

Adaptive Ray Tracing

Jeong-Gyu Kim (Princeton)

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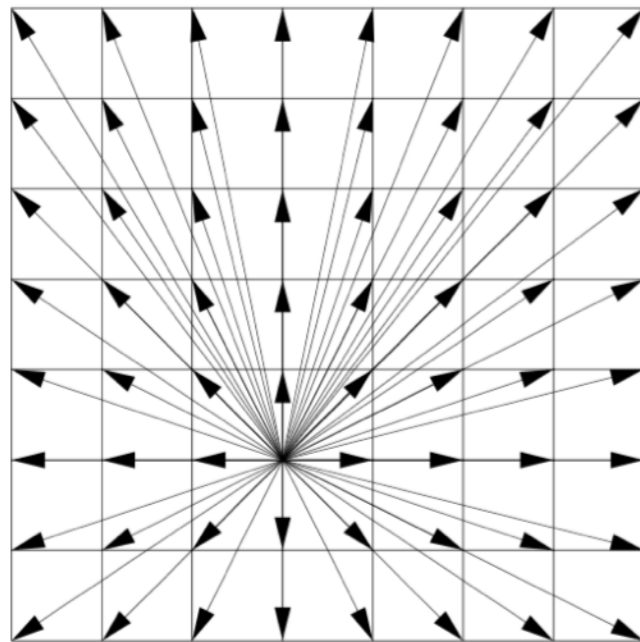
Characteristics Method for Point Source Radiative Transfer

- Solves RT equation along selected rays and computes radiation 4-force vector directly

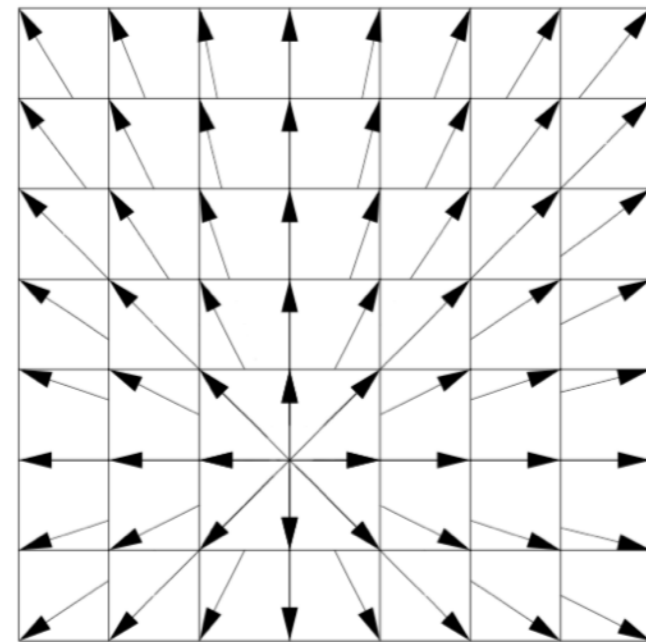
$$\frac{1}{c} \frac{\partial I_\nu}{\partial t} + \mathbf{n} \cdot \nabla I_\nu = \eta_\nu(\mathbf{n}) - \kappa_\nu(\mathbf{n}) I_\nu$$

$$c \begin{pmatrix} G^0 \\ \mathbf{G} \end{pmatrix} = \int d\nu \int d\Omega [\kappa_\nu(\mathbf{n}) I_\nu - \eta_\nu(\mathbf{n})] \begin{pmatrix} 1 \\ \mathbf{n} \end{pmatrix}$$

