

Chemistry in Athena++

Munan Gong

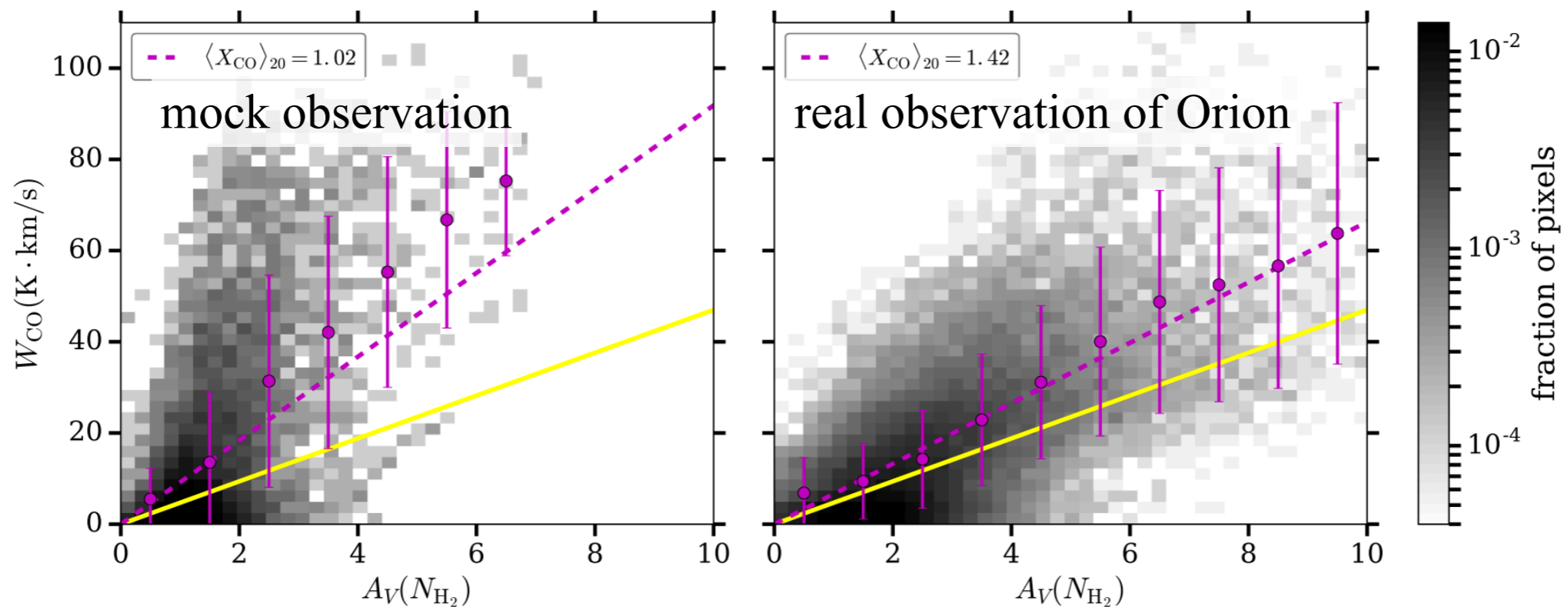
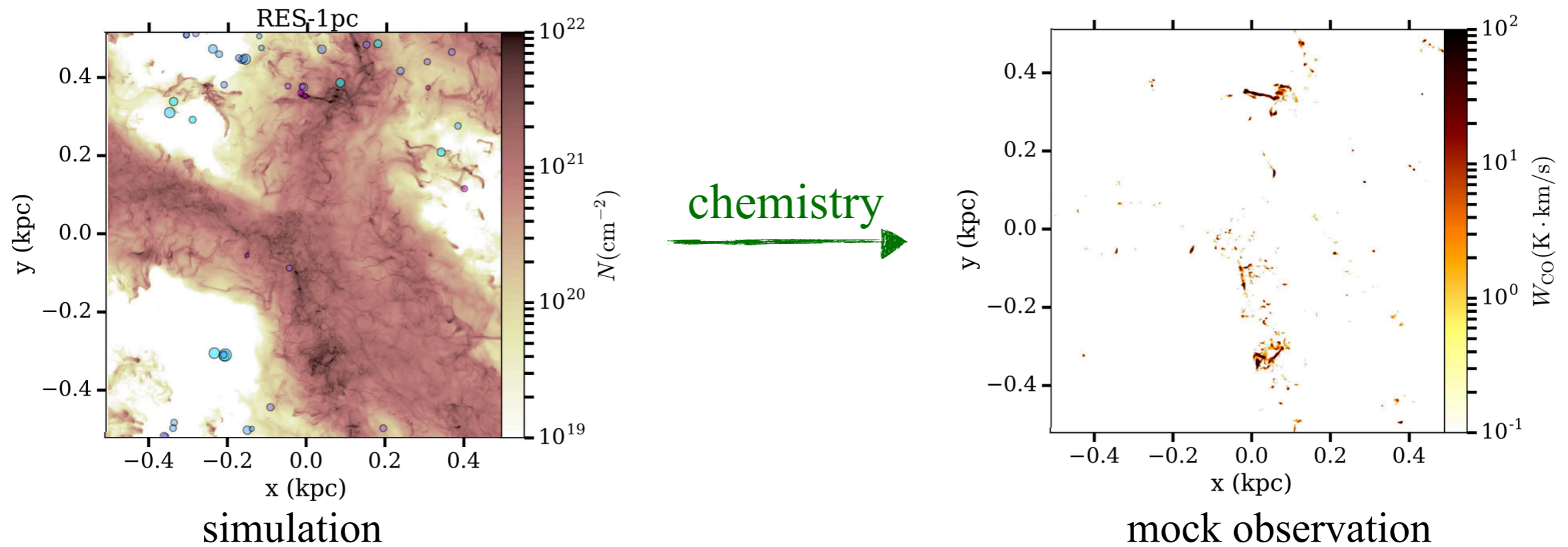
Max Planck Institute for Extraterrestrial Physics (MPE)

