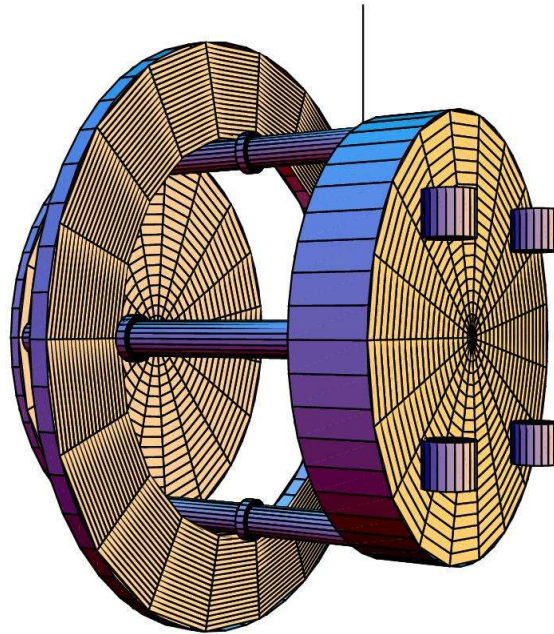


Fundamental Gravitation Physics with a Torsion Pendulum



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Fundamental Gravitation Physics with a Torsion Pendulum

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I

What Does “non-Newtonian” Look Like?

$$V = -\frac{Gm}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$

What Does “non-Newtonian” Look Like?

$$V = -\frac{Gm}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$

interaction length

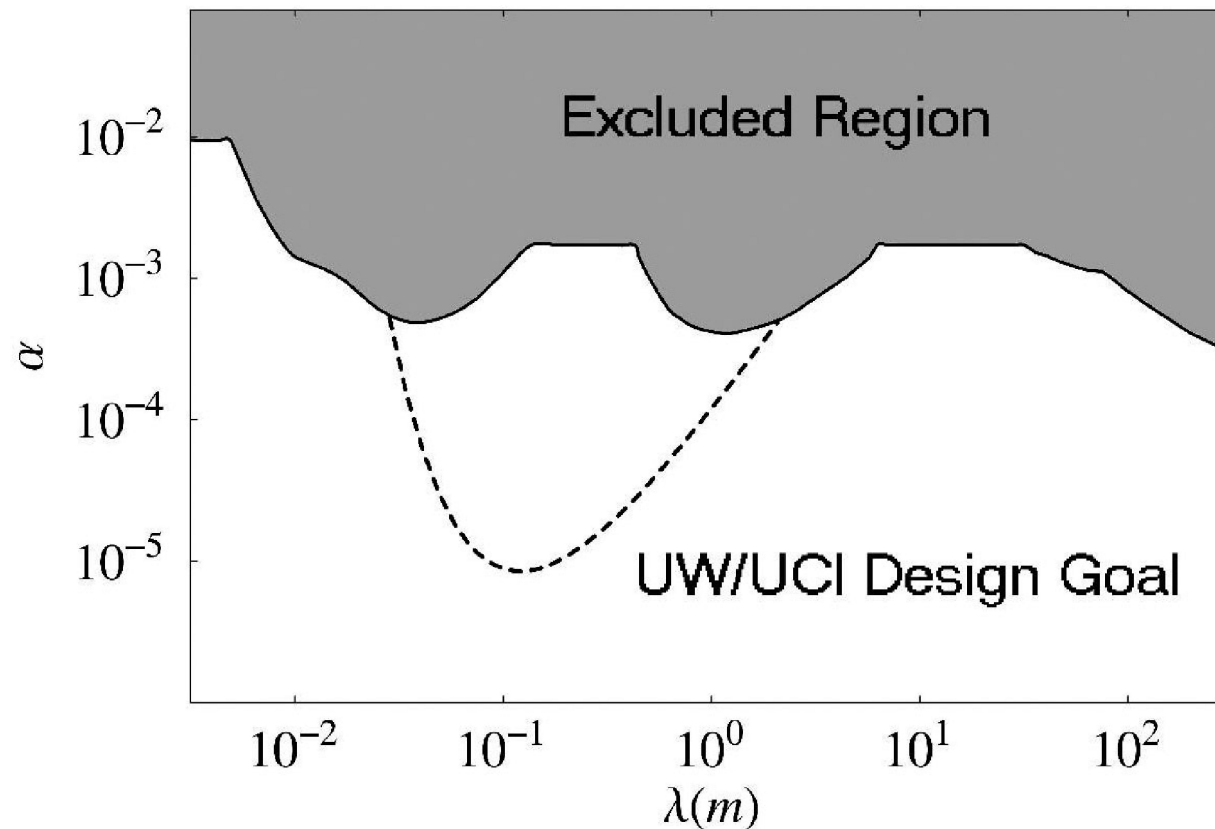
regular gravity

strength relative to gravity

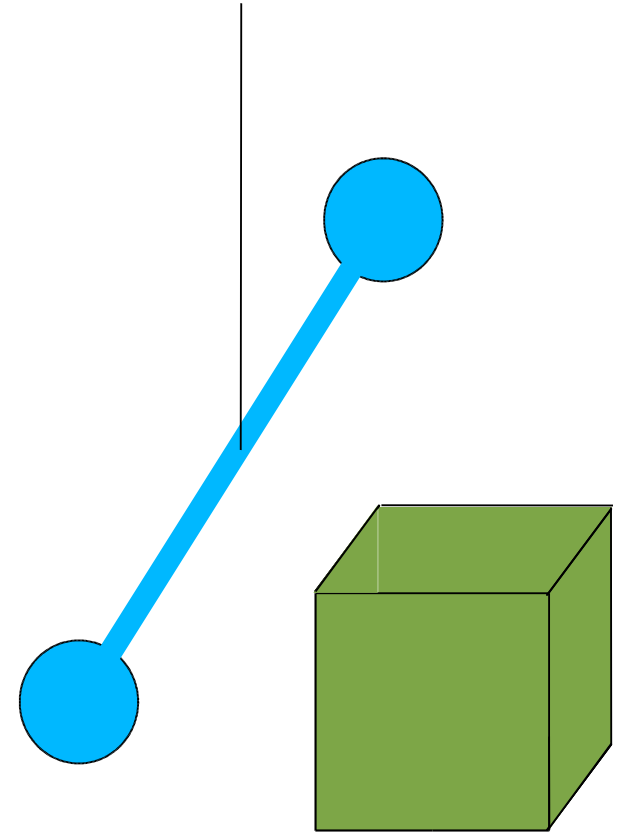
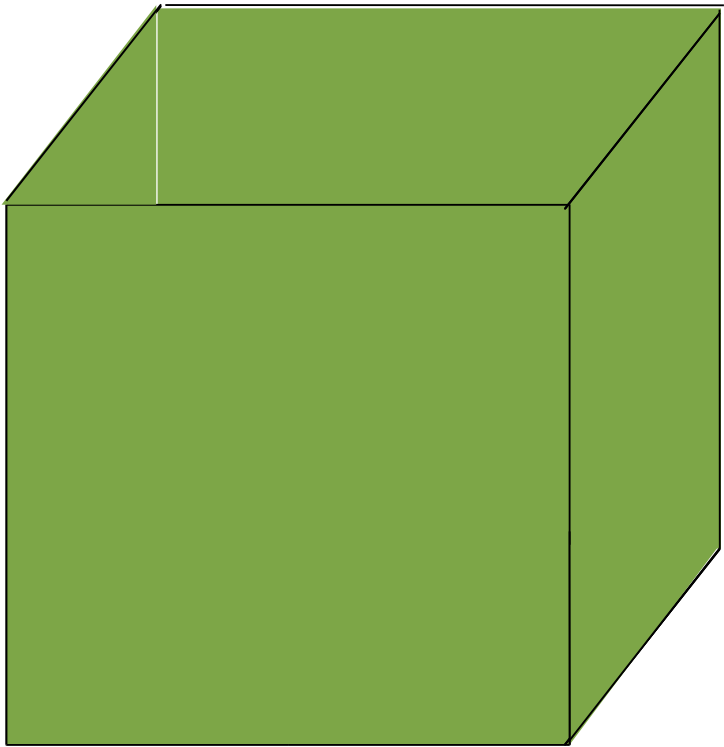
The diagram illustrates the components of the potential energy equation. A red arrow points from the label 'regular gravity' to the term $-\frac{Gm}{r}$. Another red arrow points from 'strength relative to gravity' to the coefficient α . A third red arrow points from 'interaction length' to the term $e^{-r/\lambda}$.

What Does “non-Newtonian” Look Like?