Long characteristics

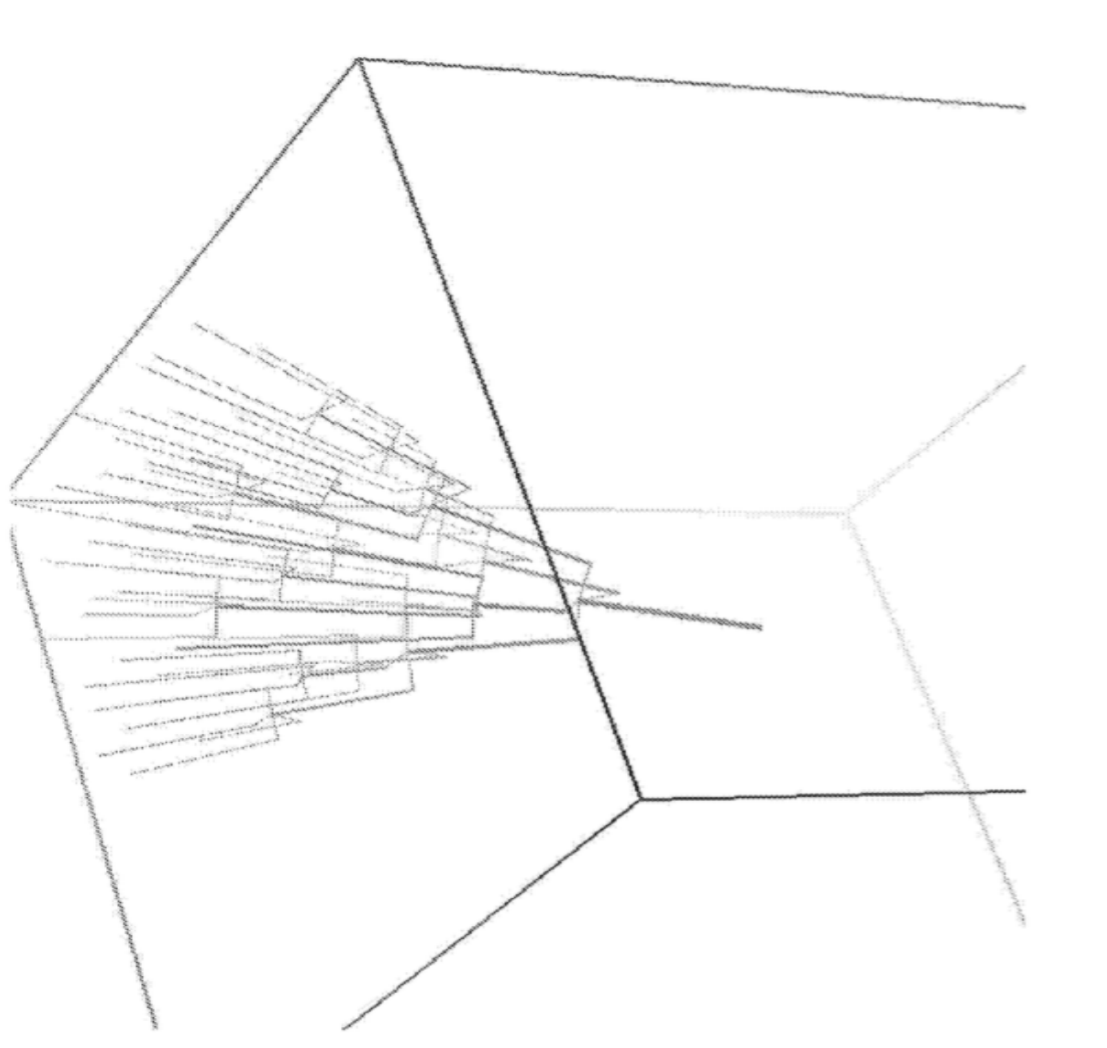


Short characteristics

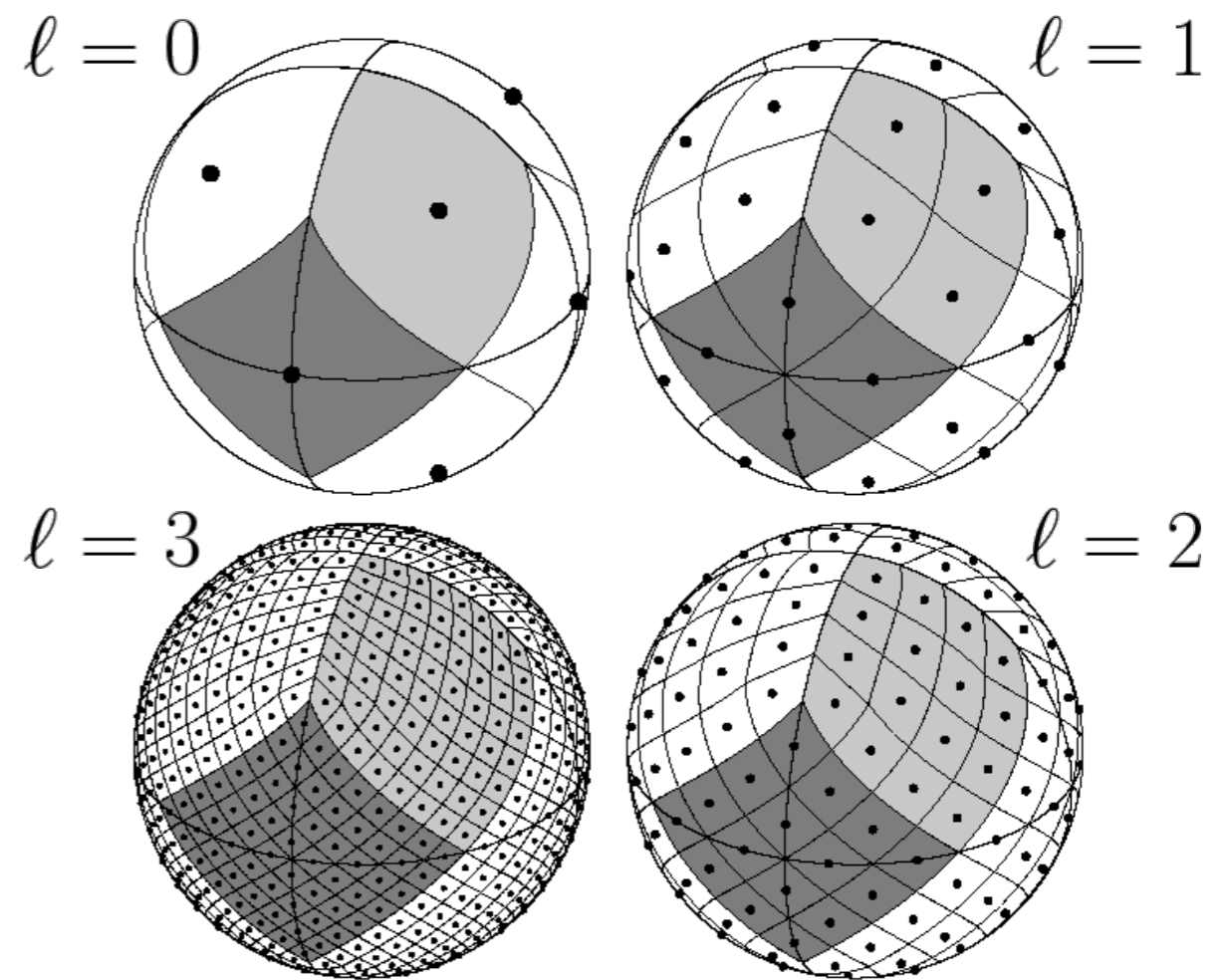


Adaptive Ray Tracing

- Spatially adaptive long characteristics
 - Split rays to match the angular resolution to that of grid cell
 - Angular discretization using HEALPix



Abel+02



Gorski 05

Pros and Cons

- Conservative of photon energy and momentum
 - Retains full information about the directionality of radiation flux
 - Best suited for UV radiation from a small number of massive stars
 - Photoionization/direct radiation pressure, coupling with chemistry
-