Athena++ workshop, UNLV, March 2019



Max-Planck-Institut für
extraterrestrische Physik

An application of chemistry



Equations

Concentration for species i : $s_i = \frac{\rho_i}{\rho}$

$$\frac{\partial s_i}{\partial t} = -\frac{1}{\rho} \mathbf{v} \cdot \nabla(\rho s_i) + K_i$$

↑
chemical reaction rates
 $K_i(\mathbf{s}, \rho, T, G, \dots)$
 G : radiation field

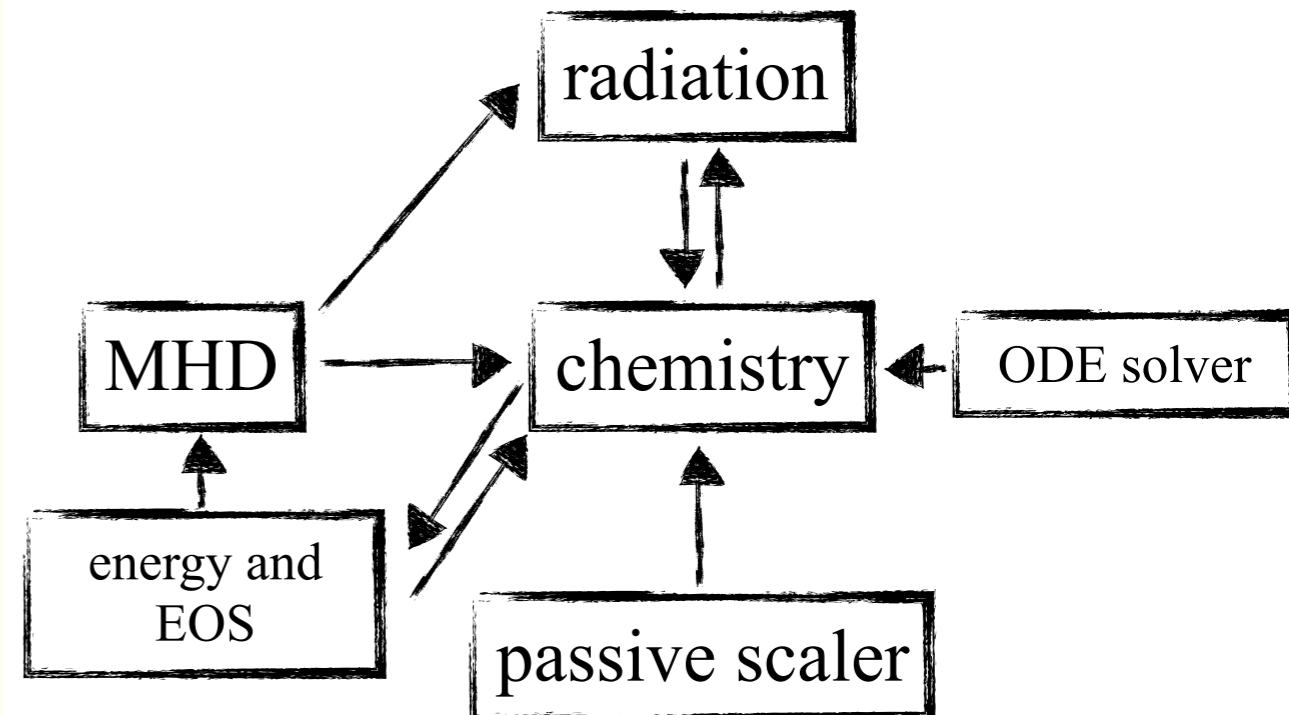
$$\frac{\partial}{\partial t} \left[\left(\frac{1}{2} \rho v^2 + \frac{P}{\gamma - 1} \right) + \nabla \cdot \left(\frac{1}{2} \rho v^2 + \frac{\gamma}{\gamma - 1} P \right) \mathbf{v} \right]$$

