

COLLISION-INDUCED LIGHT SCATTERING FROM LIQUID  $\text{CCl}_4$  AND  $\text{C}_6\text{H}_{12}$ \*

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Collision-induced light scattering was observed in pure  $\text{CCl}_4$  and  $\text{C}_6\text{H}_{12}$  and in their mixtures. The intensity  $I(\omega)$  in the high frequency wing was fitted to an expression,  $I(\omega) \propto \omega^q \exp(-\omega/\omega_0)$  where  $q$  and  $\omega_0$  are variable parameters. It was found that the values of  $q$  and  $\omega_0$  are dependent upon the region of the profile over which the fit is made; possible interpretations are discussed.

## 1. Introduction

Collision-induced light scattering (CIS) is a newly-identified phenomenon which has increased the scope of the information obtainable about dense media by scattering methods [1-4]. While free, optically isotropic atoms or molecules do not depolarize light, an anisotropy can be induced in the total polarizability of a system of interacting atoms which produces a broad depolarized wing centred about the polarized Rayleigh line. Three models for the induction mechanism have been proposed based on studies of liquids and compressed gases.

(i) *Dipole-induced dipole (DID)* [1, 2, 5]. The anisotropy results from the interaction between electric dipoles induced in the atoms by the incident light. The total field acting on a given atom is the sum of this external light field and the internal field due to the induced dipoles in its neighbours. Orientational fluctuations in the net induced moment due to the atomic motion yield the depolarized scattering. This is a long-range interaction giving an effective pair polarizability which varies as  $r^{-3}$  where  $r$  is the distance between the atoms in a collision pair.

(ii) *Electron overlap (EO)* [3, 4]. The distortion of the electron clouds during close encounters is responsible for the induced polarizability. Originally, the

form  $r^2 \exp(-ar^2)$  was proposed but recently\*\*, an  $r^{-9}$  dependence has been derived in the case of argon.

(iii) *Frame distortion* [6]. Bucaro and Litovitz [7, 8] have made an extensive study of CIS in atomic and molecular liquids and concluded that frame distortion during close collisions which gives a pair polarizability varying as  $r^{-13}$  is the principal induction mechanism in liquids composed of isotropic and non-isotropic molecules.

With the use of several simplifying assumptions, principally binary collisions with zero impact parameter, Bucaro and Litovitz were able to derive an expression for the intensity  $I$  in the wings as a function of frequency  $\omega$ ,

$$I(\omega) \propto \omega^{2[(m-7)/7]} \exp(-\omega/\omega_0), \quad (1)$$

where the induced incremental polarizability is given by

$$\Delta\alpha(r) \propto r^{-m}. \quad (2)$$

The constant  $\omega_0$  is inversely proportional to a characteristic time associated with the duration of the interaction giving rise to  $\Delta\alpha$ .

In the analysis of their spectra, they assumed a value for  $m$  and determined the corresponding  $\omega_0$  from their data. As there is evidence from experiments on compressed gases [1, 2] that the DID contribution diminishes at high densities, they assumed that, in the

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case of atomic liquids, the electron overlap effect predominates. They found that  $m = 9$  in the case of argon and xenon and  $m = 13$  in the case of molecular liquids gave values of  $\omega_0$  in agreement with their calculations. This work is an excellent attempt to categorize CIS in liquids while providing insight into the interaction mechanisms responsible for the scattering. Primarily, it shows that binary interactions remain important even in the liquid phase.

Gersten [9, 10] has pointed out that in the spectra of compressed rare gases, different parts of the profile are affected by different details of the interaction.

Encouraged by the success of Bucaro and Litovitz but mindful that the complications envisaged by Gersten should apply to liquids as well as gases, we have repeated observations of the CIS spectra in pure  $\text{CCl}_4$  and  $\text{C}_6\text{H}_{12}$ , as well as in mixtures, with the goal of further investigating the form of the spectral profile.