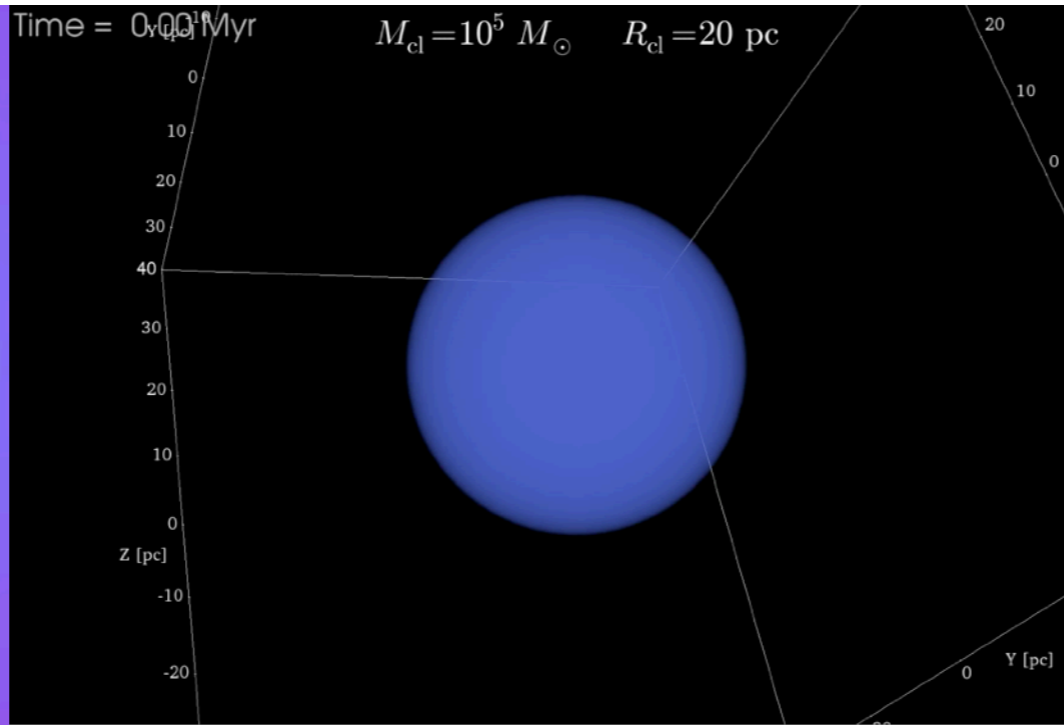
- Ill-suited to handling diffuse sources/scattering
- Computational cost scales as $N_{\text{src}} \times N_{\text{cell}} \times N_{\text{freq}} \times m_{\text{ray}}$.
 - In practice, cost depends on problem geometry, domain decomposition, and parallel algorithm
- Difficult to parallelize

