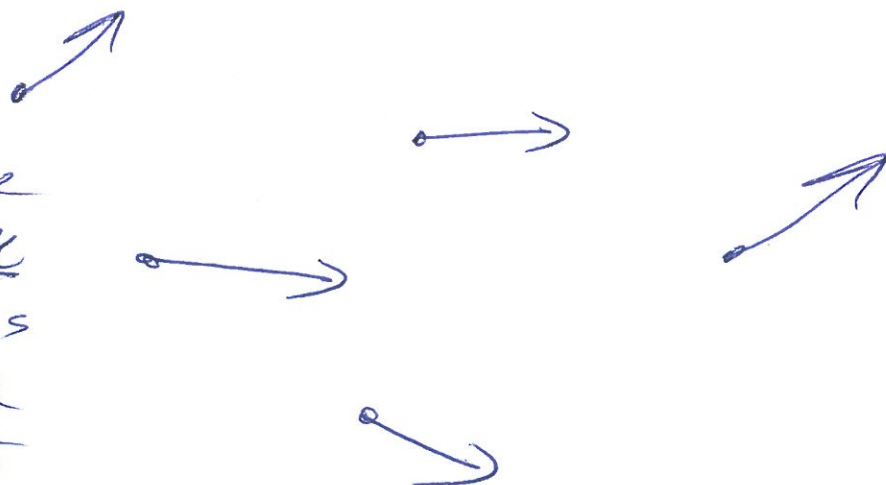
But the quantity has no direction assigned to it.

— A vector field has a magnitude and a direction.

I think of little arrows attached to each point

The arrows in space.

The arrows point in ordinary 3-d space but their extent is their own abstract space.



Of course, there is a continuum infinity of such arrows — so one can only draw a representative sample which in mapping can be made large enough to allow the whole field to be visualized by interpolation.

## 2) The Electric Field

The electric field (E-field) in one sense extends throughout space and is singular.

A) But particular regions of this ~~of~~ universal  $\mathbf{E}$ -field can have their own special structure and rather than refer to them as  $\mathbf{E}$ -field regions, we just call them  $\mathbf{E}$ -fields for particular systems.

~~The  $\mathbf{E}$  or  $\mathbf{A}$~~  Context decides which is meant.

The  $\mathbf{E}$ -field is the cause of the electric ~~or~~ force

For a point charge  $q$

$$\mathbf{F} = q \mathbf{E} \quad \left\{ \begin{array}{l} \text{unit of } \mathbf{E}\text{-field} \\ \frac{\text{N}}{\text{C}} = \frac{\text{V}}{\text{m}} \end{array} \right. \left. \begin{array}{l} \text{volt} \\ \text{per} \\ \text{meter} \end{array} \right.$$

is the ~~charge~~  
electric force on  $q$ .

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— the electric field has an associated energy density and variations in the  $\mathbf{E}$ -field propagate thru vacuum at the vacuum light speed.

— The electric field is a real thing, not a mathematical auxiliary, in electromagnetism.

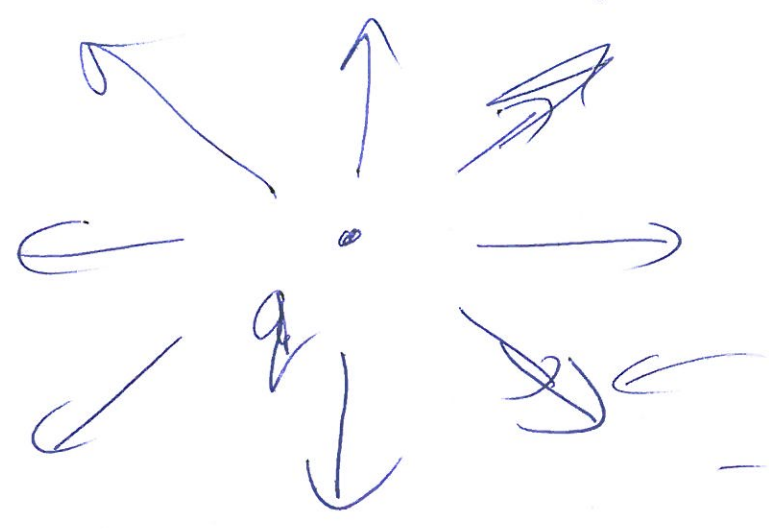
— The  $\mathbf{E}$ -field can be caused by charge.

For a point charge  $q$

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$$\vec{E} = \frac{kq}{r^2} \hat{r}$$

with the origin at the point charge.



$\vec{E}$ -field vectors  
 - Recall they point in ~~real~~ physical space

The  $\vec{E}$ -field of collections of point charges can be calculated

by adding up with vector addition the  $\vec{E}$ -fields of the individual charge.

but extend in their own abstract  $\vec{E}$ -field space.

Their length is their strength.

An  $\vec{E}$ -field can also be caused by

a time varying magnetic field without charge

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This effect is described by Faraday's law of induction (well the Maxwell-Faraday version)

We will get to that in a later lab

The  $E$ -field in one sense is invisible to the human eye but in another sense it's half of all we do see.

— light is a self-propagating coupled electromagnetic field.

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The electromagnetic field being a coupled (i.e., interacting) electric & magnetic field

OR the  $\mathbf{E}$ -field & magnetic field considered jointly.

③

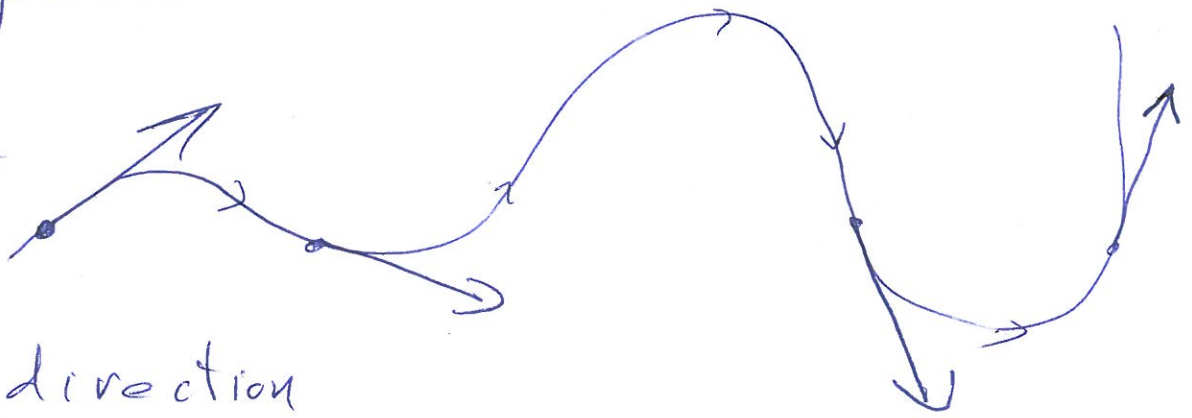
Field Lines

In mapping and visualizing  $\mathbf{E}$ -fields (and other vector fields too), one can use field lines (introduced by Faraday — what a guy!).