$$= \Gamma - \Lambda$$

↑
heating and cooling
 $\Gamma, \Lambda(\mathbf{s}, \rho, T, G)$

$$P = \frac{R}{\mu} \rho T$$

↑
mean molecular weight $\mu(\mathbf{s})$



Post-processing chemistry

Concentration for species i : $s_i = \frac{\rho_i}{\rho}$

$$\frac{\partial s_i}{\partial t} = -\frac{1}{\rho} \mathbf{v} \cdot \nabla (\rho s_i) + K_i$$

\uparrow
 chemical reaction rates
 $K_i(\mathbf{s}, \rho, T, G, \dots)$
 G : radiation field

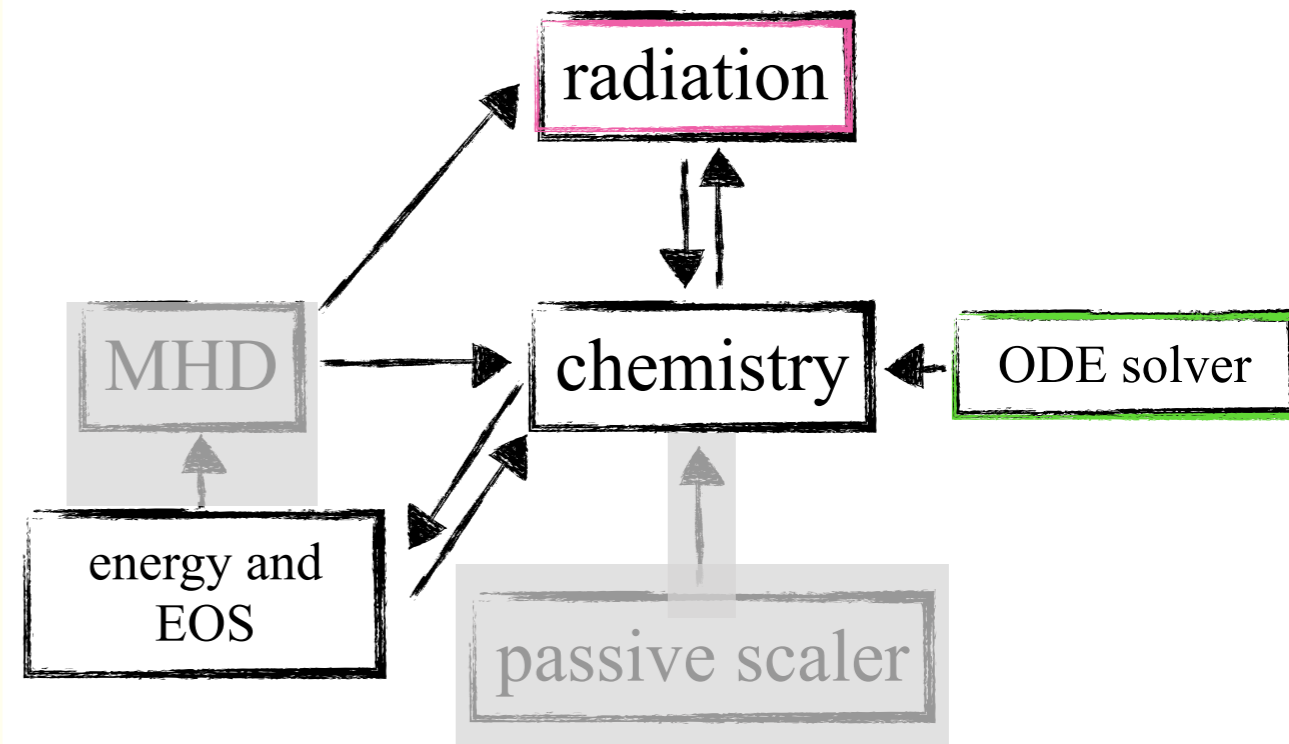
$$\frac{\partial}{\partial t} \left[\left(\frac{1}{2} \rho v^2 + \frac{P}{\gamma - 1} \right) + \nabla \cdot \left(\frac{1}{2} \rho v^2 + \frac{\gamma}{\gamma - 1} P \right) \mathbf{v} \right]$$