Science Applications

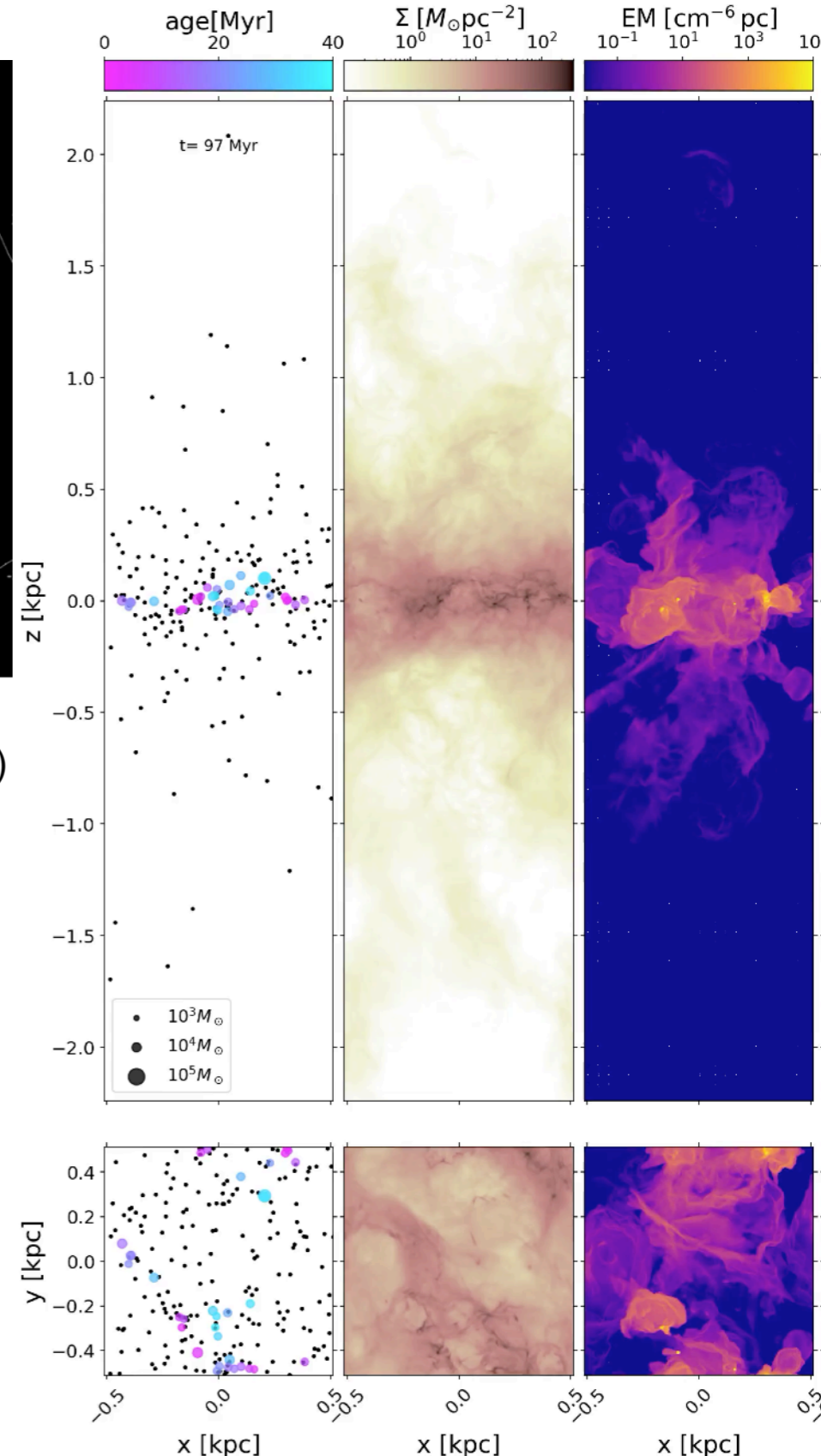
Rosen+16



Kim, J.-G.+18



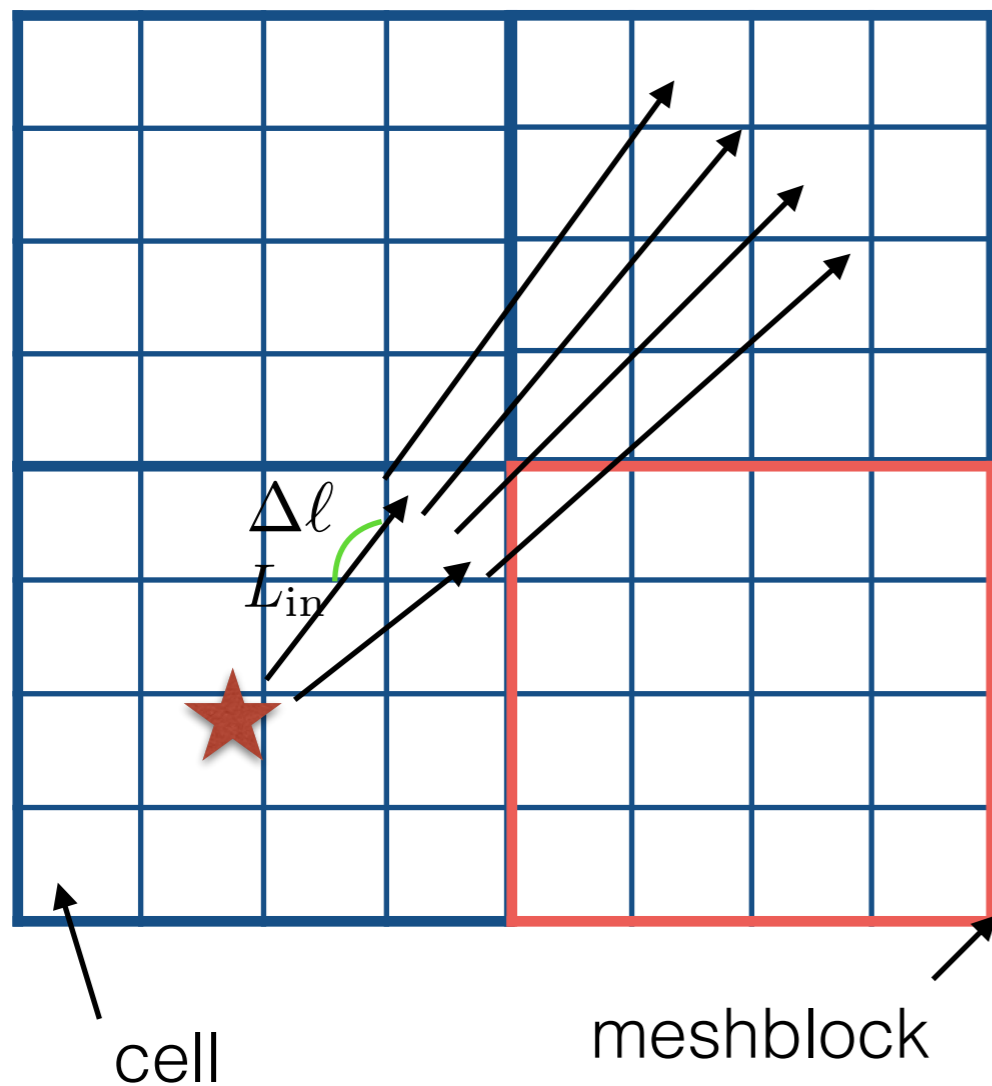
Kado Fong+19



- Massive star formation with radiation feedback (Rosen+16, 19)
- Destruction of molecular clouds (Kim, J.-G.+17, 18, 19)
- Post-processing kpc-scale galactic disk simulations TIGRESS (Kim, C.-G.+17,18)
 - Diffuse ionized gas (Kado Fong+19, in prep)
 - H_2 and X_{CO} (Gong+19, in prep)
- TIGRESS with ART (see also Peters+17)
- Escape of radiation (e.g., Wise+09, Kim, J.-h.+13)

Ray-cell Interaction

- Photon Packets (**PPs**) are transported radially outward from the source and attenuated by gas and dust.



$$\mathbf{n} \cdot \nabla I = -\chi I$$

$$\mathcal{E} = \frac{1}{c} \int I d\Omega = |\mathbf{F}|/c$$

$$\mathbf{F} = \int I \hat{\mathbf{n}} d\Omega = \hat{\mathbf{r}} L e^{-\tau(r, \hat{\mathbf{n}})} / (4\pi r^2)$$

$$\frac{\partial L_{\text{ray}}}{\partial r} = -\chi L_{\text{ray}}$$

$$\Delta L = L_{\text{in}} (1 - e^{-\Delta\tau})$$

opacity per length

$$\Delta\tau = \chi \Delta l$$

$$\mathcal{E} = \frac{1}{\chi \Delta V} \sum_{\text{rays}} \frac{\Delta L_{\text{ray}}}{c},$$

$$\mathbf{F} = \frac{1}{\chi \Delta V} \sum_{\text{rays}} \Delta L_{\text{ray}} \mathbf{n}_{\text{ray}},$$