The idea is to draw [ 9  
a continuous line (that  
not a straight one in general)  
that is tangent at  
every point in space  
to the  $\mathbf{E}$ -field at that  
point

Example



The direction  
of the field is that  
of the tangent  $\mathbf{E}$ -field  
vectors,

Question

Can field lines  
ever cross?

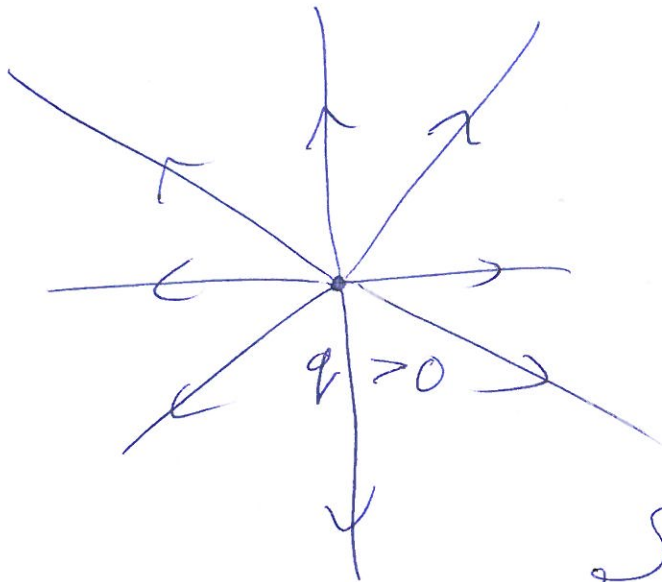
10) Ans No & Yes (sort of)

No field lines cannot cross because to cross the  $E$ -field would have to point in two directions at one point which is impossible

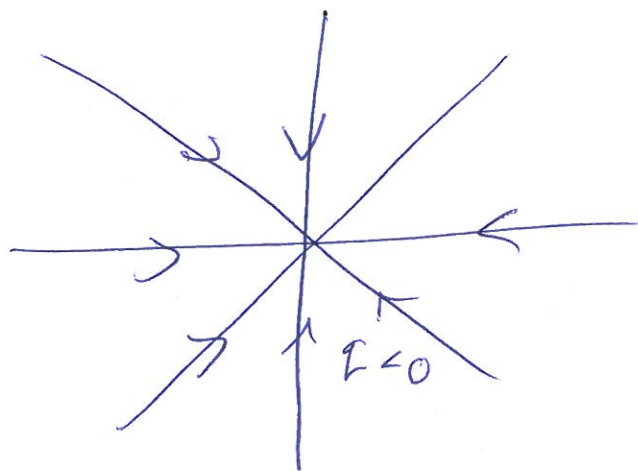
Yes (sort of) . If the  $E$ -field goes to zero at a point, then one can sort of say  $E$ -field lines cross there or alternatively end there. ~~Well~~ We'll see ~~consider~~ this in ~~some~~ examples below.

# Example E-fields

a) Point charges — isolated one



Field lines start on positive charge and extend to infinity

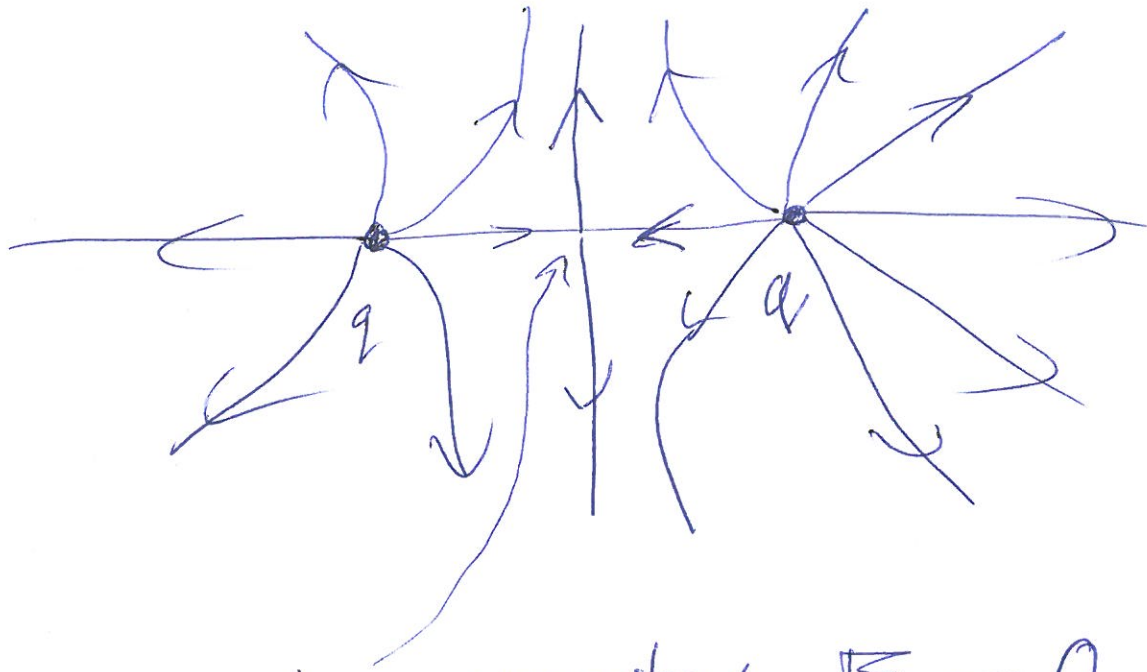


Field lines end on negative charge and come in from infinity.

one is only looking at a planar slice of space here and one ~~can~~ can only draw a representative set of field lines

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b) Two equal positive charges



by symmetry  $\vec{E} = 0$

and the field lines

cross on end and start

here depending on  
your point of view.