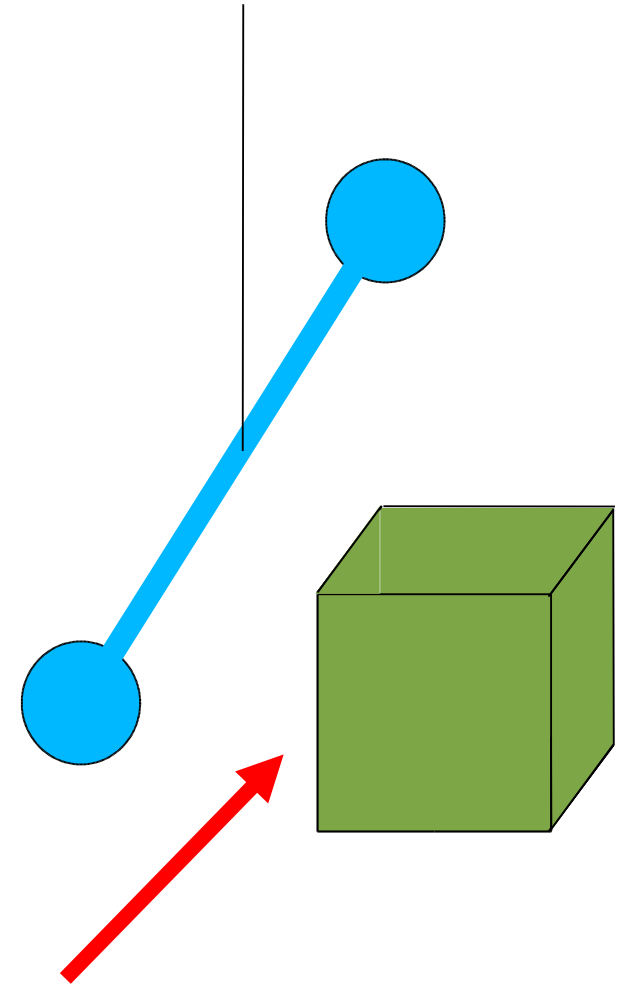
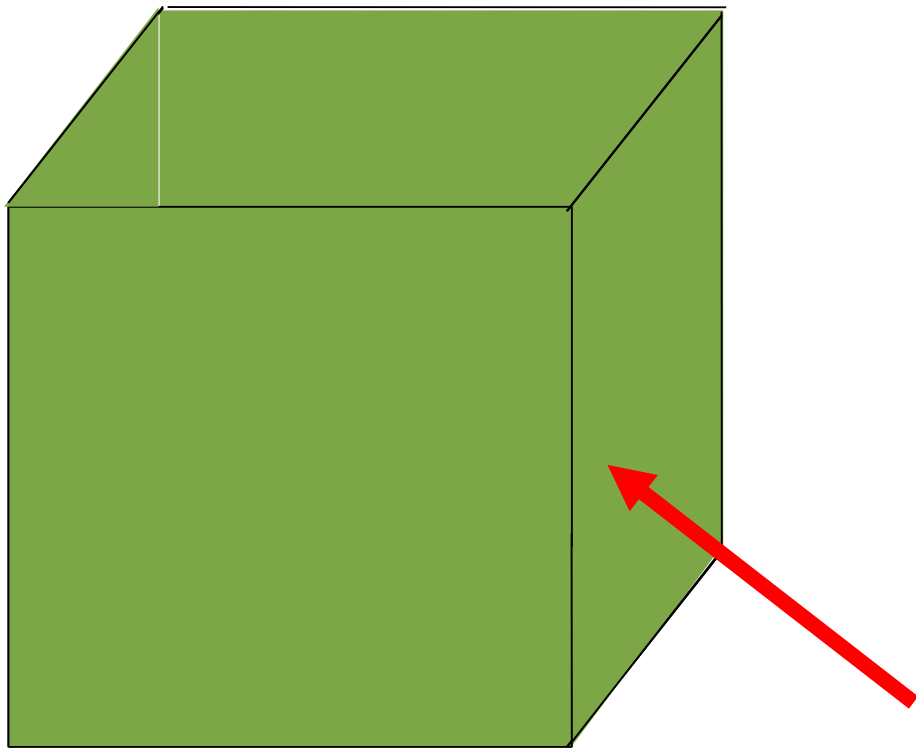
$$V = -\frac{Gm}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$



Detecting non-Newtonian Interactions



Detecting non-Newtonian Interactions



Newtonian gravity should cancel
leaving residual non-Newtonian interaction

Identifying the Leading Systematic Effect

$$\begin{aligned} U &= \int \rho V d^3 r \\ &= \int \rho \left(1 + x \frac{d}{dx} + y \frac{d}{dy} + z \frac{d}{dz} + x^2 \frac{d^2}{dx^2} + \dots \right) V dx dy dz \\ &\quad \vdots \\ &\quad \text{algebra} \\ &\quad \vdots \\ &= \sum_{nlm} M_{nlm} V_{nlm} \end{aligned}$$

Identifying the Leading Systematic Effect

$$U = \int \rho V d^3 r$$
$$= \int \rho \left(1 + x \frac{d}{dx} + y \frac{d}{dy} + z \frac{d}{dz} + x^2 \frac{d^2}{dx^2} + \dots \right) V dx dy dz$$

⋮

algebra

symmetries of electron orbitals

⋮

$$= \sum_{nlm} M_{nlm} V_{nlm}$$

field moments

mass moments

Identifying the Leading Systematic Effect

Newtonian gravity satisfies Laplace's Equation. Thus, only terms for which $n = l$ contribute to the interaction.

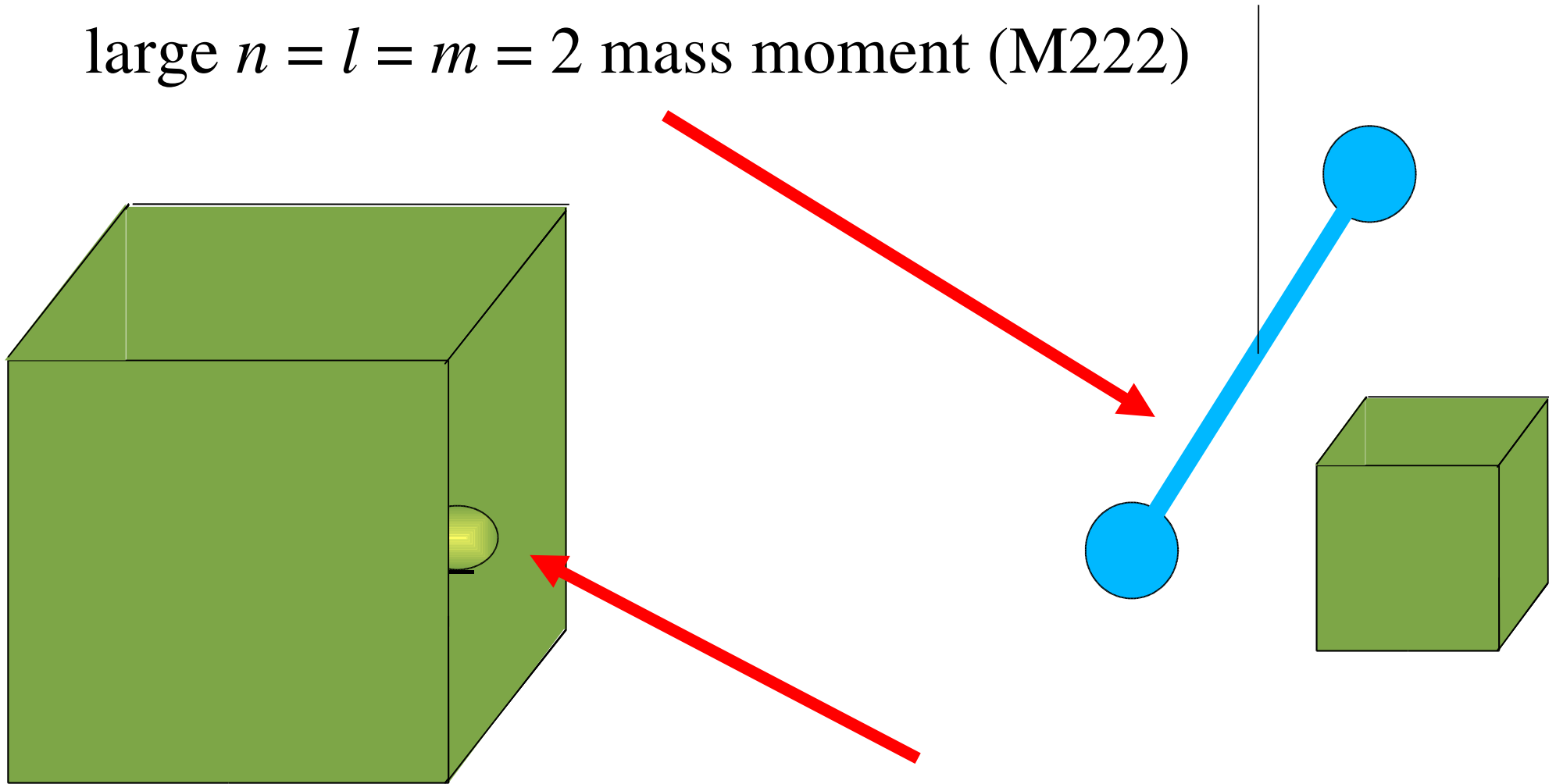
Call these “Newtonian Moments”.

Non-Newtonian forces do not satisfy Laplace's Equation and can contribute to the interaction for any combination of n and l .

When $n \neq l$, call these “non-Newtonian”.