Flow Chart

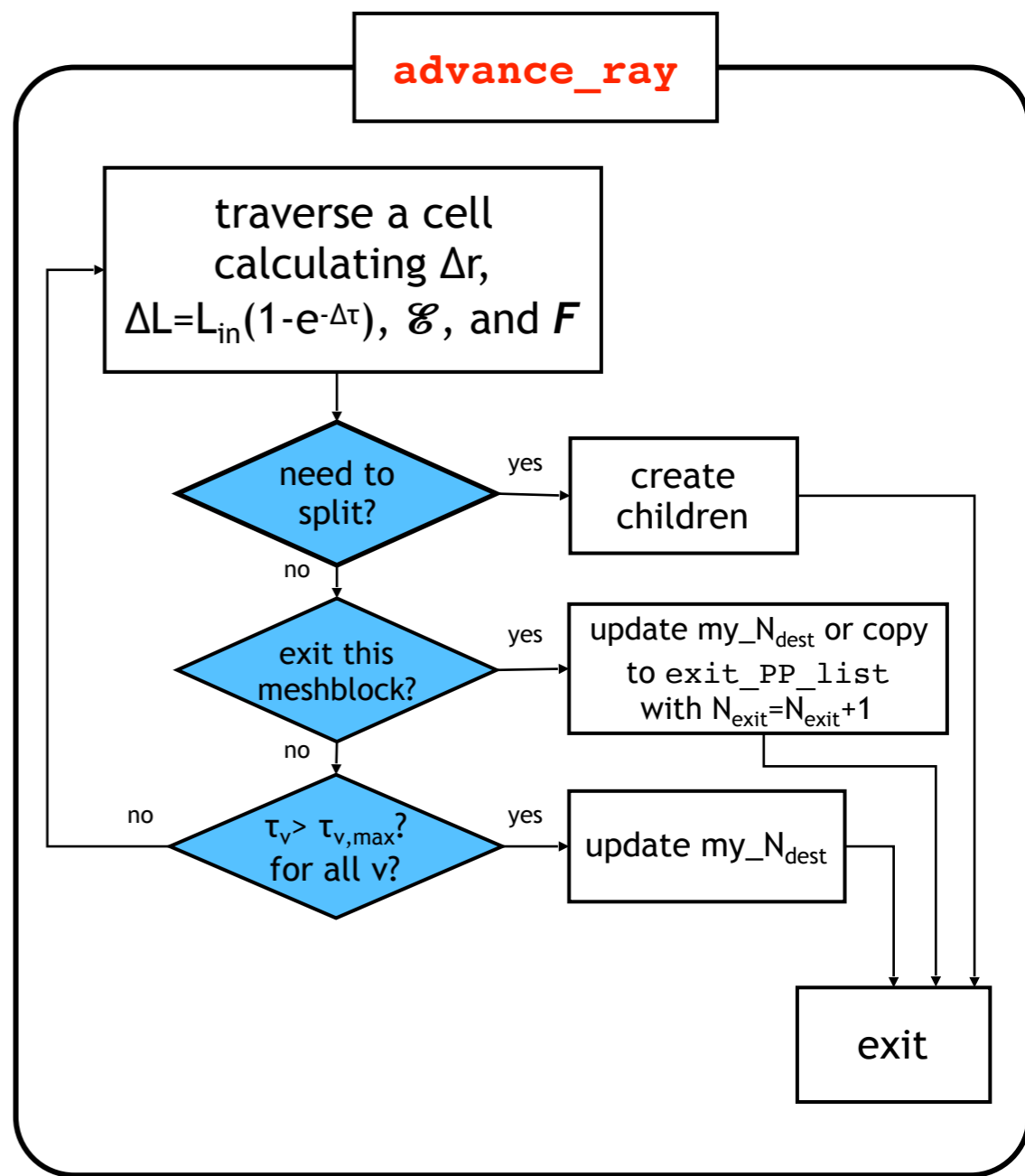
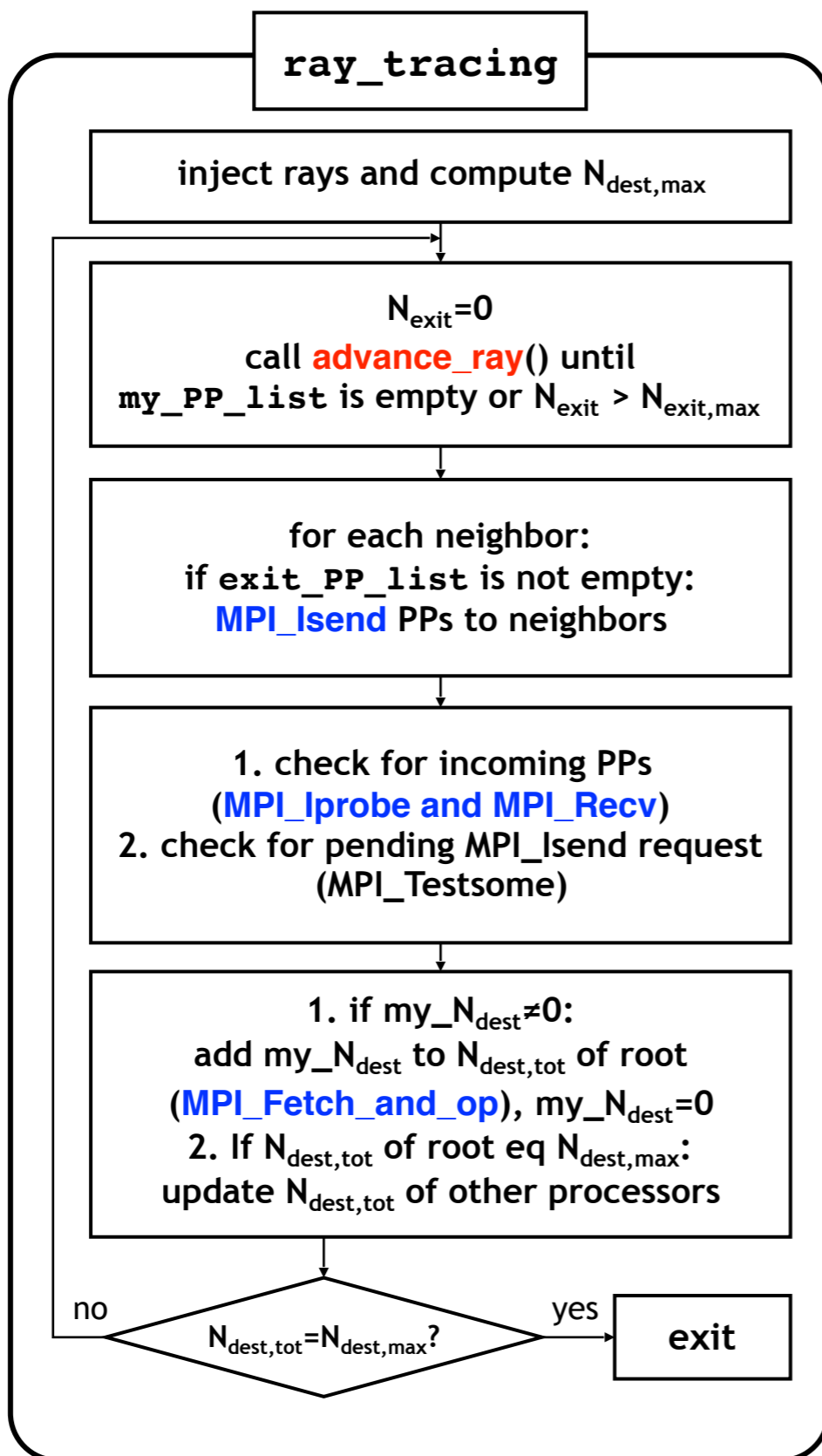
Inject rays