- up close to either charge each has a point-charge  $E$ -field for a charge  $q$
- far away from both the  $E$ -field approaches

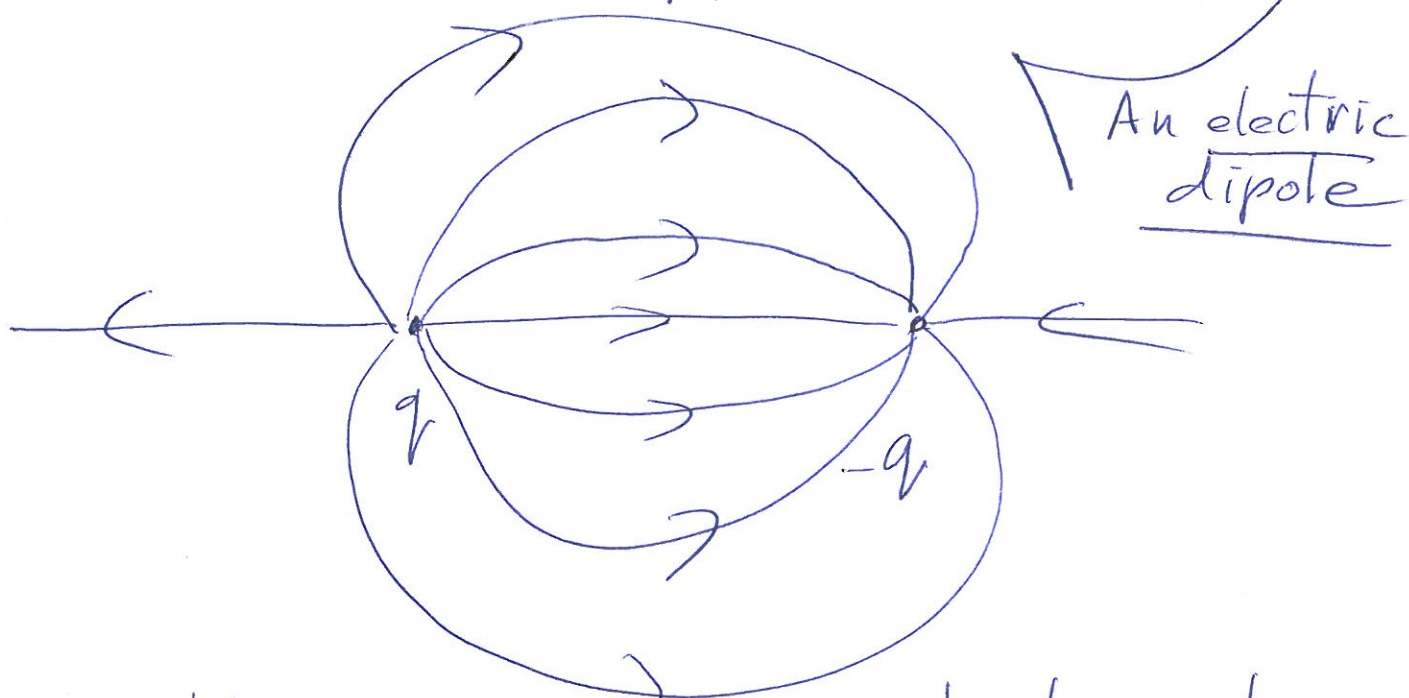
That of a point

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In between  
one interpolates,

change of charge  $2q$   
located at the center  
of symmetry.

c) Two point charges  
of equal magnitude  
and opposite sign



— the field has rotational  
symmetry about the  
symmetry axis

— in a planar slice the dipole field

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has a butterfly shape

— at far field, the dipole field never looks like a monopole field (i.e., the field of one point charge)

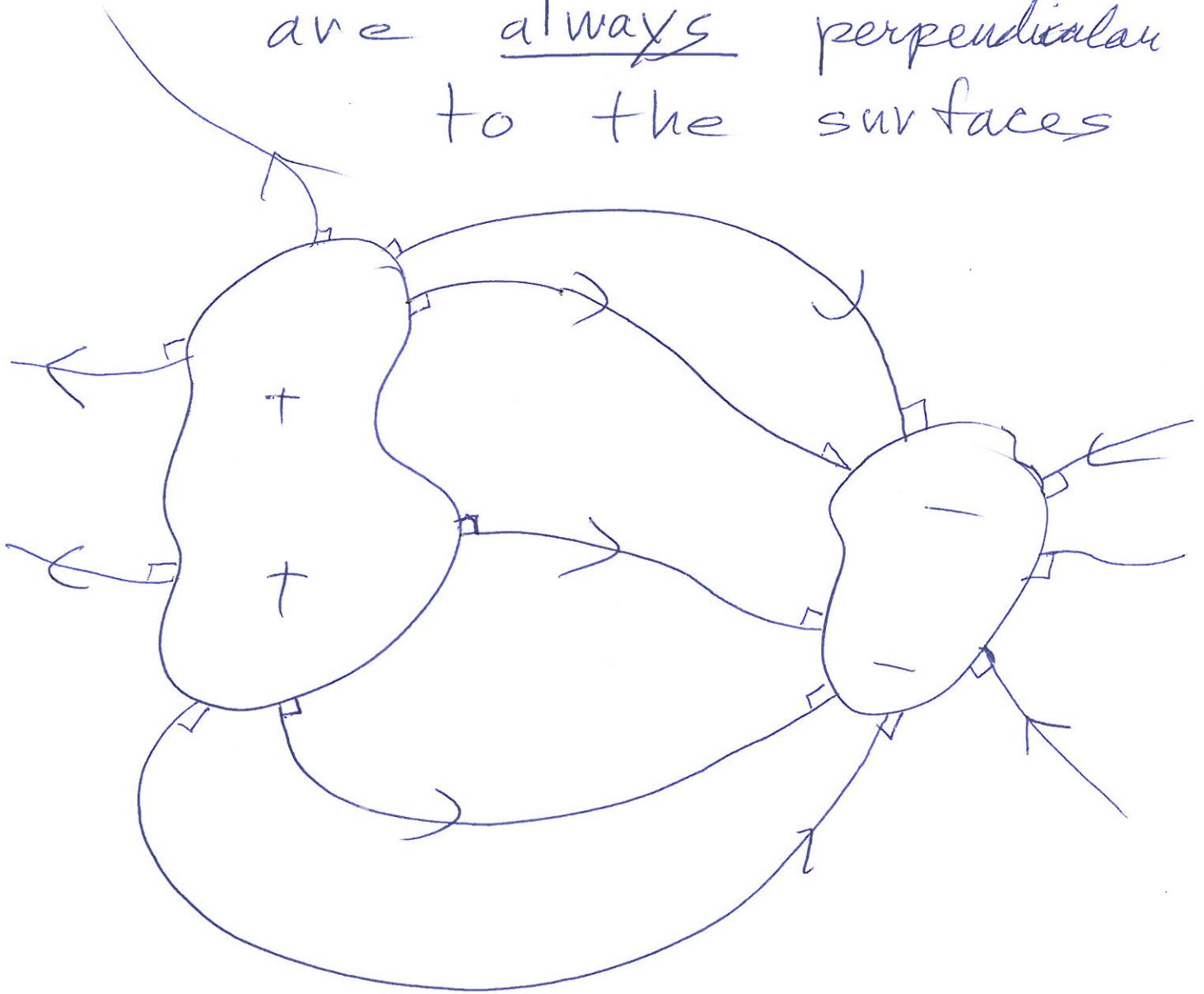
d) Equipotential surface of electrostatic or at least constant potential conductors