$$= \Gamma - \Lambda$$

\uparrow
 heating and cooling
 $\Gamma, \Lambda(\mathbf{s}, \rho, T, G)$

$$P = \frac{R}{\mu} \rho T$$

\uparrow
 mean molecular weight $\mu(\mathbf{s})$



$$\frac{ds_i}{dt} = K_i$$

$$\frac{dT}{dt} = \frac{\Gamma - \Lambda}{c_v}$$

$$G = G(\mathbf{s}, \rho)$$

Running chemistry on Athena++

- Download CVODE library

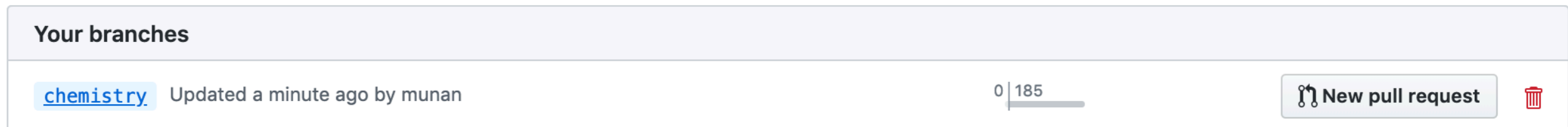
<https://computation.llnl.gov/projects/sundials/cvode>



SUNDIALS: SUite of Nonlinear and Differential/ALgebraic Equation Solvers

CVODE

- Checkout the chemistry branch on Athena++ GitHub page



- Configure

```
./configure.py -pp --chemistry=gow16 --radiation=six_ray --cvode_path=/usr/local -mpi ...
```

post-processing flag
(skip the MHD task-list)

chemical network

Radiation solver
(six_ray, loc_jeans, const)

CVODE library path

Radiation and chemistry
are parallelized

- Regression tests

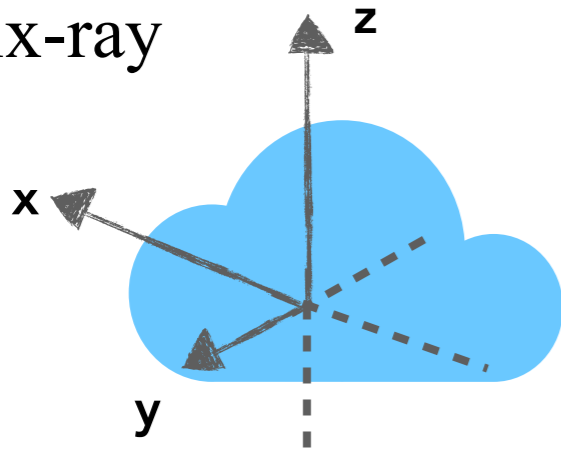
```
./run_tests.py chemistry (problem generator that reads Athena4.2 VTK output)
```