## 2. Experimental method

The experimental set-up is typical of laser Raman scattering studies. Light from an argon-ion laser (CRL 52) operating at about 3/4 watt at 4880 Å is passed through a half-wave plate and prism polarizer before being focussed in the sample cell. The light scattered at 90° is collected by an  $f/2$  system and brought to a double scanning monochromator (Jarrell-Ash 25-100) having a spectral slit width of 1  $\text{cm}^{-1}$ . The detector is a cooled EMI 6256B photomultiplier tube used in the photon-counting mode. With the discriminator levels set for an optimum signal-to-noise ratio at low light intensities, the dark count is 1/3 cps. The output is stored in a multi-channel analyzer (Victoreen ST400M) whose channel advance is controlled by the stepping drive for the monochromator gratings. The geometry used is such that if the incident light is considered to travel in the  $x$  direction, polarized in the  $z$  direction, then observations are made in the  $z$  direction. All experiments are performed at 295°K.

## 3. Analysis of results

If a frame distortion origin for the induced polarizability is assumed, eq. (1) leads to a linear relation-

ship between  $\ln[I(\omega)/\omega^{12/7}]$  and  $\omega$  with a slope  $(-1/\omega_0)$ . When this test is applied to the data, it is found that  $\omega_0 = 12.1 \text{ cm}^{-1}$  for  $\text{CCl}_4$  and  $14.7 \text{ cm}^{-1}$  for  $\text{C}_6\text{H}_{12}$  in excellent agreement with Bucaro and Litovitz (11.9 and  $14.8 \text{ cm}^{-1}$  respectively). The frequency range over which this linear relation holds is 30 to  $80 \text{ cm}^{-1}$  for  $\text{CCl}_4$  and 30 to  $120 \text{ cm}^{-1}$  for  $\text{C}_6\text{H}_{12}$  (fig. 1).

Frame distortion may not however be the only interaction mechanism contributing to the scattering. It was noted that much of the high frequency tail of the  $\text{CCl}_4$  could not be accounted for by the above method. When  $m = 9$  was tried, a value consistent with an electron overlap interaction (at least for rare gas atoms), eq. (1) held over an increased frequency range, 20  $\text{cm}^{-1}$  to  $100 \text{ cm}^{-1}$ . Moreover the quality of the fit was much improved over that with  $m = 13$ . This result led us to perform the analysis based on the following considerations.

All authors who have proposed mechanisms for collision-induced scattering conclude that the high frequency profile is described by an expression:

$$I(\omega) = f(\omega) \exp(-\omega/\omega_0). \quad (3)$$

In the original model of Levine and Birnbaum,  $f(\omega)$  is approximated by  $\omega^{1/2}$ ; the more general function  $\omega^{2[(m-7)/7]}$  shows clearly that the power of  $\omega$  is a function of the induction process. Gersten [10] has emphasized that the exponential factor in (3) is model independent (although the value of  $\omega_0$  is not). The accurate determination of  $f(\omega)$  should lead to meaningful information not available through the exponential. Because of the presence of this strong exponential factor, the exact form of  $f(\omega)$  is difficult to extract from the experimental data.

In an effort to acquire some estimate of  $f(\omega)$  directly from the observed spectra, we have assumed that the high frequency profile can be represented by:

$$I(\omega) \propto \omega^q \exp(-\omega/\omega_0), \quad (4)$$

where both  $q$  and  $\omega_0$  are taken as variable parameters and made a least squares fit to the spectra by applying the technique of multiple regression. The results given in table I are averages over several spectra. The errors quoted represent one standard deviation. For  $\text{C}_6\text{H}_{12}$ , the fits in the range 25  $\text{cm}^{-1}$  and 40  $\text{cm}^{-1}$  to 100  $\text{cm}^{-1}$  are the more significant as they are over a region sufficiently removed from the laser line to be