— We'll discuss equipotentials below, but the

key point for

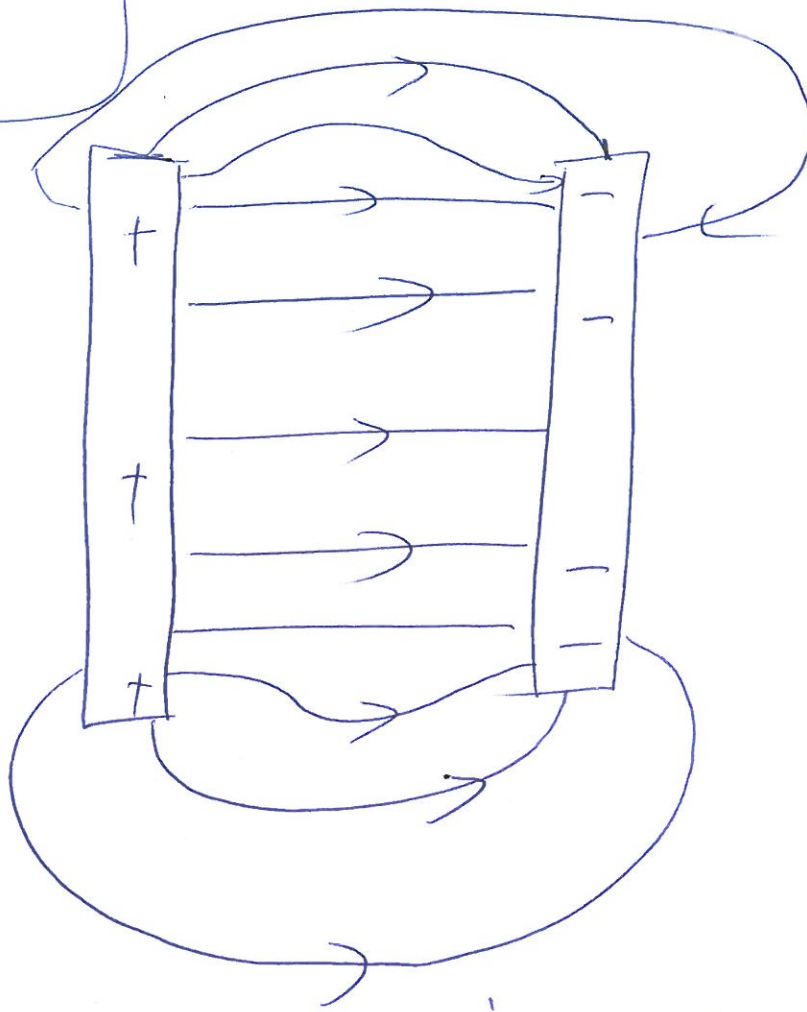
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visualizing the field lines  
is that field lines  
are always perpendicular  
to the surfaces



The shape of such a field  
can often be estimated by  
interpolation.

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This is sort of a parallel plate capacitor.

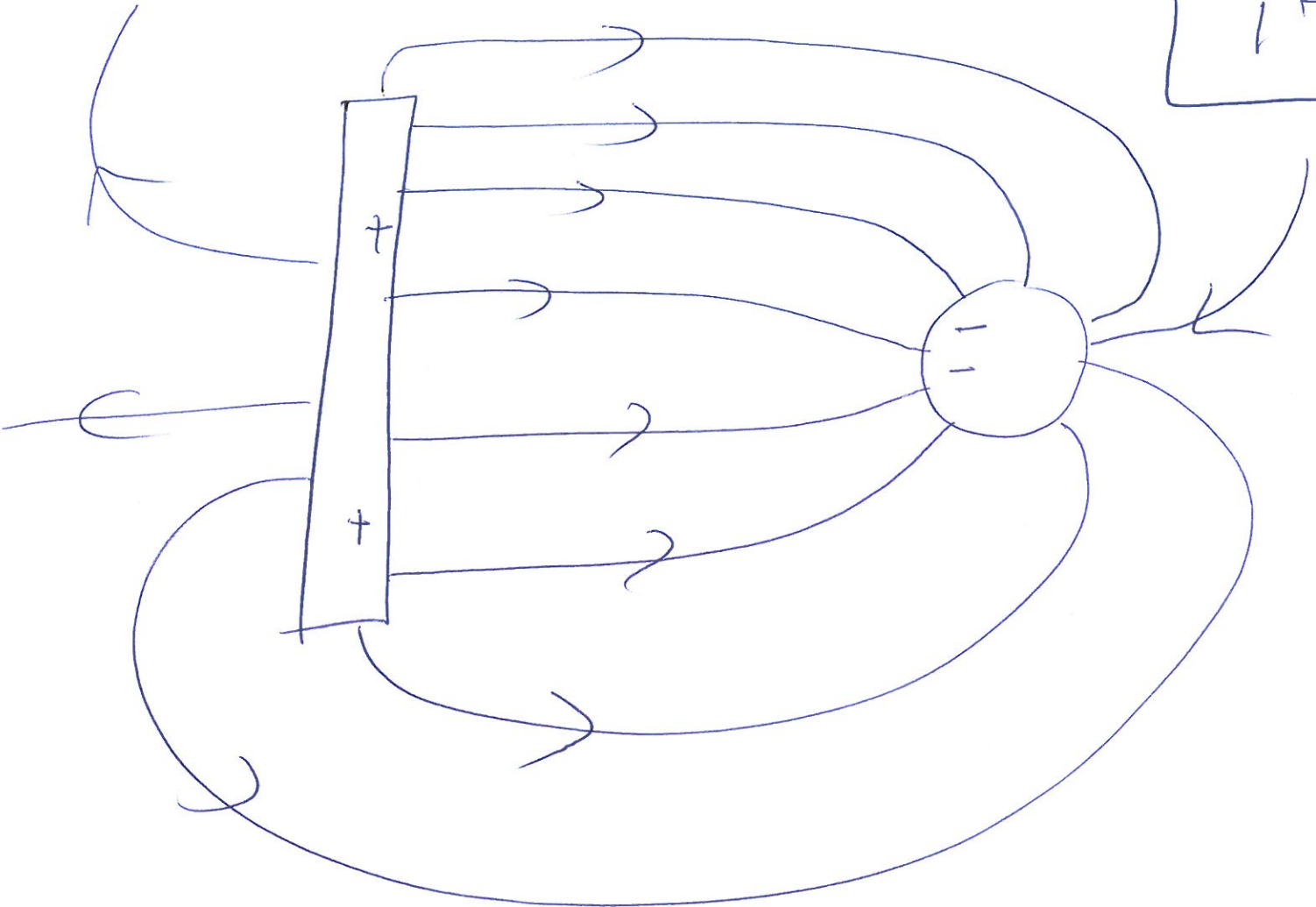
The field is strong between the plates and weak outside.