Current code implementations

- CVODE

Dense matrix solver: computational cost $\sim N_s^3$

- Six-ray

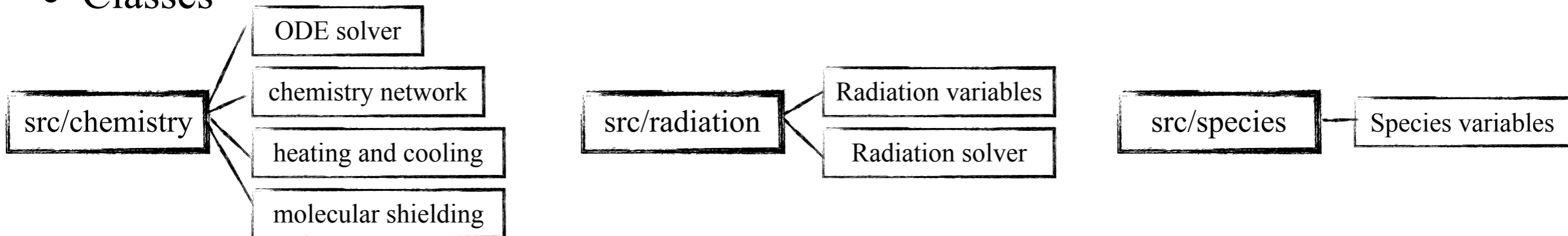


$$G = \frac{1}{6} \sum G_i$$

$$G_i = G_0 \exp(-\sigma N_i)$$

Fast compared to chemistry, pretty good approximation for the turbulent ISM.