Identifying the Leading Systematic Effect

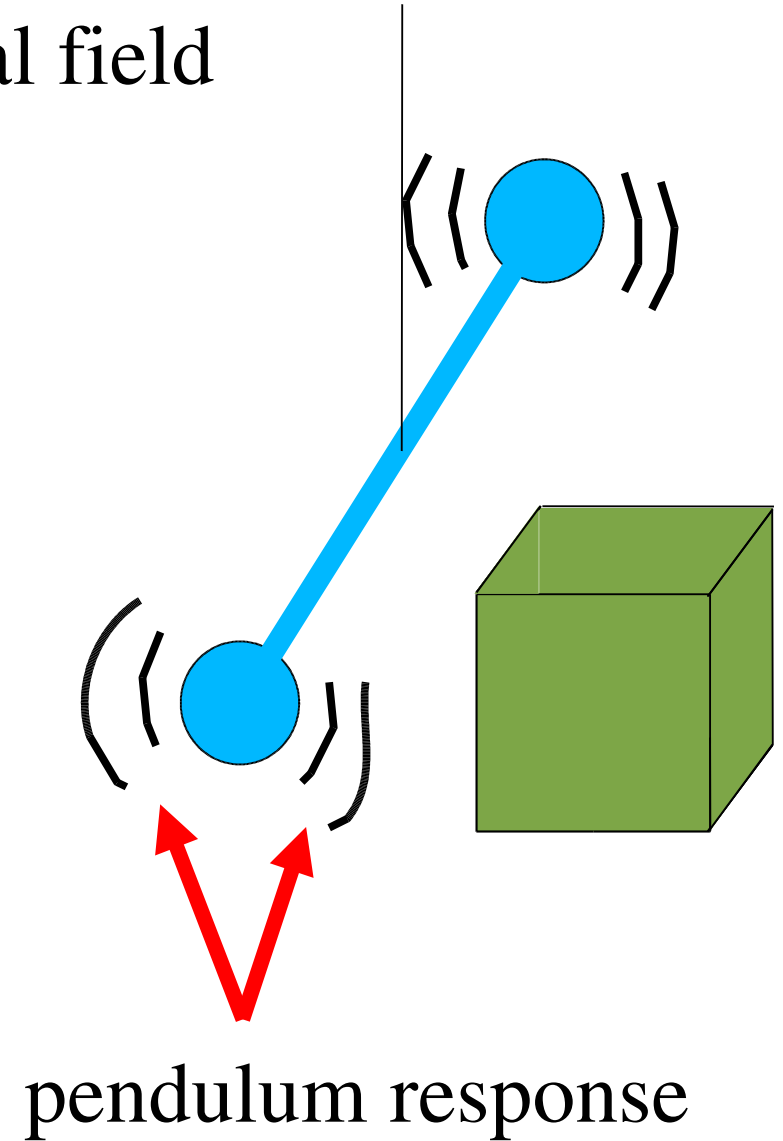
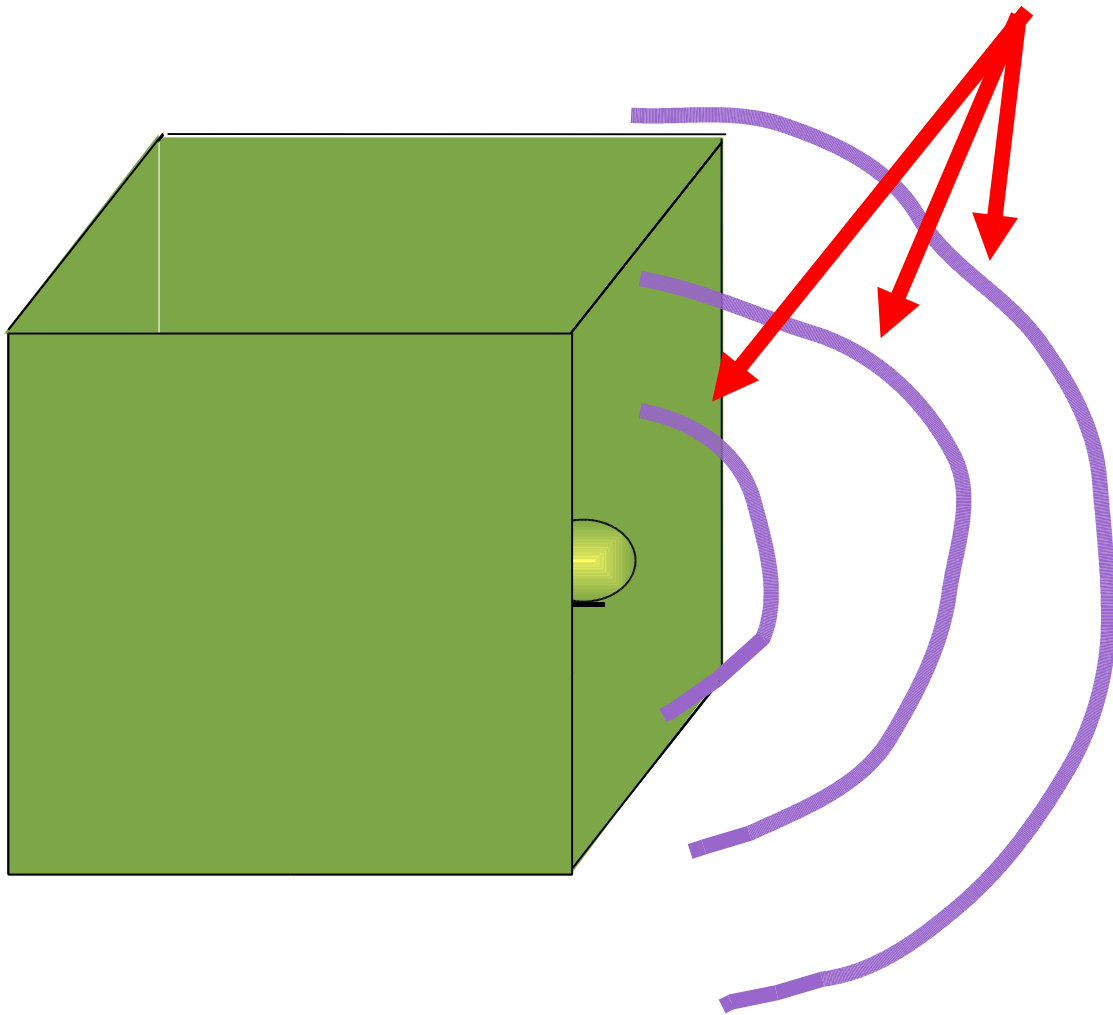
large $n = l = m = 2$ mass moment (M222)



fabrication error

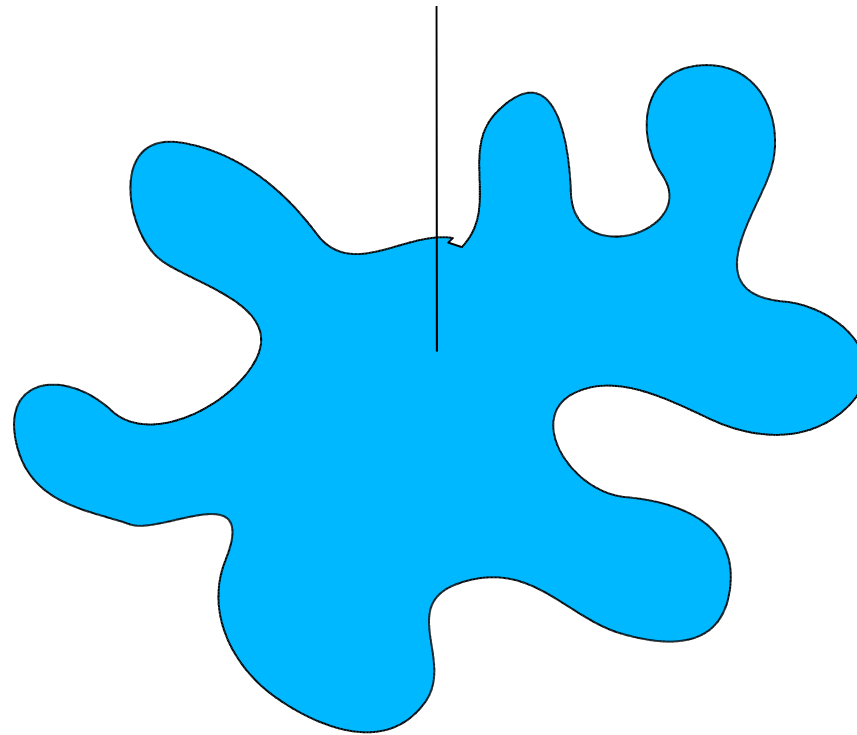
Identifying the Leading Systematic Effect

unwanted V222 gravitational field

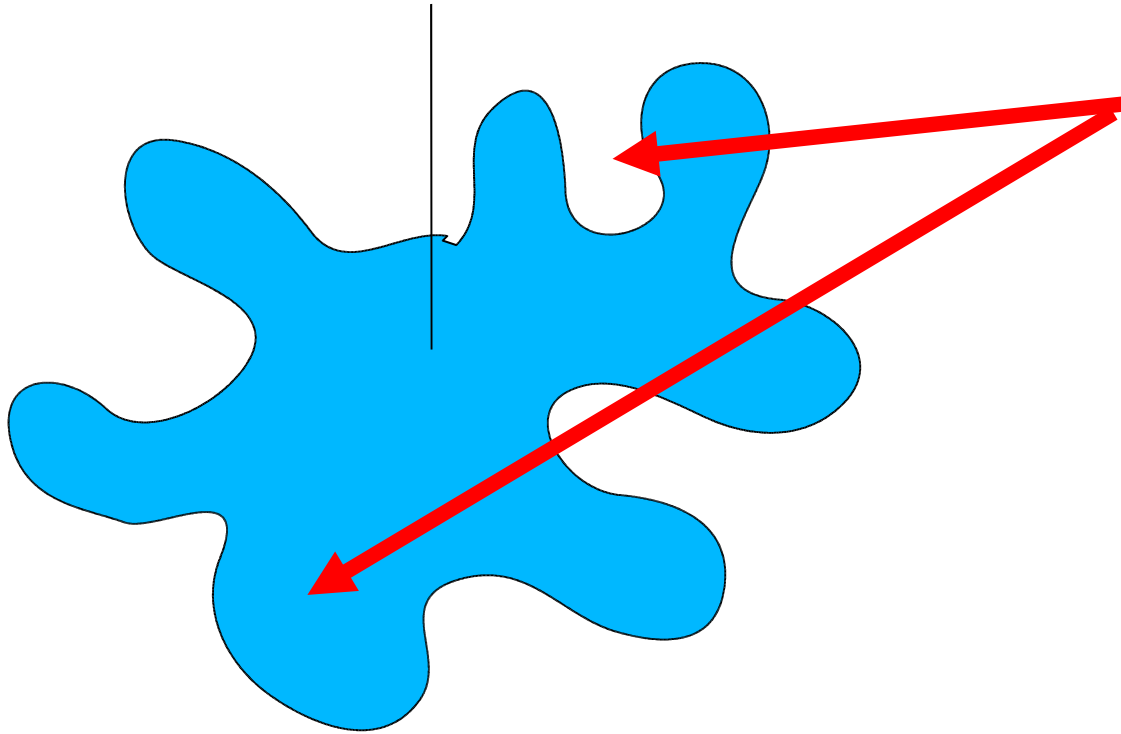


pendulum response

What would be nice...