In the center region between the plates,

the  $E$ -field is nearly uniform

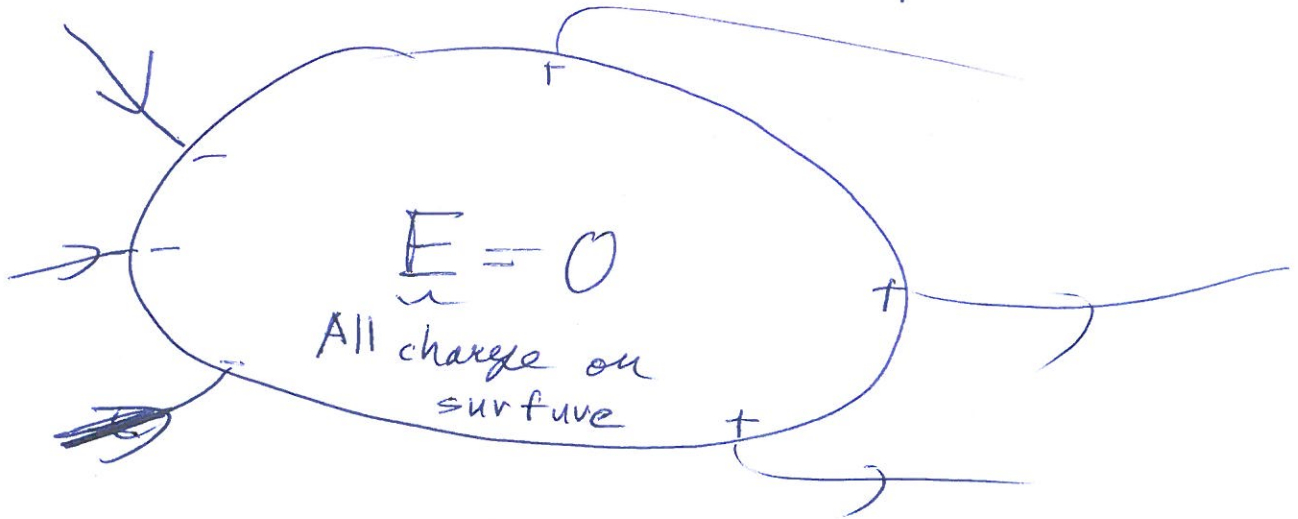
— i.e., nearly constant in direction and magnitude





e)  $\vec{E}$  - field inside  
an electrostatic conductor

~~no char~~  
no macroscopic currents

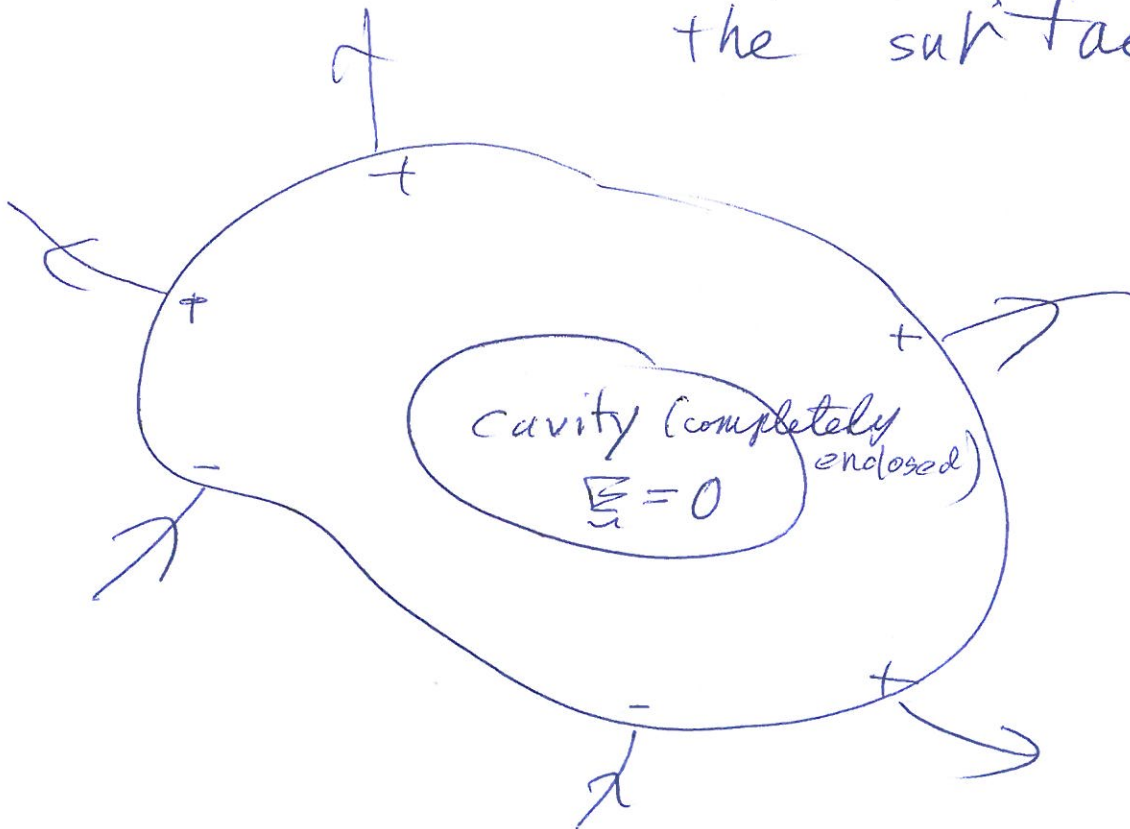


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Microscopic fields of electrons and atoms vary strongly but average to zero over macroscopic distances.

The macroscopic  $\mathbf{E}$ -field is zero inside and over macroscopic regions the inside is neutral.

All net charge or separated charge is on the surface.



Strictly  $\underline{E=0}$   
in cavity

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only when the  
situation is electrostatic

No currents, no  
changing external  
fields

But in practice

the field is often nearly  
zero inside even

when there are external  
changing  $E$ -fields

and when the cavity  
has holes to the  
outside.

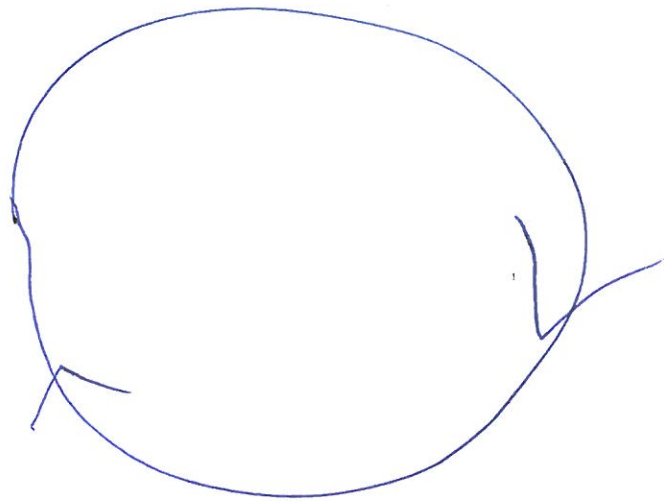
20)

As a ~~device~~ device  
such a cavity is  
a Faraday ~~shield~~ Cage  
and is use to  
shield from external  
E-fields

- if grounded the cage  
will shield the outside  
world from fields in  
the cavity caused  
by charges put there.