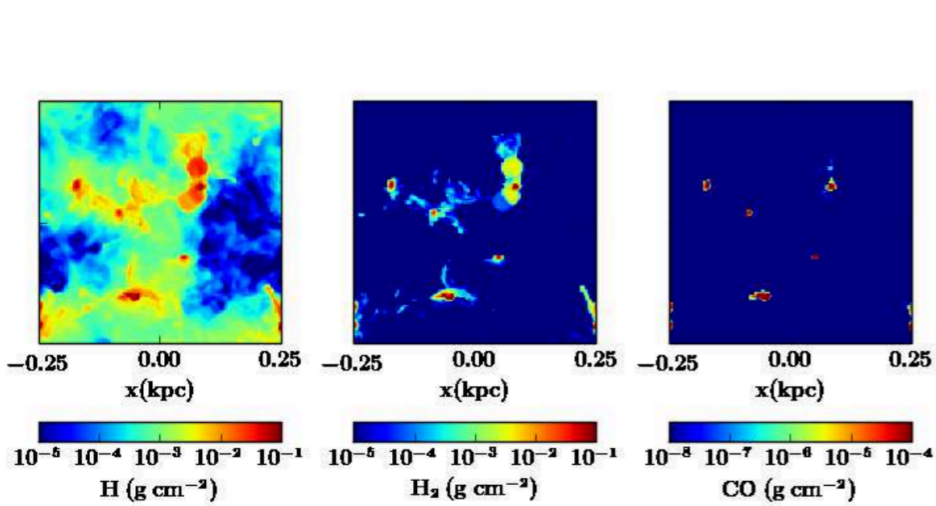
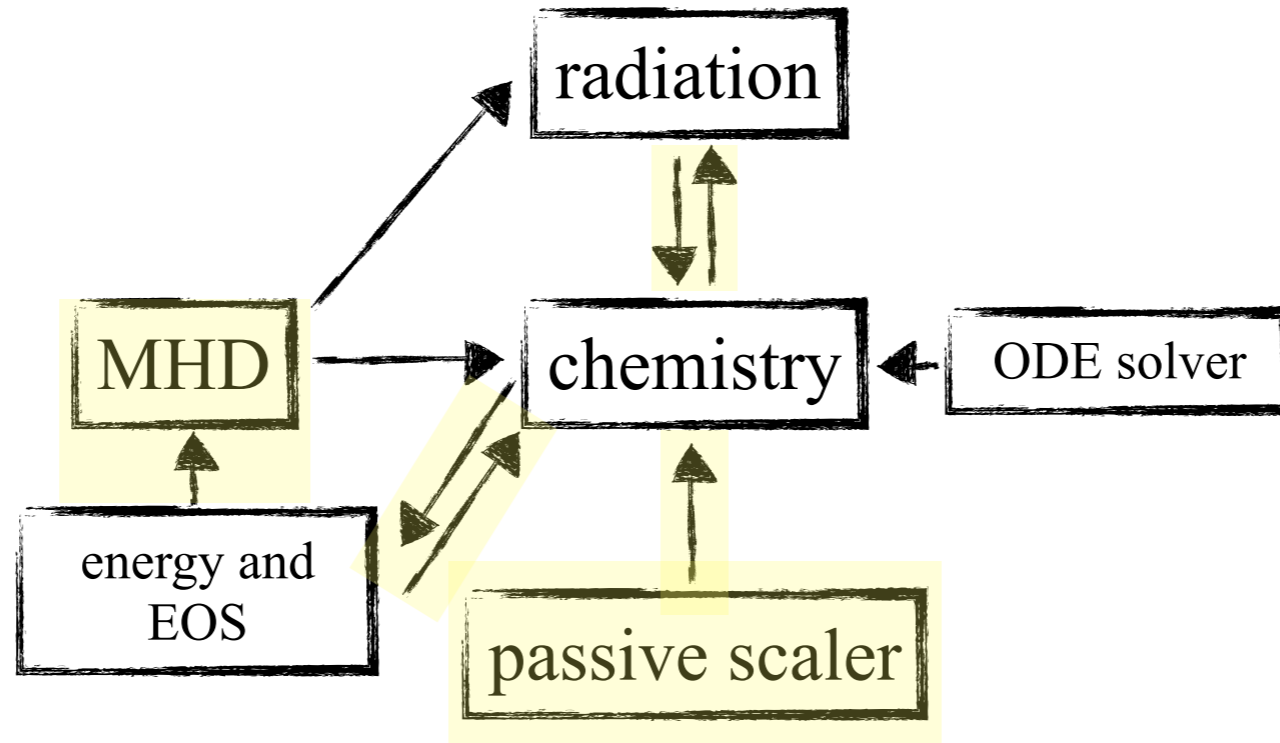
- Classes