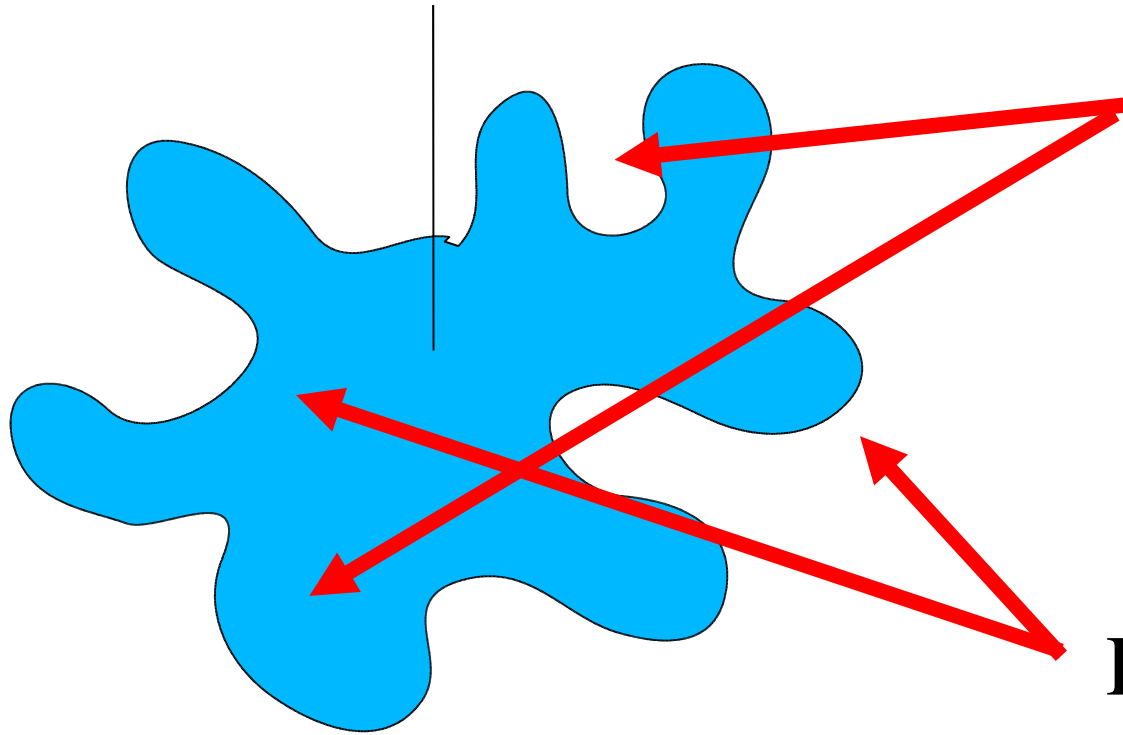


What would be nice...



No Newtonian
mass moments.

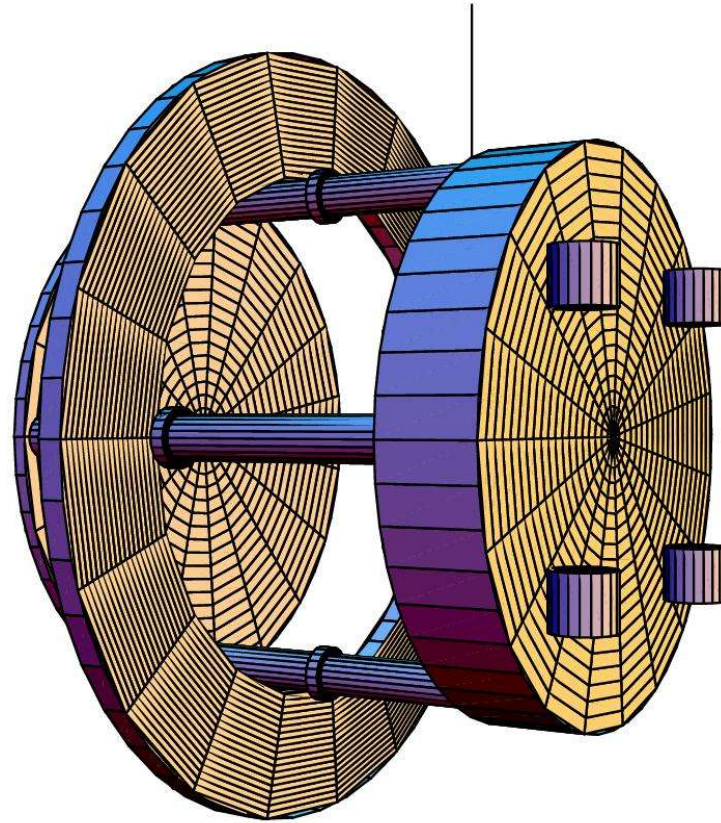
What would be nice...



No Newtonian
mass moments.

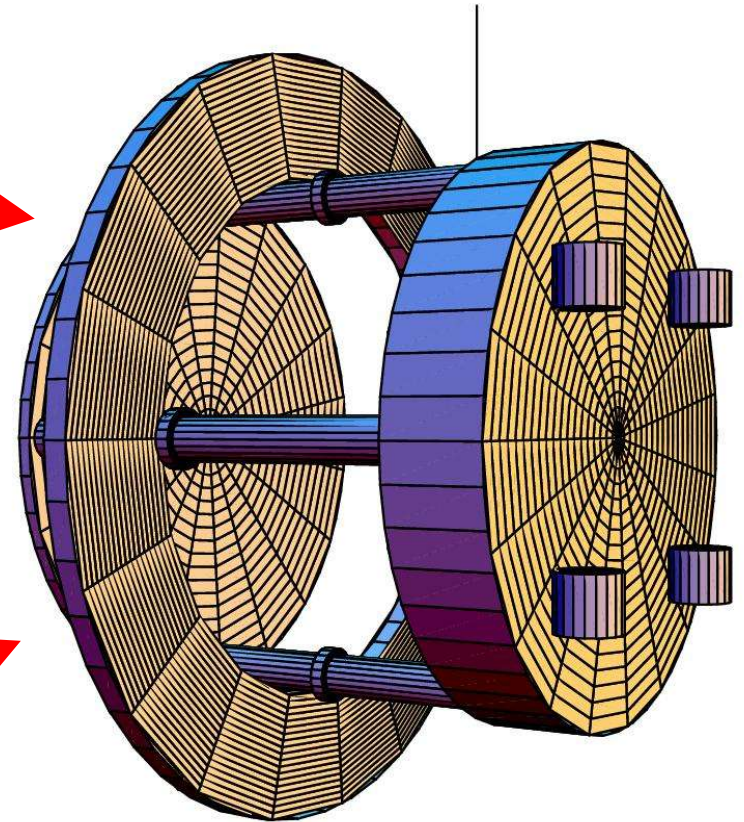
Large non-Newtonian
mass moments.

What will do...



What will do...

No low-order Newtonian
mass moments



One large, low-order
non-Newtonian mass moment

What will do...