~~\*)~~

Faraday law - induced  
E-fields caused by  
changing Magnetic  
fields



These form closed loops.

or extend to infinity

(Wik: field line)

No charges cause these (in a direct sense)

## 4) Potential

— some  $E$ -field structures, but

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not all

(Not Faraday law-induced  $\mathbf{E}$ -fields — without being tricky)

allow potential energy to be defined.

Potential energy (PE)

is the energy of position associated with a charge located in the  $\mathbf{E}$ -field,

at a more basic level this is energy of the  $\mathbf{E}$ -field structure,

but that is  
a tricky way  
to deal with the  
energy

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- the  $\mathbf{E}$ -field structure energy is ~~all~~ always there
- $PE$  is a quick way to deal with that energy when  $PE$  can be defined.

Potential is  $PE$  per  
(symbol  $V$ ) unit  
change.

So potential is NOT  
something associated  
with ~~the charge~~  
particular charges

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but is associated  
with the  $\mathbf{E}$ -field  
itself.

It's very useful (and  
arguably completely correct)  
to view potential as  
being landscape with  
hills and valleys  
and planes.



of course the height of  
this landscape is in  
a abstract space

— at every point in the  
region where the potential  
is definable there  
is a "height"



Potential is, in fact,  
a scalar field

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given the symbol  $V$  { It also  
is a  
variable

and the MKS unit  
is the volt (symbol  $V$ ) { Remark  
since  
a unit.

(potential is often called  
voltage, but not  
in physics books)  
~~and voltage actually~~

The zero point of potential  
is arbitrary and is chosen  
for convenience.

Only changes in potential  
affect anything  
(aside from potential  
itself).

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If a <sup>point</sup> charge  $q$  goes through a potential change  $\Delta V$ ,

then there is ~~an~~ PE energy change

$$\Delta PE = q \Delta V$$

$$\text{If } q \Delta V > 0,$$

Going "uphill"  
for a +ve charge

energy goes into  
PE

(into electric field structure)

$$\text{If } q \Delta V < 0,$$

energy comes out of PE

(out of E-field structure)

Going "downhill"  
for a positive charge.

Where does the PE [27]  
energy come from or  
go to?

That depends.

If only the electric force  
is present, the energy  
comes from the ~~particles~~  
charges' kinetic energy  
or goes to it.

In circuits, the PE can  
go into waste heat  
or mechanical work  
or other things.

It can come from  
an EMF (we'll discuss  
later)  
or other things.

2 Sa

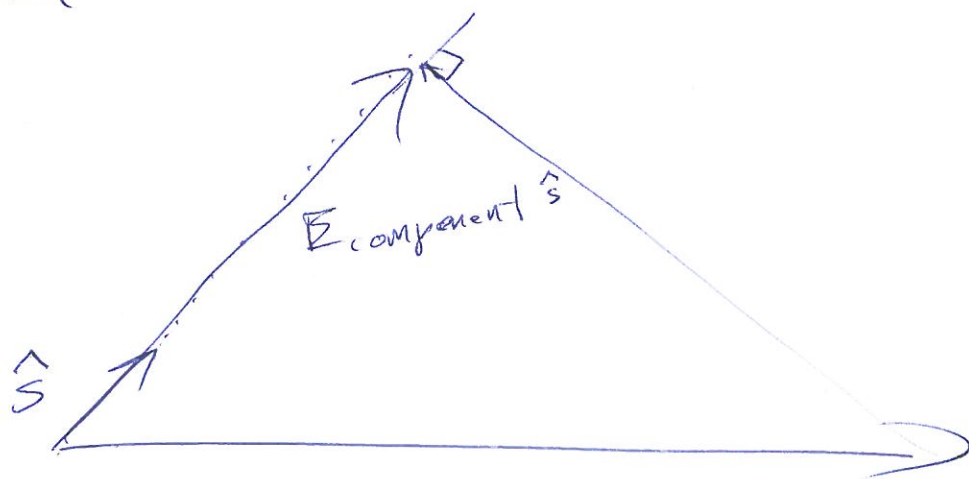
## 5) Potential & Electric Field

Potential is derivable  
from the  $\mathbf{E}$ -field  
and vice versa.

Here we only need the  
equation

$$E_{\text{component}} = \mathbf{E} \cdot \hat{s} = - \frac{dV}{ds} \approx \frac{\Delta V}{\Delta s}$$

is  $\hat{s}$   
direction



Note  $\mathbf{E}$  and  $\mathbf{E}_{\text{com}} \hat{s}$  have  
extend ~~into~~ in abstract space only.

Getting  $V$  from  $\mathbf{E}$

takes an integral

$$\Delta V_{ab} = - \int_a^b \mathbf{E} \cdot d\mathbf{s}$$

differential displacement

dot product

The minus sign is mathematically annoying, but is physically clarifying

Potential hill  $V$  up

$\mathbf{E}$  is actually ~~the fastest~~ points down the fastest path of descent at any point.



the  $\mathbf{E}$ -field points down

the hill analogous to gravity

- Going uphill against the

28c

$\vec{E}$  - field increases  
the potential

For a differential change

$$dV = - \vec{E} \cdot d\vec{s}$$
$$= - \vec{E} \cdot ds \hat{s}$$

$$\text{or } \vec{E} \cdot \hat{s} = - \frac{dV}{ds}$$

and so we have  
recovered the  
result of p. 28a and  
verified it

Rate of decrease of  $V$  with distance is  
most rapid along the path of  $\hat{s}$  aligned  
with  $\vec{E}$

In vector calculus  $\vec{E} = -\nabla V$   
where  $\nabla V$  is the gradient of  $V$ .

Ideally to measure

~~E~~ component

in  $\hat{s}$  direction

you should measure

the derivative  $\frac{dV}{ds}$

of  $V$  in the  $\hat{s}$  direction.

In our experiment,

we approximate

$$\frac{dV}{ds} \approx \frac{\Delta V}{\Delta s}$$

finite  
change  
in  $\Delta V$   
over  
a finite  
displacement.