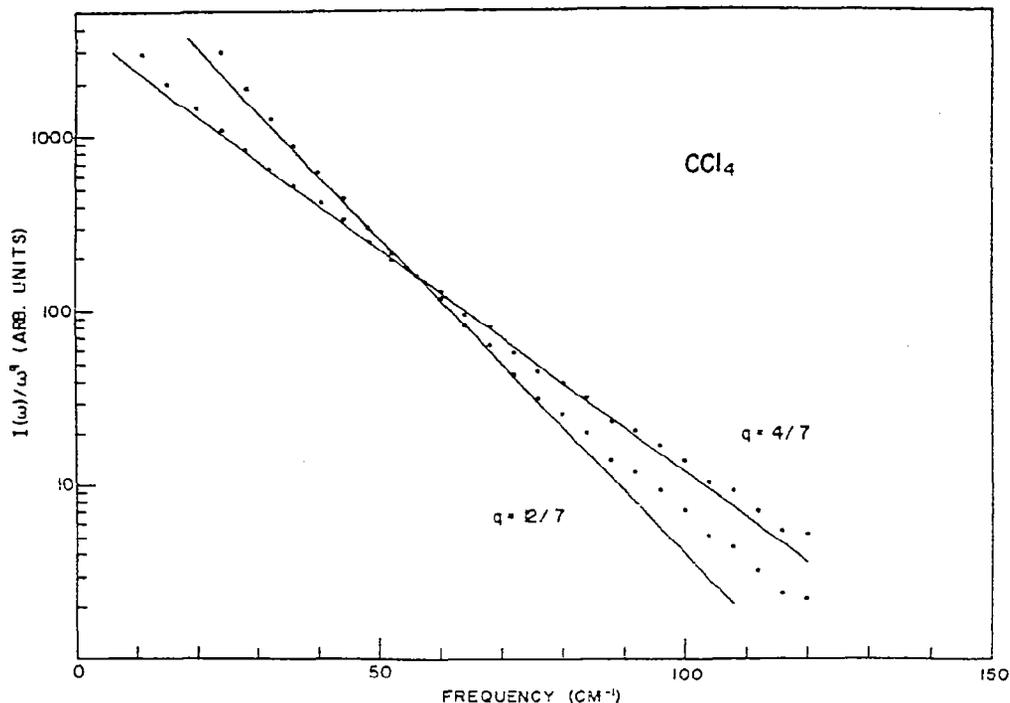


Fig. 1.  $I(\omega)/\omega^q$  for the observed spectrum of  $\text{CCl}_4$  at  $293^\circ\text{K}$  where  $q$  is  $12/7$  and  $4/7$  corresponding to  $\Delta\alpha(r)$  varying as  $r^{-13}$  and  $r^{-9}$  respectively. Data points are shown only every  $4\text{ cm}^{-1}$ .

Table 1  
Parameters obtained from the least squares fit

	Range ( $\text{cm}^{-1}$ )	$q$	Effective $m$	$\omega_0$ ( $\text{cm}^{-1}$ )	Standard error of estimate
$\text{CCl}_4$	16 → 85	$0.49 \pm 0.04$	$8.7 \pm 0.13$	$17.0 \pm 0.25$	0.05
	16 → 105	$0.22 \pm 0.03$	$7.8 \pm 0.12$	$19.1 \pm 0.25$	0.06
	16 → 125	$0.15 \pm 0.04$	$7.5 \pm 0.13$	$19.6 \pm 0.24$	0.11
	40 → 100	$-0.72 \pm 0.19$	$4.5 \pm 0.67$	$25.3 \pm 1.9$	0.09
$\text{C}_6\text{H}_{12}$	15 → 115	$0.78 \pm 0.05$	$9.7 \pm 0.17$	$19.2 \pm 0.32$	0.11
	25 → 115	$1.36 \pm 0.07$	$11.7 \pm 0.23$	$16.7 \pm 0.28$	0.10
	40 → 115	$2.04 \pm 0.13$	$14.1 \pm 0.46$	$14.5 \pm 0.33$	0.10

free of contributions due to the permanent anisotropy of the molecule. The 'effective  $m$ ' is determined by setting

$$q = (2/7)(m - 7). \quad (5)$$

The standard error of estimate is calculated only over the range of the fit.

#### 4. Discussion

The most striking result in table 1 is the fact that for both liquids, the values of  $q$  and  $\omega_0$  depend on the frequency region over which the fit is made. For  $\text{C}_6\text{H}_{12}$  the result in the range 40 to  $115\text{ cm}^{-1}$  agrees with that of Bucaro and Litovitz. On the other hand,

for  $\text{CCl}_4$ , as more of the tail is included in the fit, the effective  $m$  decreases and  $\omega_0$  increases, nowhere approximating  $m = 13$  or  $\omega_0 = 11.9 \text{ cm}^{-1}$ .