Newtonian mass moments:

$$\left. \begin{aligned} V_{22m} &= 0 \\ V_{33m} &= 0 \\ V_{44m} &= 0 \end{aligned} \right\} \text{(for all } m)$$

$$V_{551} = 0$$

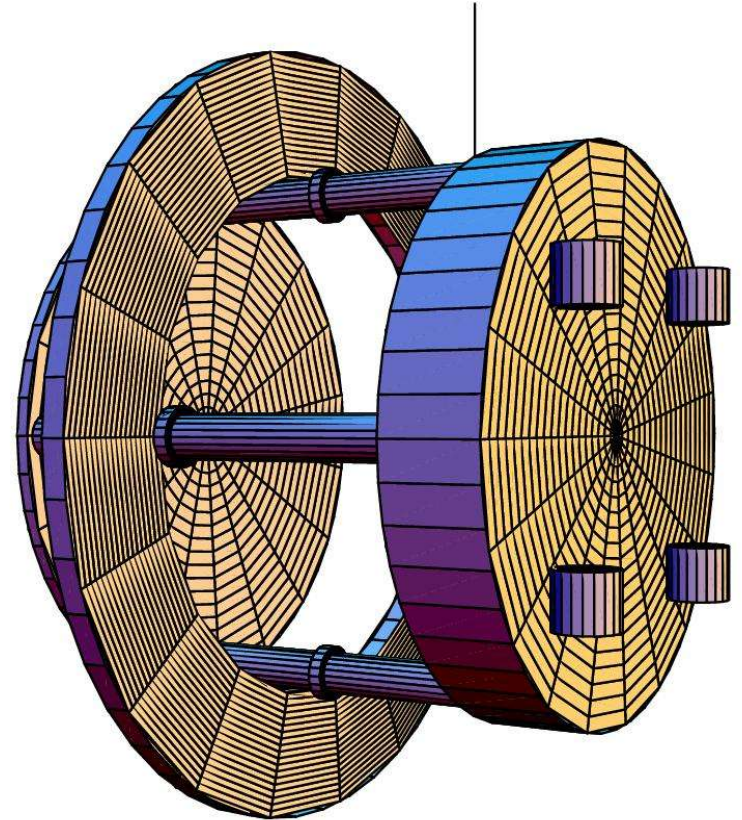
$$V_{661} = 0$$

$$V_{771} = 0$$

$$V_{881} = 0$$

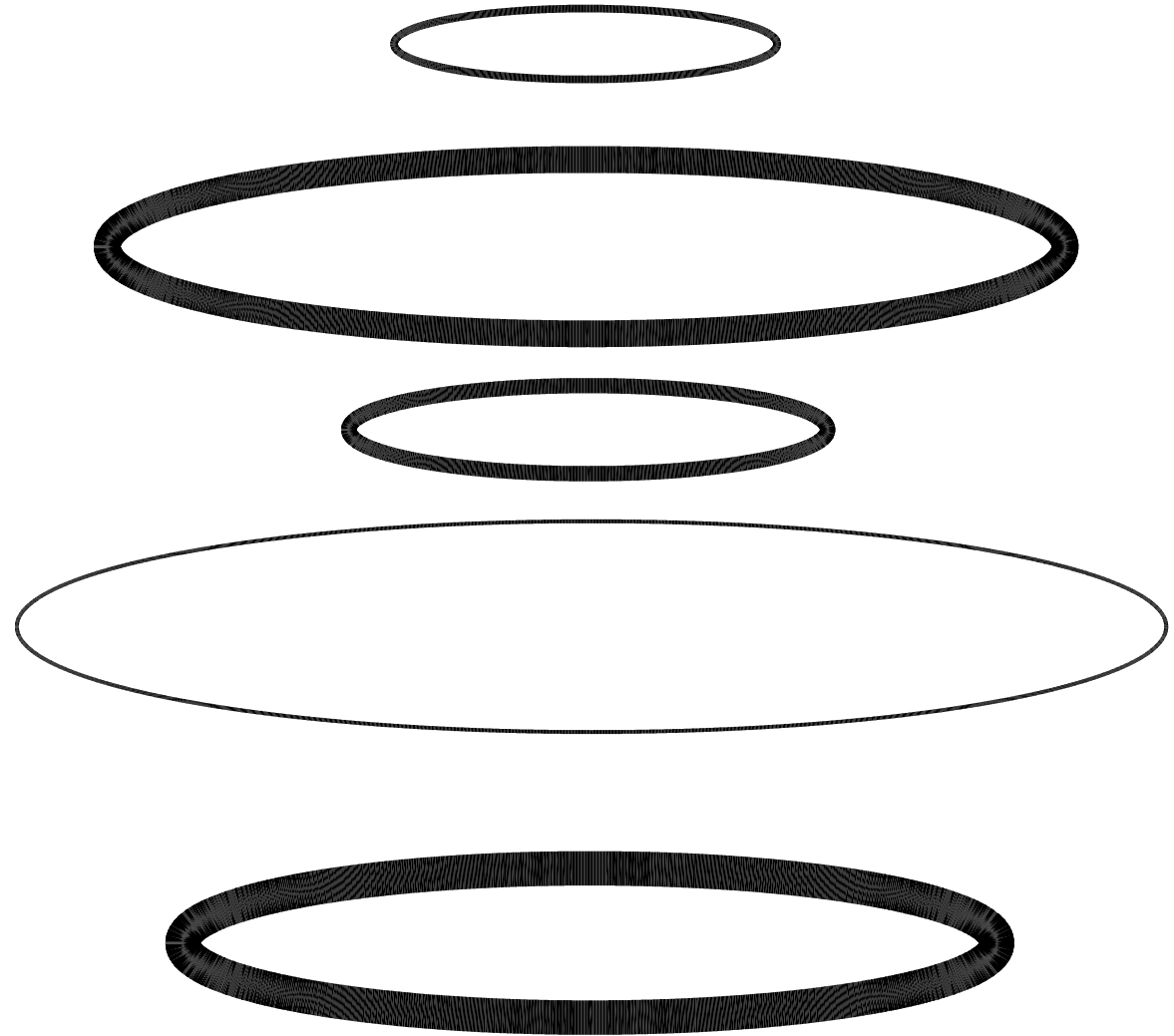
non-Newtonian moment:

$$V_{311} = \text{Large}$$



How to design what will do...

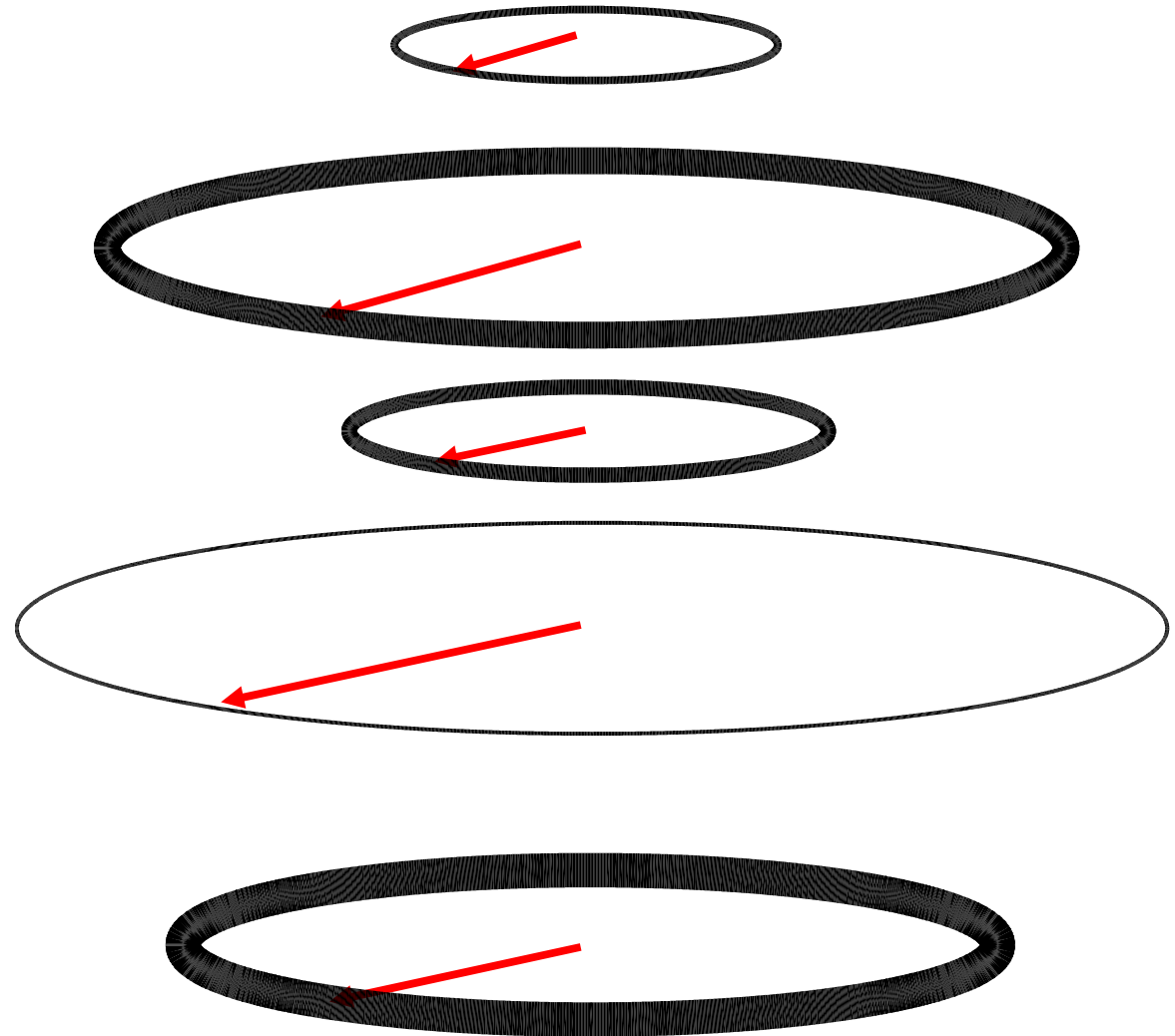
Start with 5 rings.



How to design what will do...

Start with 5 rings.