$$\text{If } \frac{dV}{ds} = 0$$

then  $E_{\text{component}} = 0$   
in  $\hat{s}$  direction

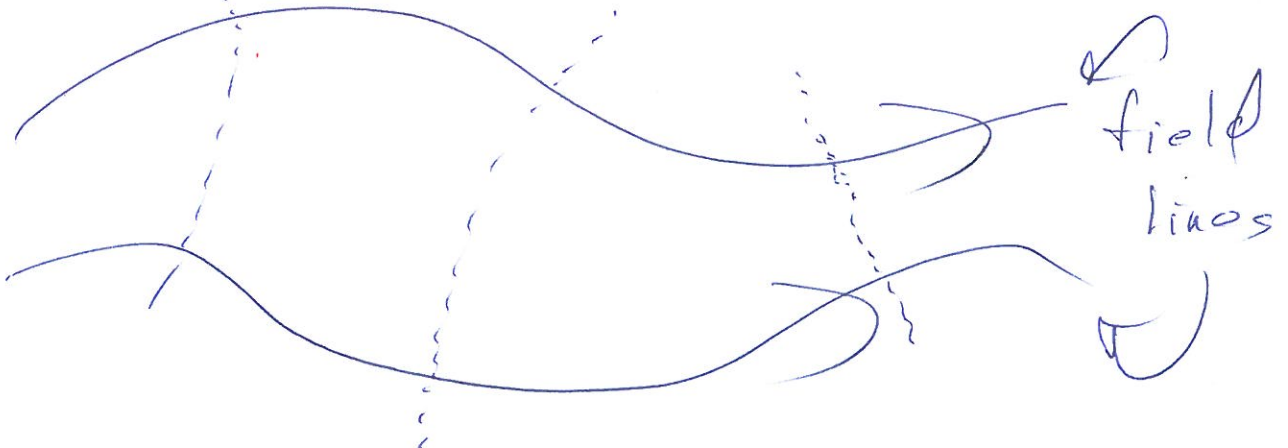
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The  $\vec{E}$  ~~vector~~ vector is perpendicular to the direction where  $V$  is constant.

So surfaces of constant

$V$   
or ~~equipotentials~~ equipotentials

are always perpendicular to the  $\vec{E}$ -field and the ~~equipotentials~~ field lines

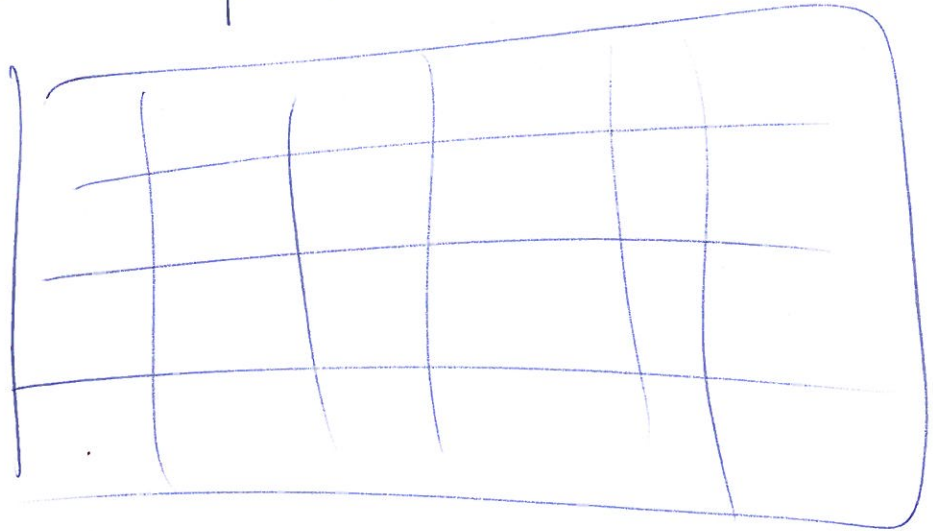




# 6) Our Experiment

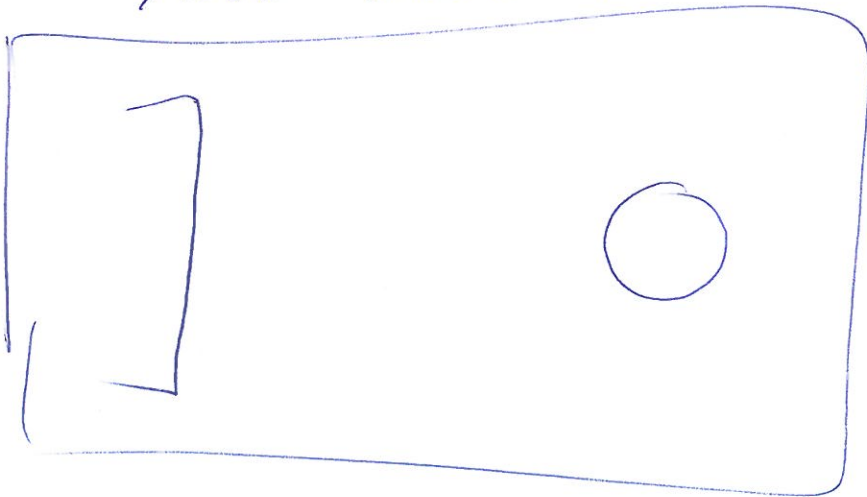
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→ sheet of  
Graph paper



~~→ mark~~

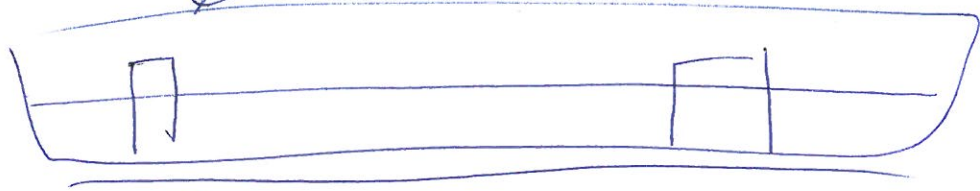
— Trace on it two plate  
locations → so  
you know where to



keep  
the  
plates  
— they  
are  
light  
and  
easily  
moved.

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Plates

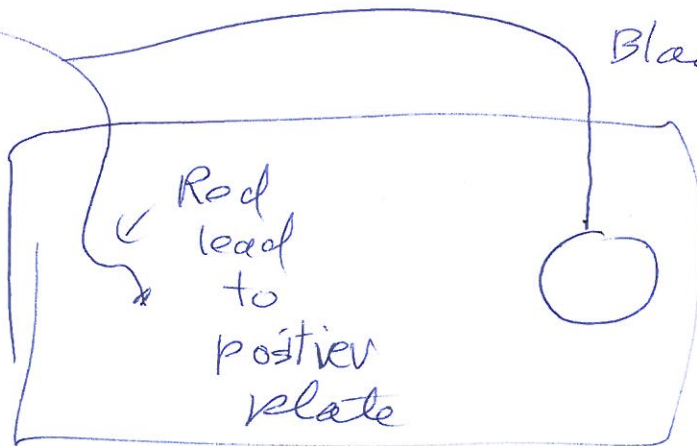


Tray

~~about~~  
about  
half  
full  
of water

Graph paper with tracings

— one straight plate  
and one funny  
shaped (but  
not too large)  
plate works well.



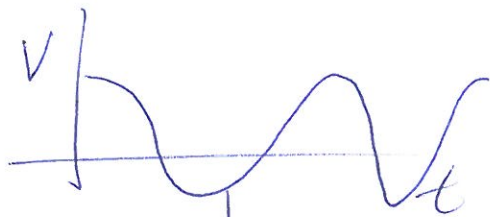
Black lead  
to  
negative  
plate.