Ray tracing

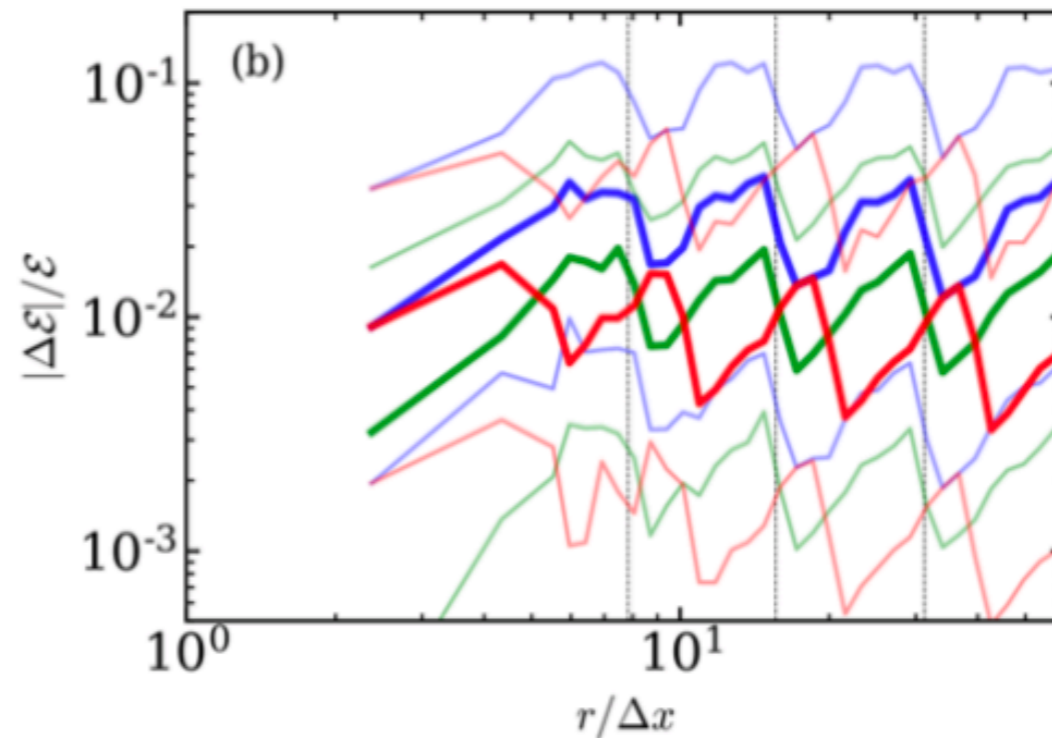
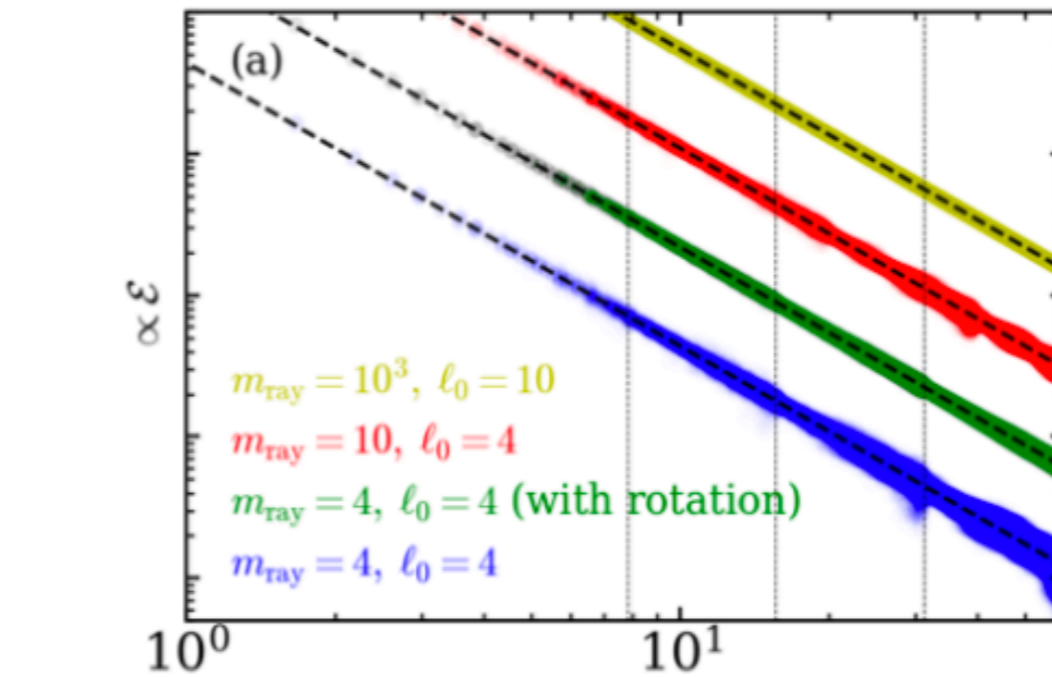
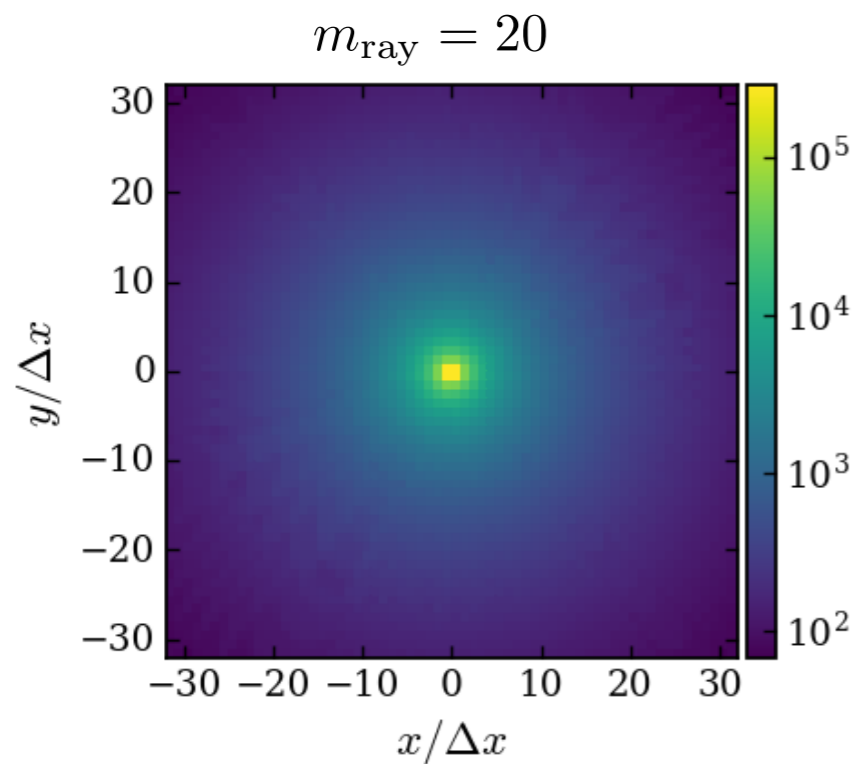
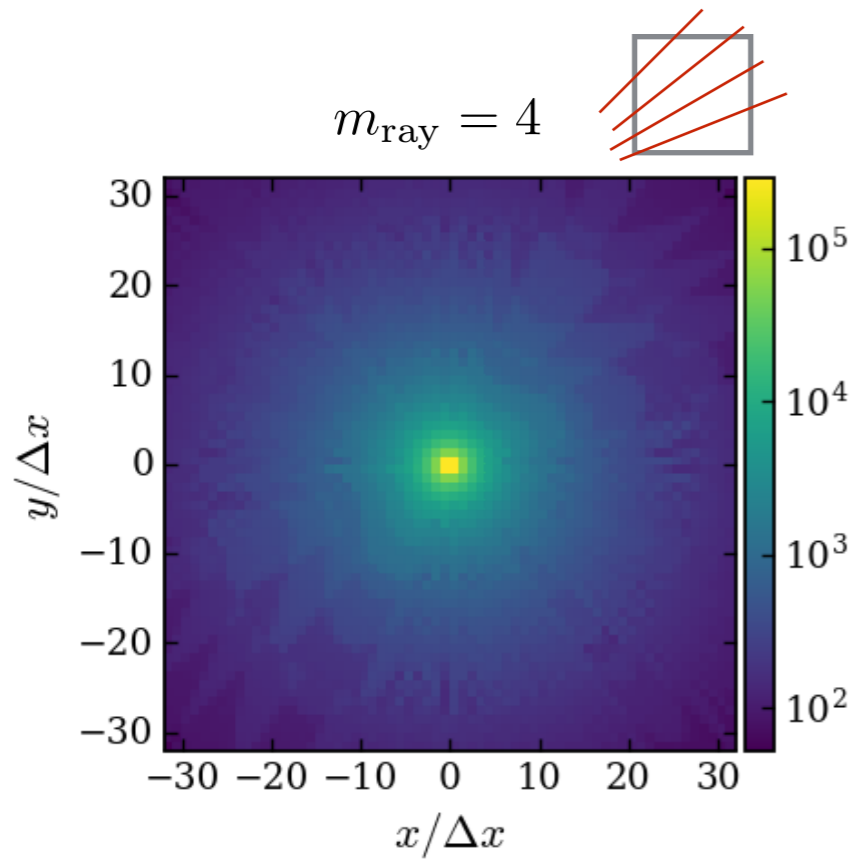
Send to Neighbors