5 radii

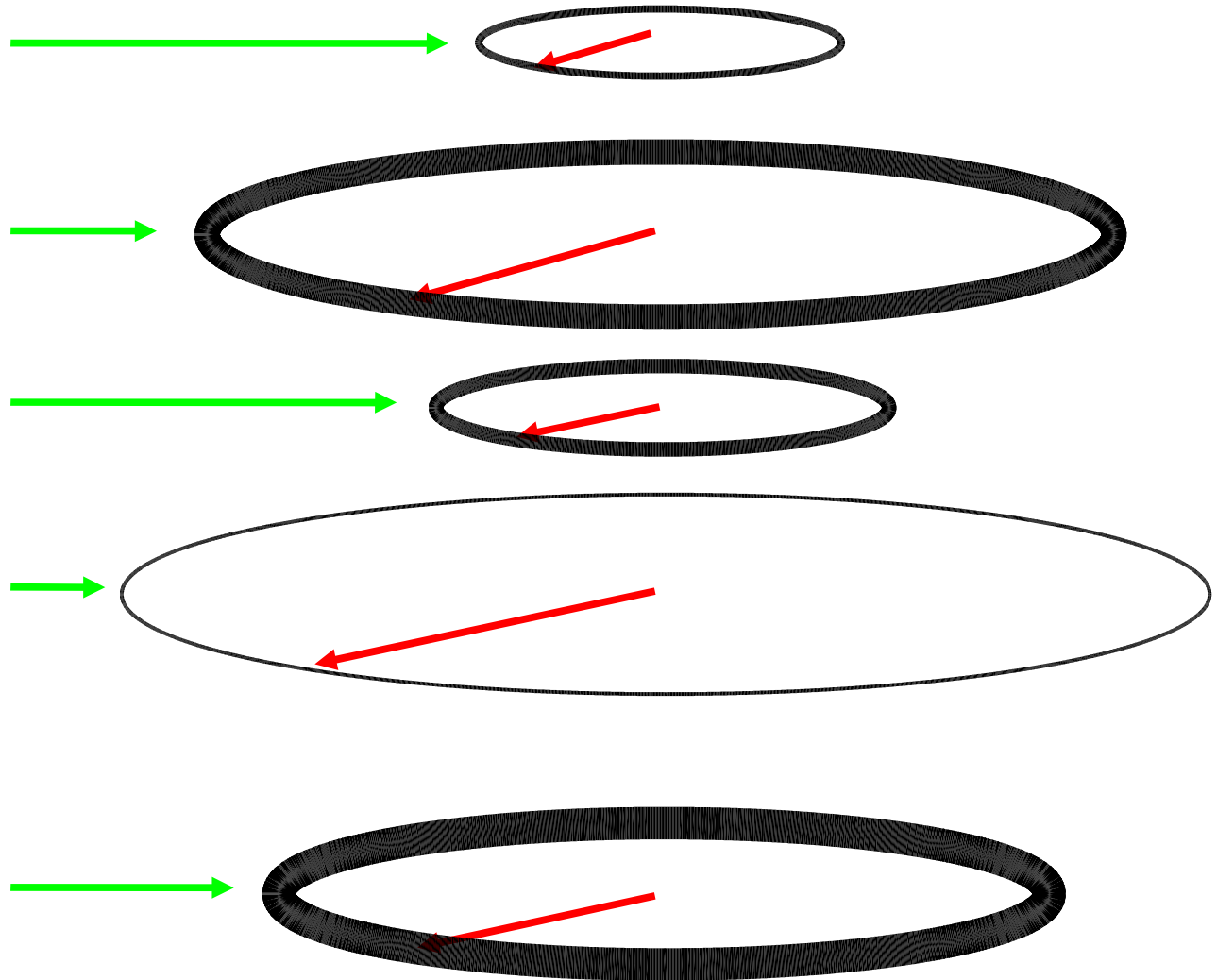


How to design what will do...

Start with 5 rings.

5 radii

5 heights



How to design what will do...

Start with 5 rings.

5 radii

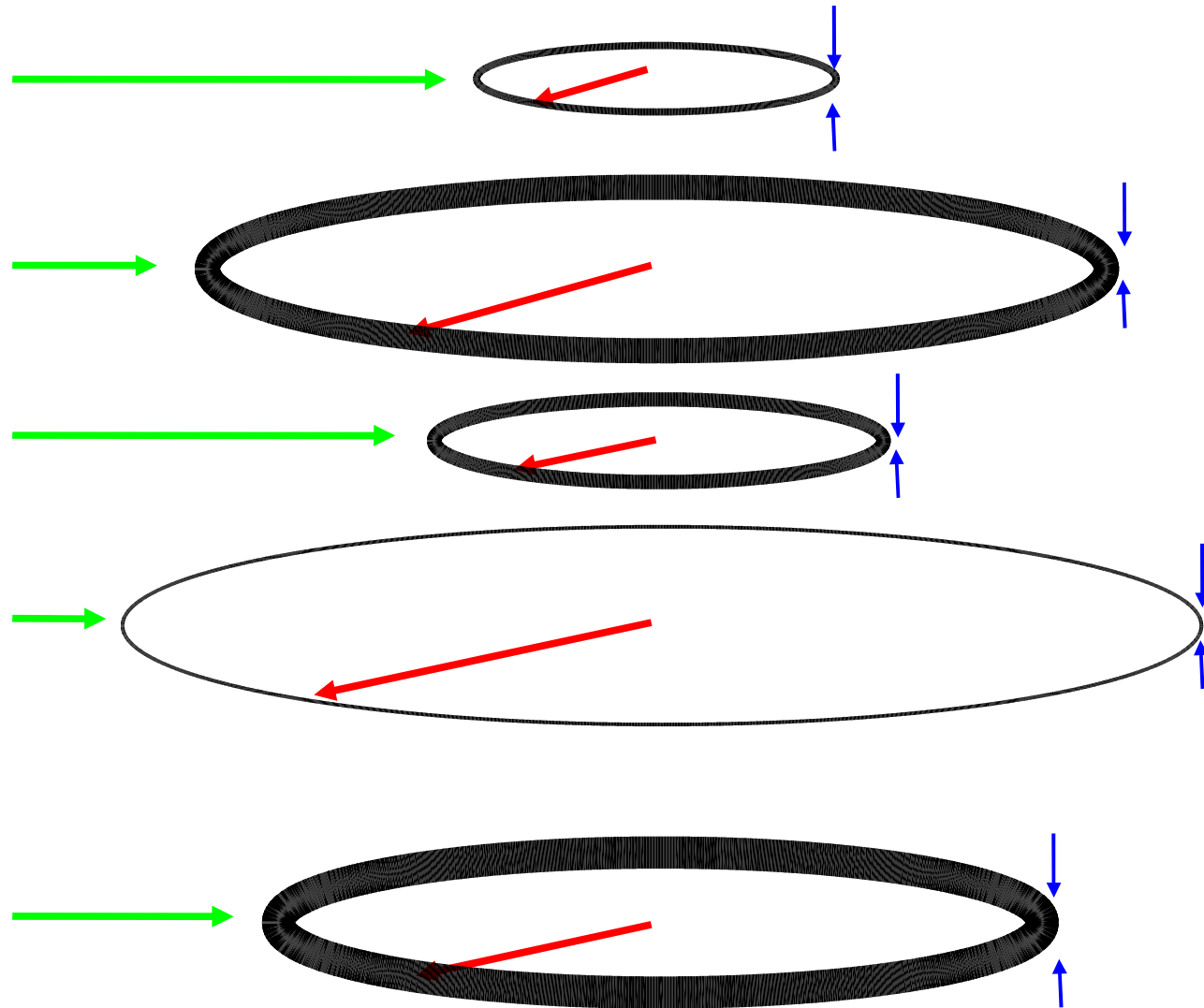
5 heights

5 masses

15 parameters

Only $m = 0$ moments.

Use parameters to null
Newtonian moments and
to maximize 310 moment.