The failure of eq. (1) to hold over the entire tail with one set of values for  $q$  and  $\omega_0$  indicates that more than one type of interaction is operative in the scattering. For  $\text{C}_6\text{H}_{12}$ , short-range effects seem to be important with frame distortion especially dominant beyond  $40 \text{ cm}^{-1}$ . The theory of Bucaro and Litovitz holds well in this case: basically a single short-range interaction. For  $\text{CCl}_4$ , both short- and long-range interactions contribute. Here the theory of Bucaro and Litovitz is not entirely applicable as their calculations of  $\omega_0$  are valid only near the turning point. Judging from the effective  $m$  values, the short-range part includes both electron overlap and frame distortion. The long-range interaction could be of the dipole-induced dipole type.

It should be recalled that because of symmetry effects, the intensity of the scattering through DID at liquid densities is much less than that predicted from an extrapolation of the gas results using a quadratic dependence on density; however it should not necessarily vanish. In liquids the DID interaction would be effective through rapid local fluctuations in the positions of molecules, not describable by the trajectory dynamics used to derive eq. (1). Thus the spectral profile due to DID would broaden as the density increases and it would be expected to contribute to the far wings of spectrum.

The  $\omega_0$  found for  $40 < \omega < 100$  corresponds to a time of  $2.1 \times 10^{-13}$  sec which is of the order of magnitude of the time between collisions in a cell model for liquid  $\text{CCl}_4$  [11]; the time between collisions would be the time characterizing these fluctuations in positions.

The values of  $\omega_0$  obtained from the spectra of mixtures in the range  $40$  to  $100 \text{ cm}^{-1}$  are plotted in fig. 2 as a function of  $\text{CCl}_4$  concentration. A least squares fit to a polynomial in concentration shows that the variation of  $\omega_0$  with concentration can be well represented by a quadratic and a cubic term, the higher order and linear terms being negligible. Since  $\omega_0$  characterizes the spectral profile, this means that changes in the line shape occur roughly in the same way with concentration. The cell model used by Thi-beau [1, 2] to explain the results in gaseous argon at high pressures predicts a density dependence of the

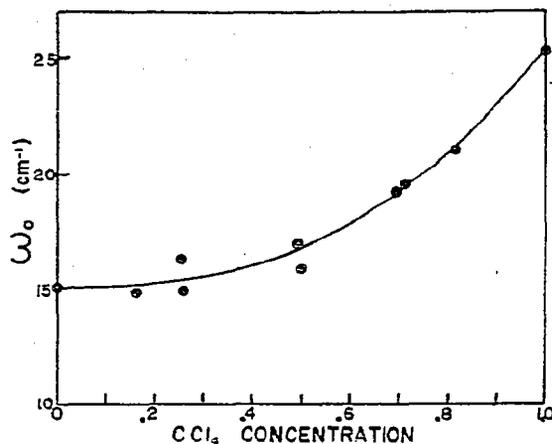


Fig. 2. The variation of  $\omega_0$  with the concentration of  $\text{CCl}_4$  in the frequency range  $40$  to  $100 \text{ cm}^{-1}$ .

total intensity involving several terms of the form  $(\rho/\rho_s)^x$  where  $x$  is between 2 and 3.3;  $\rho_s$  is the maximum density taken to be that of the solid. Therefore as one goes from pure  $\text{C}_6\text{H}_{12}$  which is of frame distortion origin to pure  $\text{CCl}_4$ , the concentration dependence of  $\omega_0$  is similar to the density dependence of the intensity for DID scattering in dense media. A thorough treatment of scattering from mixtures is complex and difficult to apply [12]; nevertheless this result appears to support the conclusion that the tail of the  $\text{CCl}_4$  spectrum contains a contribution from DID scattering. In any event, the low power of the concentration dependence reaffirms that the scattering is due to interactions between a few molecules even in the liquid phase.

## 5. Summary

Based on the statistical accuracy of the data further speculation on the physical meaning of results in table 1 is uncertain. It is clear however that the values of  $q$  and  $\omega_0$  giving the best fit to the observed spectra change over the profile. This variation is attributable to the total induced polarizability being due to more than one type of interaction. For  $\text{CCl}_4$ , it appears that both short- and long-range forces are effective in the interaction; electron overlap, DID and frame distortion could all be contributing. On the other hand for  $\text{C}_6\text{H}_{12}$ , only the short-range interactions seem to be important.

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