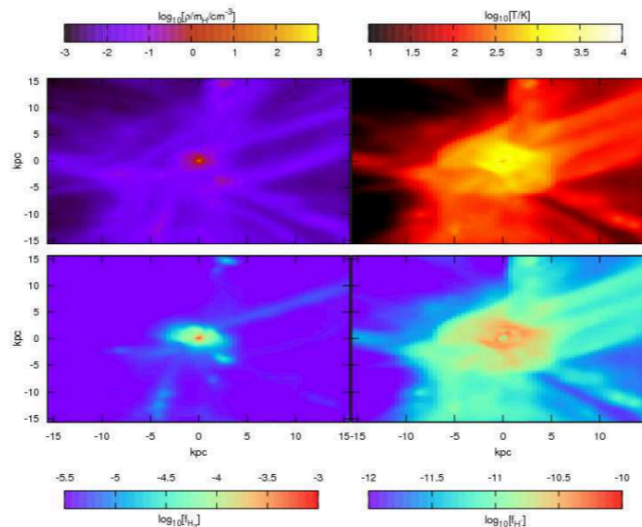
- Task-list



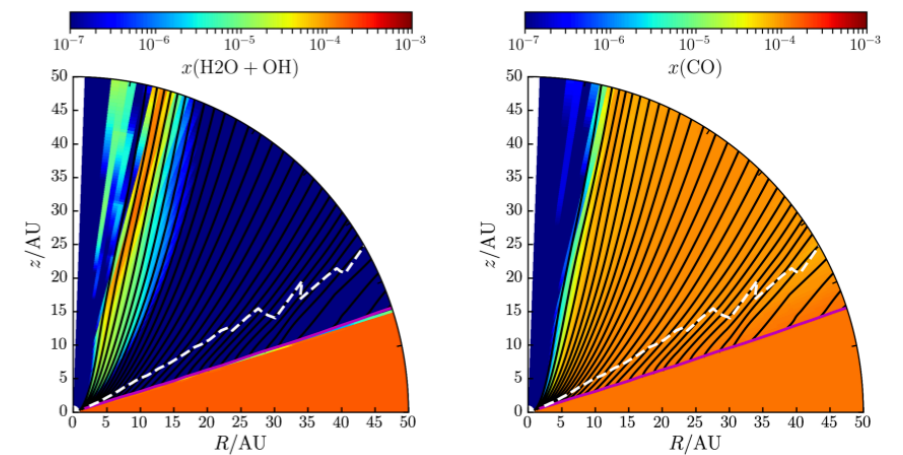
The goal: general time dependent chemistry