Rod  
lead  
to  
positive  
plate

(nothing safer than  
putting live wires  
in water)

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The function generator  
provides an  
AC potential

to the plates. 

— They are nearly  
equipotentials

at an instant in time

charge is moving in  
conductors, but  
resistance is low  
and so nearly equipotential  
in and on conductors.

34)

~~The plates create~~

The change in the  
plates creates an  
E-field

which because the signal  
is AC

is actually varying  
in time

but the Root Mean Square

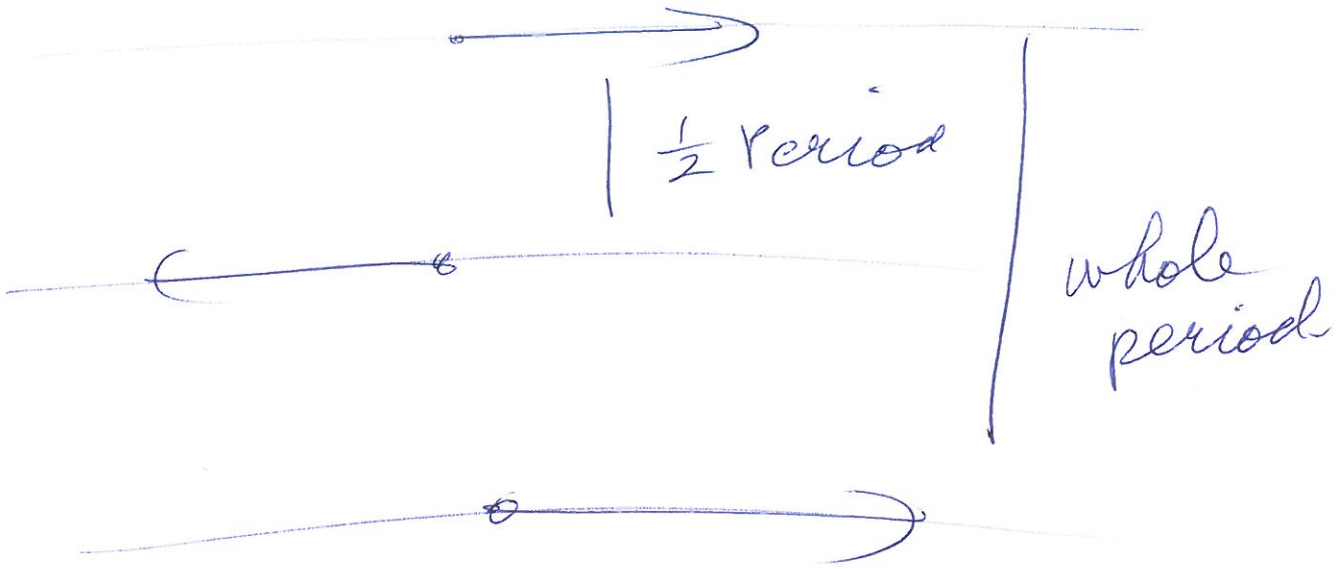
(RMS) magnitude

at every point

is constant

and direction is

constant except  
for sense flips

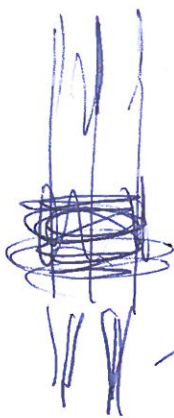


So the field lines  
 stay constant  
 except for direction sense

We arbitrarily say  
 the field lines  
 run from the  
red connected plate  
 to the black connected plate.

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We use  
a multimeter  
to measure  
 $\Delta V$   
over a fixed  $\Delta S$



prongs of multimeter  
taped together.

The multimeter is set  
to potential measurement

AC

select

push select

to get the "V" symbol

# The multimeter

It autoscales and check the units: Volts or millivolts.

Reads RMS potential difference (so no sign)

Question Why do we need the water

Answer to measure potential the multimeter must . . . .

Tap water has lots of ions in it.

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Question

Why use AC?  
Wouldn't DC work?

Answer

Well AC  
lets us use  
the headsets  
and hear  
the AC.

And well the  
ions would  
lead to

u u u

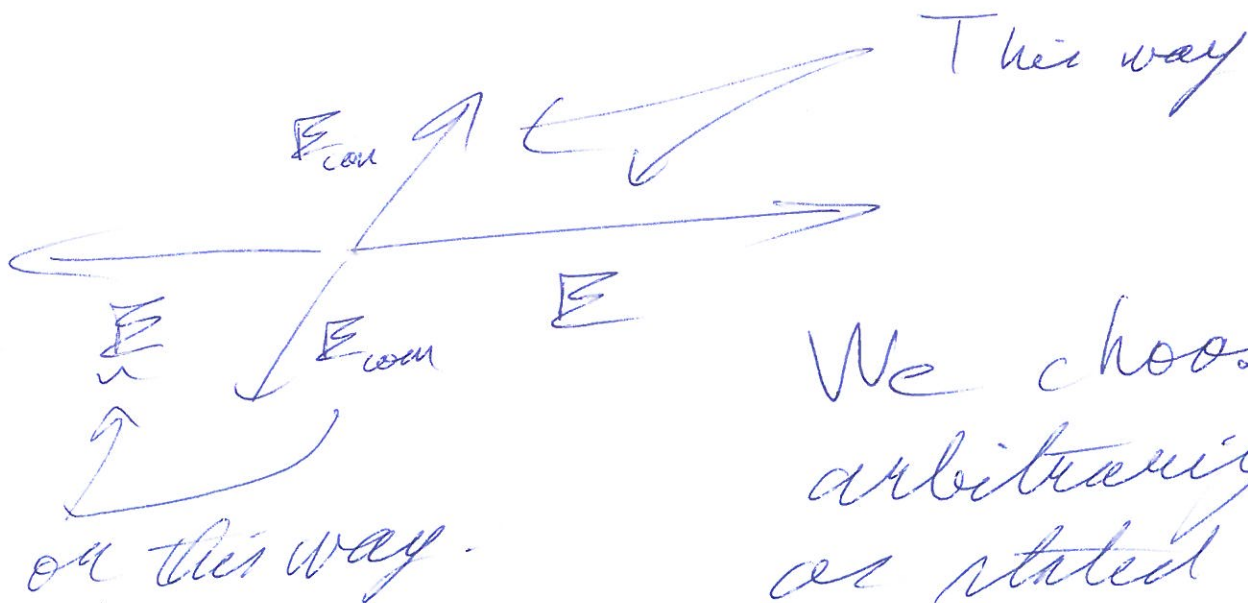


Because we use

AC and  $\Delta V$   
is just the RMS  
value of a time  
varying field

$$|E_{\text{com}}| \approx \frac{\Delta V}{\Delta S}$$

We don't get the  
sign of the component.



We choose  
arbitrarily  
as stated  
above on p. 35

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Red positive

Black negative

traditional

choice

in

electric

circuits

- so our choice

of red

and black connections

decides the field

direction.