Receive from Neighbors

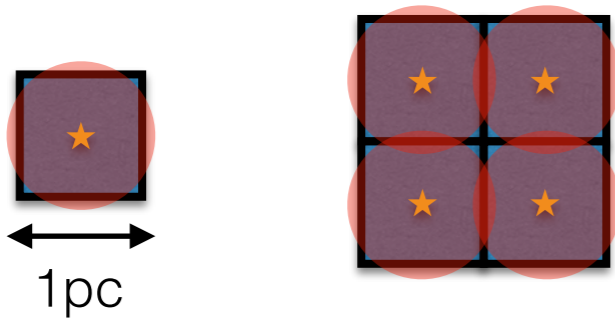
Check if all rays are destroyed or exits the domain



Radiation in Vacuum

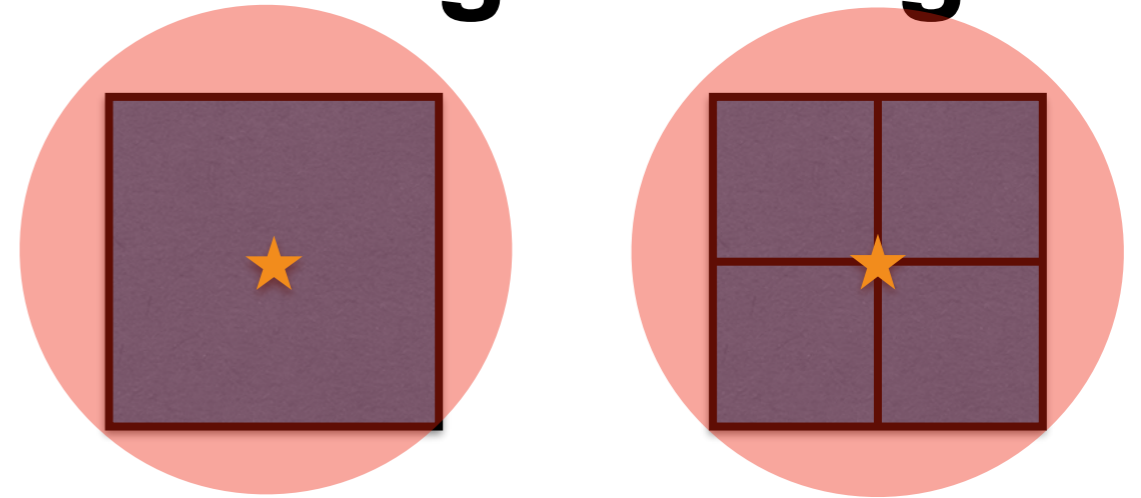


Weak Scaling

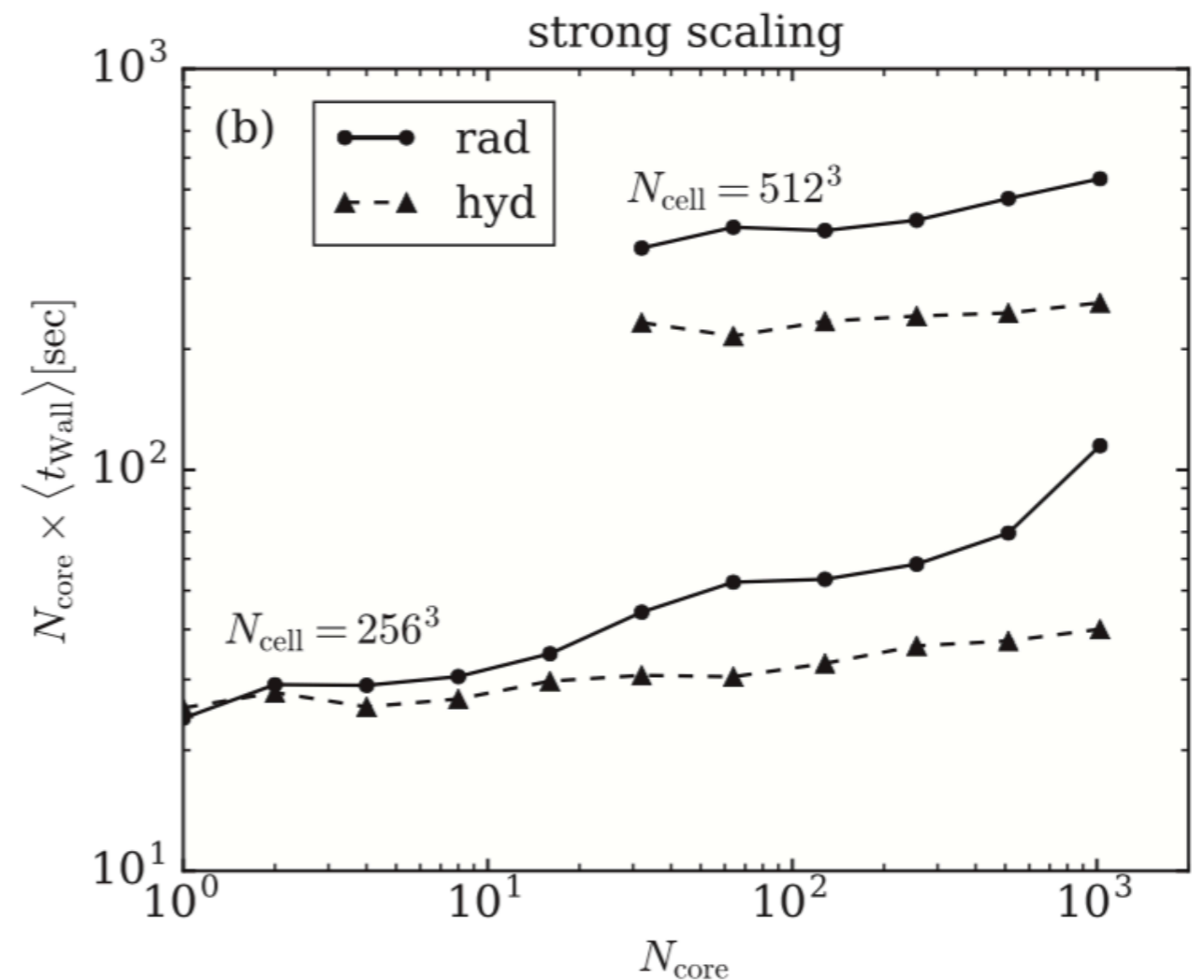
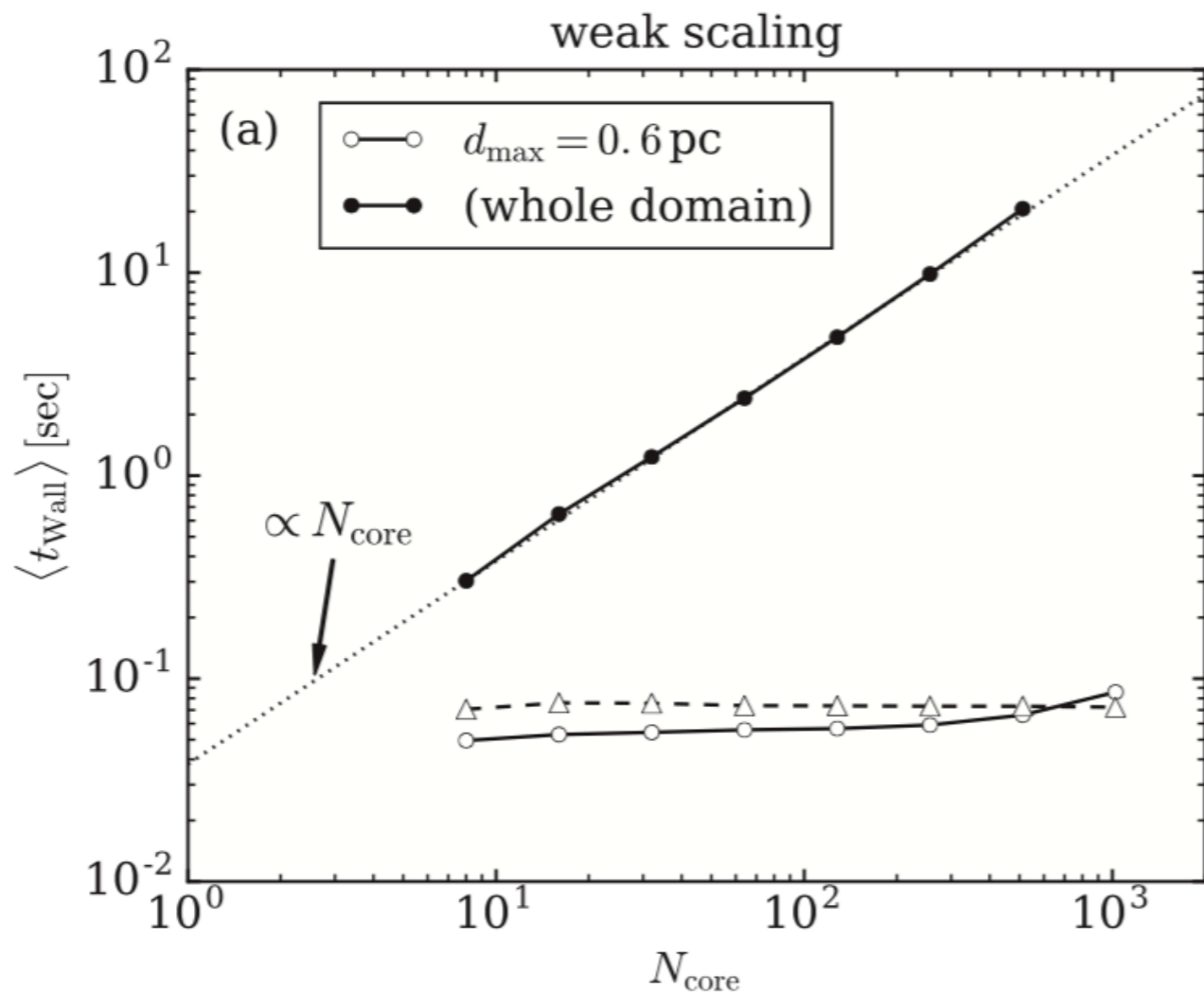


- Constant amount of work per process (32^3 cells/proc)

Strong Scaling



- Fixed problem size (256^3 , 512^3 cells)



Thoughts

- Need to minimize the overhead associated with finding neighboring meshblocks when multiple meshblocks are assigned to a single processor
- Control flow with chemistry module
 - Update species abundances based on radiation field
 - Is operator split method with substepping best approach?
- Hybrid RT
 - Absorption of UV radiation calculated by ART
 - Moment method to follow diffuse IR emission from dust
- ART as an on-the-fly integration tool?
 - Synthetic observation, column density maps, etc.