Walch+ 2014, FLASH



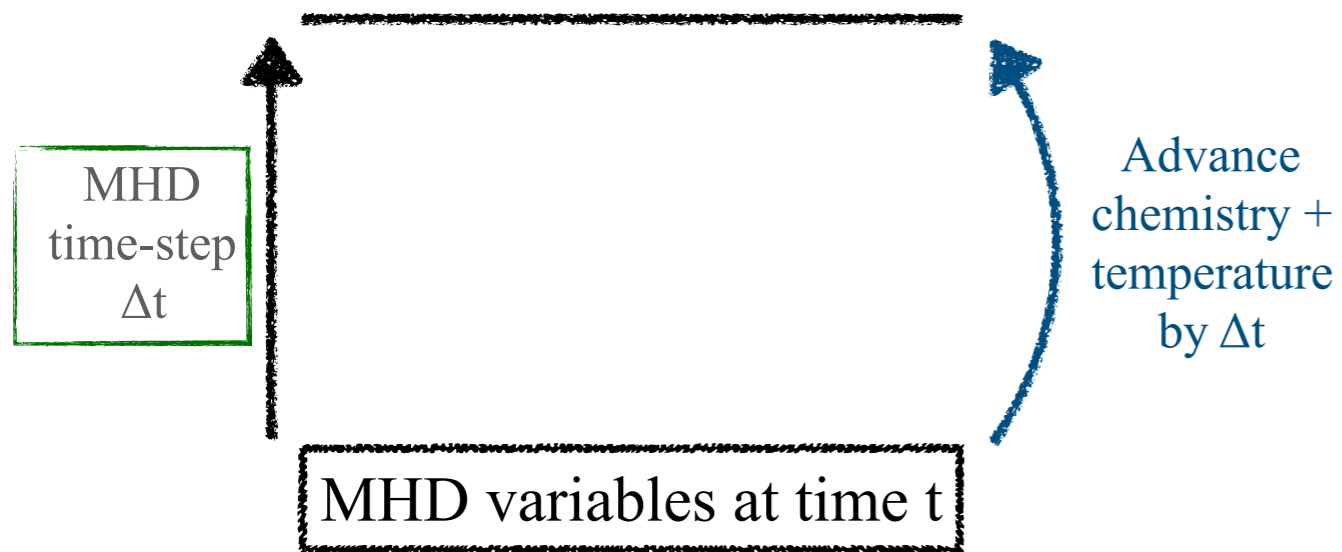
Grassi+ 2012, KROME



Wang+ 2018, Athena++

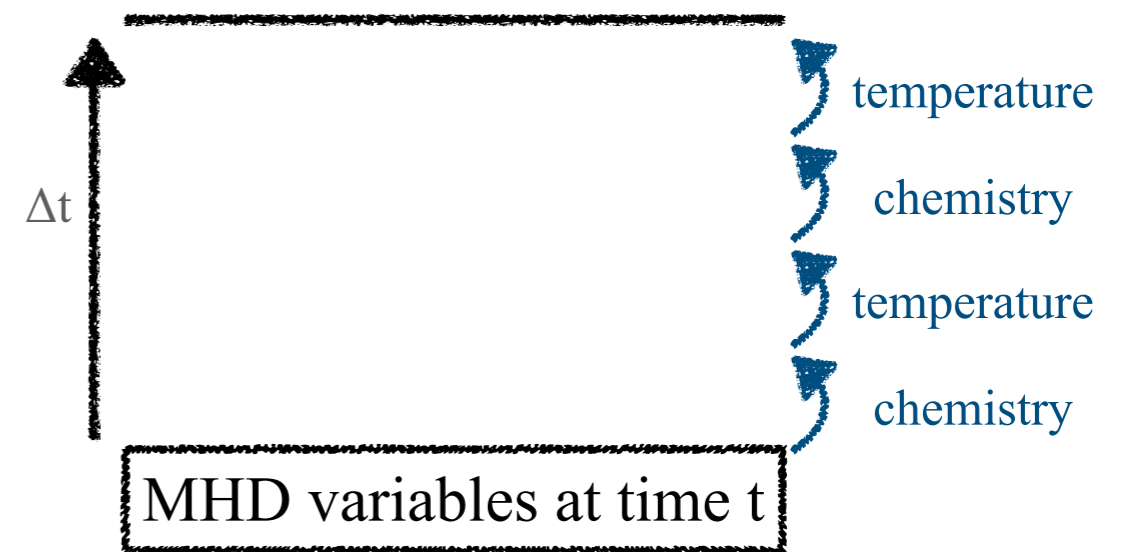
Towards time dependent chemistry

- Passive scaler, advection of chemical species
 - Merge the species class with the **passive scaler class**.
 - Conservation of elemental abundances: **normalise the fluxes in the advection step** (Glover+ 2010).
- Heating and cooling: the energy equation and EOS



Same as current post-processing implementation
(Grassi+ 2012, Wang+ 2017)

Shall we limit Δt according to heating and cooling rates?



Solve chemistry and temperature separately, sub-cycling: might be faster (Glover+ 2010, Walch+2014)

- Radiation

- Do we simply update radiation field after chemistry (current implementation and literature), or do we need to iterate between chemistry and radiation (for H_2 self-shielding)?

- Performance: cost function for Meshblocks, GPU, AMR

Summary

$$E = K_0 t + \frac{1}{2} \rho v t^2$$

ALL KINEMATICS
EQUATIONS

$$K_n = \sum_{i=0}^{\infty} \sum_{\pi=0}^{\infty} (n - \pi)(i + e^{\pi - \infty})$$

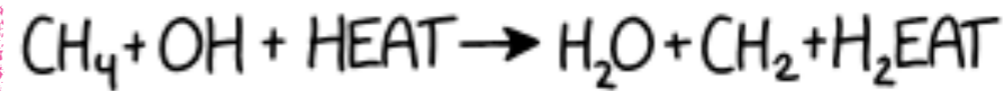
ALL NUMBER
THEORY EQUATIONS

$$\frac{\partial}{\partial t} \nabla \cdot \rho = \frac{8}{23} \iint \rho ds dt \cdot \rho \frac{\partial}{\partial \nabla}$$

ALL FLUID DYNAMICS
EQUATIONS

$$|\psi_{x,y}\rangle = A(\psi) A(|x\rangle \otimes |y\rangle)$$

ALL QUANTUM
MECHANICS EQUATIONS



ALL CHEMISTRY
EQUATIONS

$$\text{SU}(2) \text{U}(1) \times \text{SU}(U(2))$$

ALL QUANTUM
GRAVITY EQUATIONS

$$S_g = \frac{-1}{2\epsilon} i \delta \left(\hat{\epsilon}_{\alpha\beta} + \rho_{\epsilon} \rho_{\nu}^{abc} \cdot \hat{\eta}_{\alpha} \right) \hat{F}_{\alpha}^{\rho} a \lambda(\xi) \psi(0_{\alpha})$$

ALL GAUGE THEORY
EQUATIONS

$$H(t) + \Omega + G \cdot \Lambda \dots \begin{cases} \dots > 0 & \text{(HUBBLE MODEL)} \\ \dots = 0 & \text{(FLAT SPHERE MODEL)} \\ \dots < 0 & \text{(BRIGHT DARK MATTER MODEL)} \end{cases}$$

ALL COSMOLOGY EQUATIONS

$$\hat{H} - \psi_0 = 0$$

ALL TRULY DEEP
PHYSICS EQUATIONS