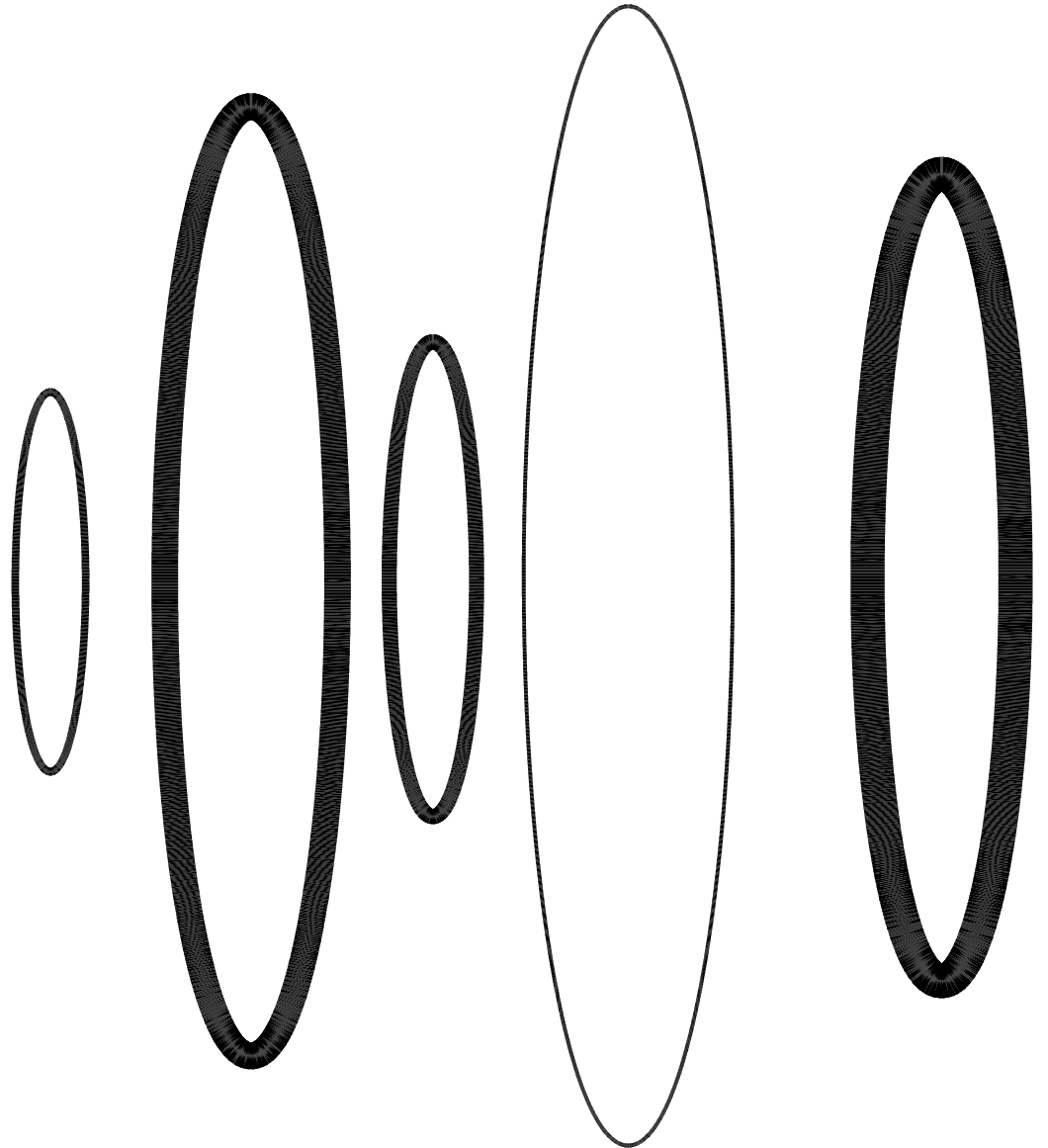


How to design what will do...

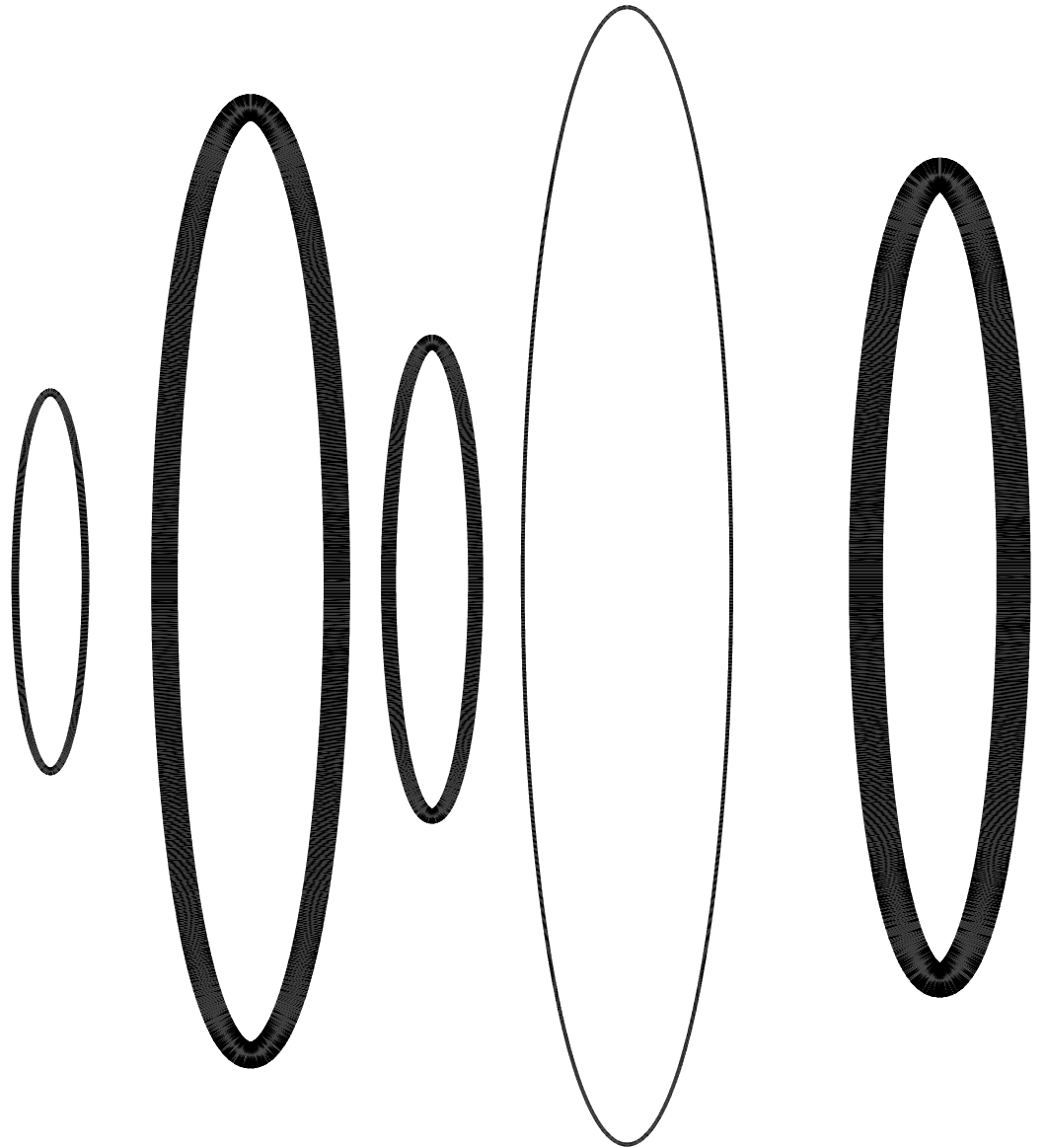
Now rotate by 90 degrees.

Nullified Newtonian moments remain zero.

Large 310 moment rotates into a large 311 moment.



How to design what will do...



Now for the Source Mass

Newtonian Potentials:

$$V_{22m} = 0 \text{ (for all } m)$$

$$V_{331} = 0$$

$$V_{441} = 0$$

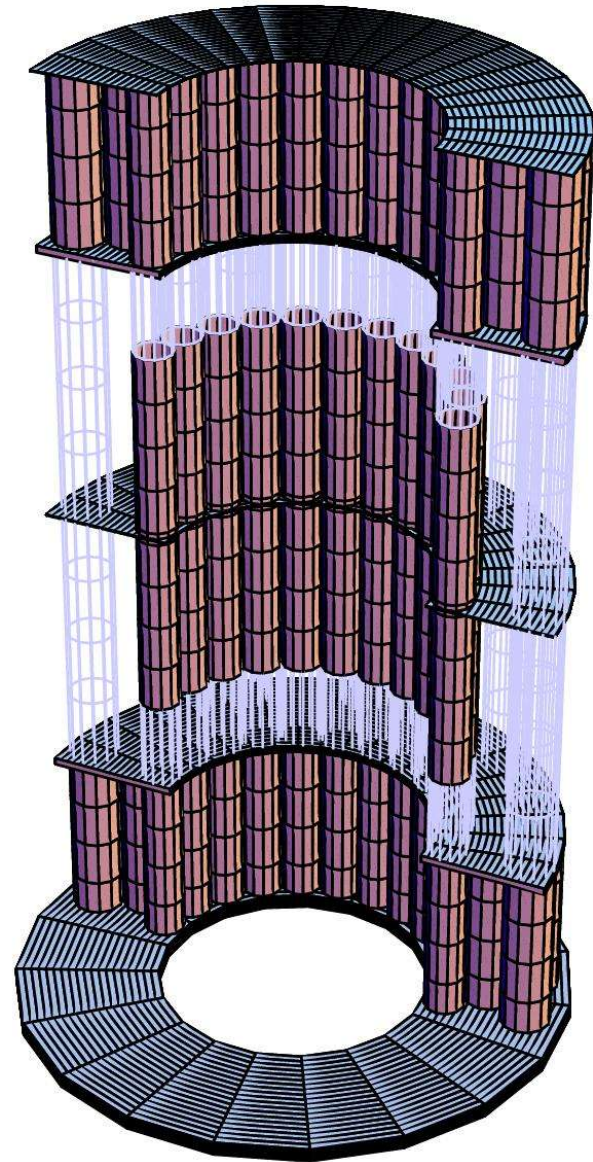
$$V_{551} = 0$$

$$V_{661} = 0$$

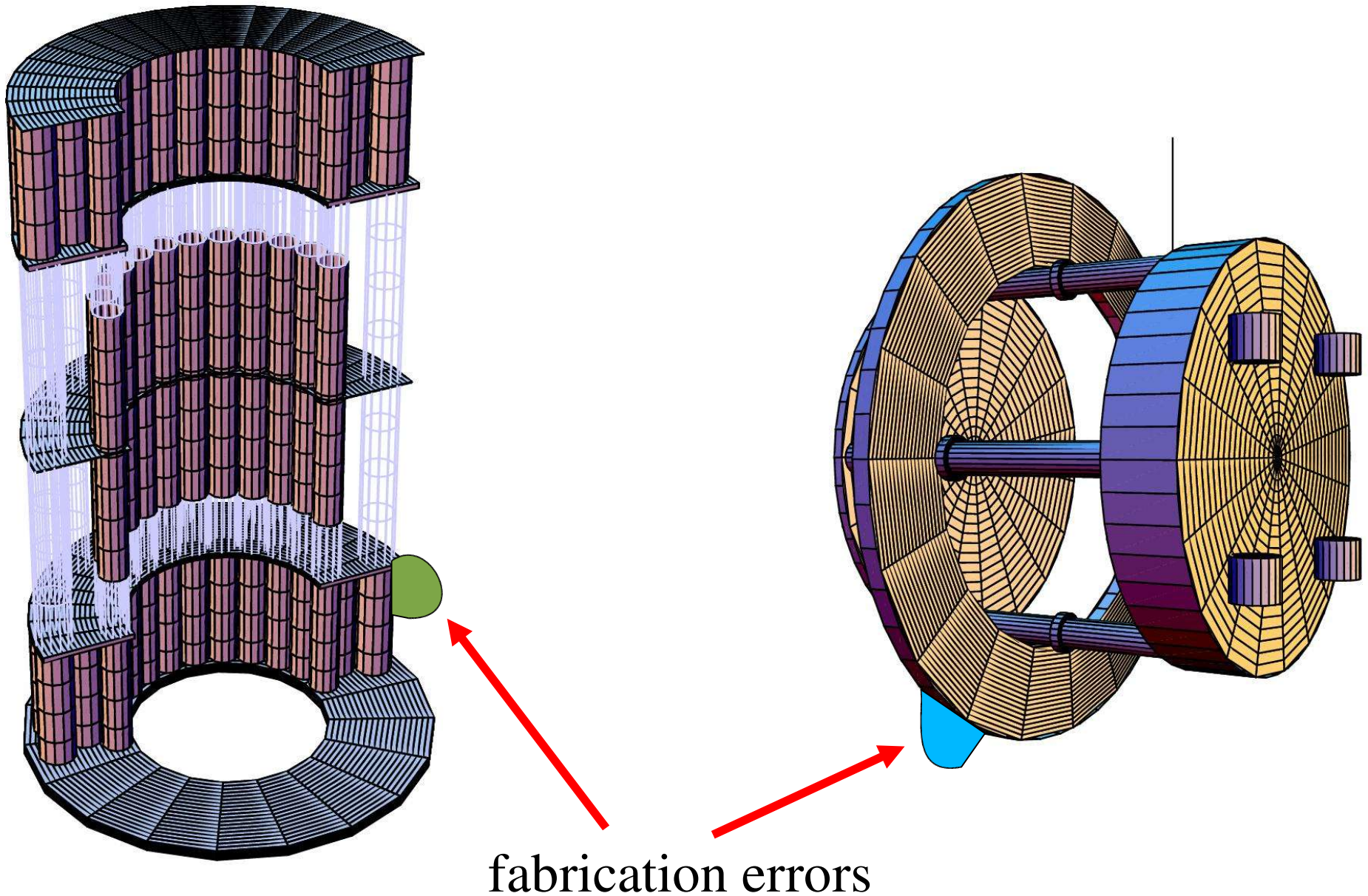
$$V_{771} = 0$$

non-Newtonian Potential:

$$V_{311} = \text{Large}$$

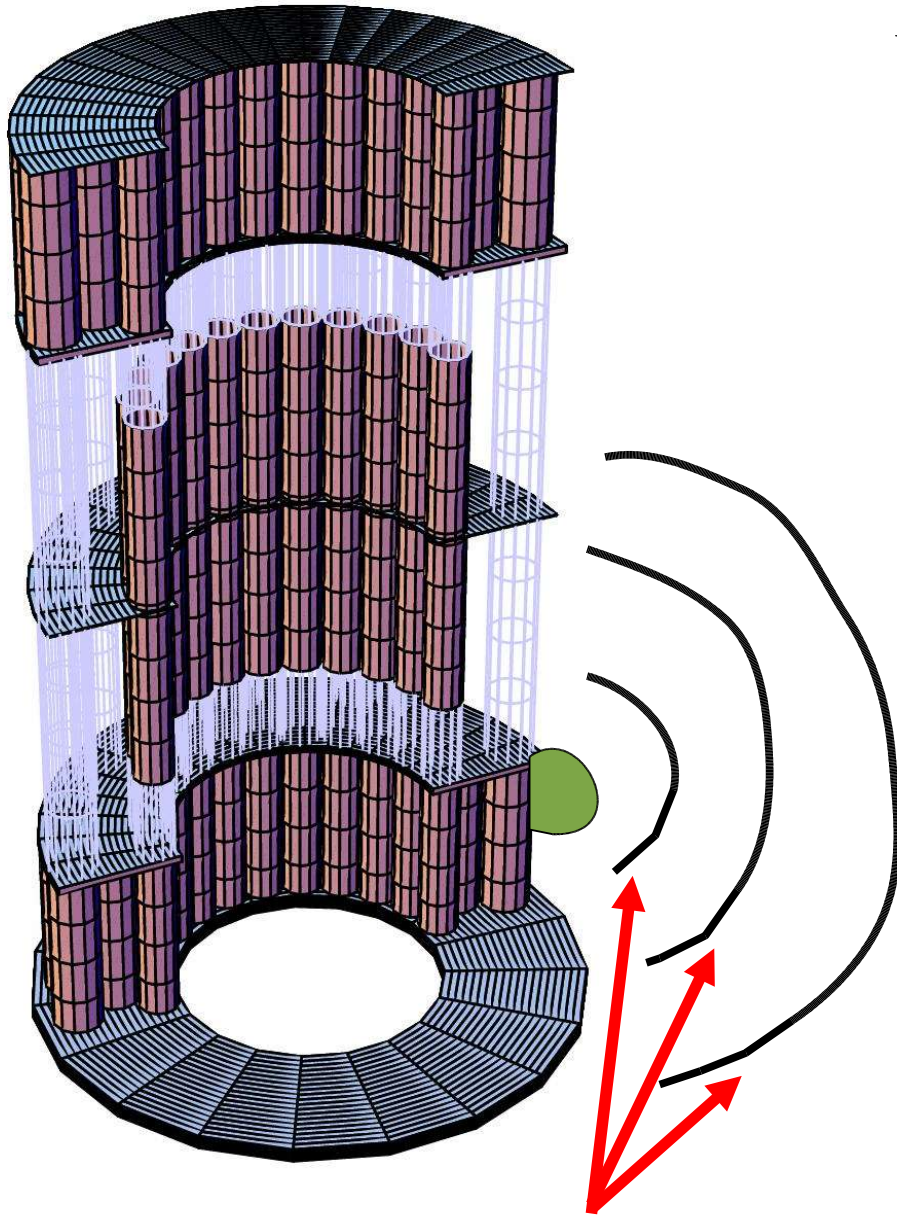


Leading Systematic Effect

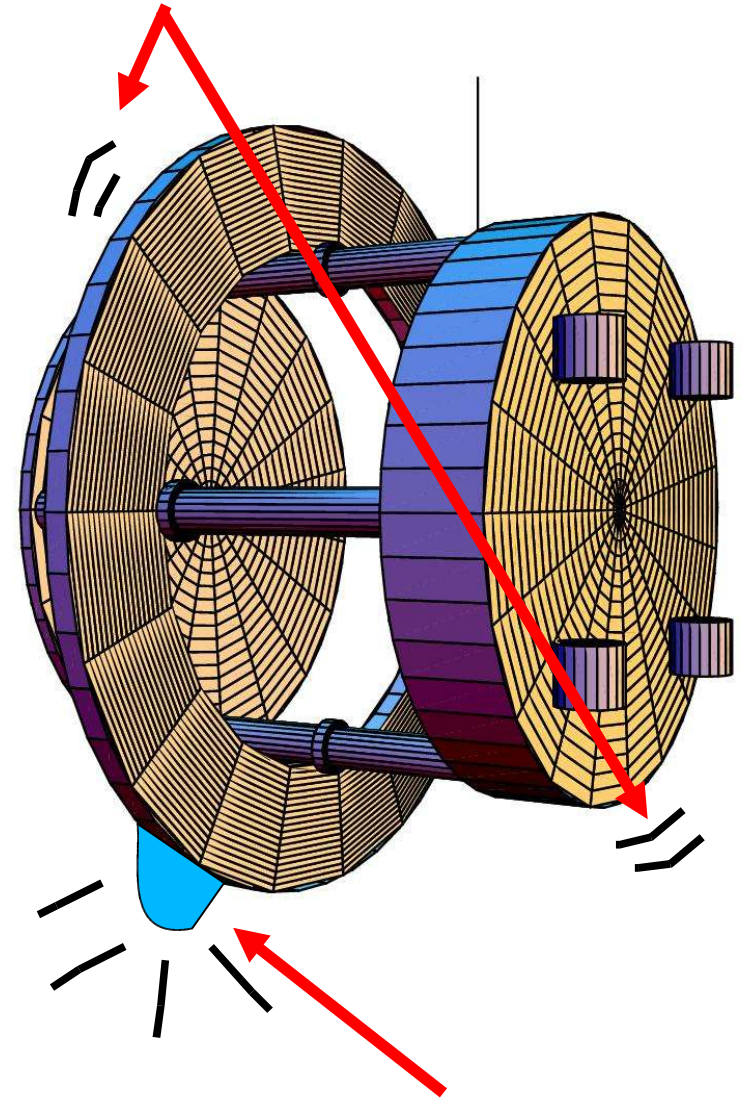


Leading Systematic Effect

very small pendulum response



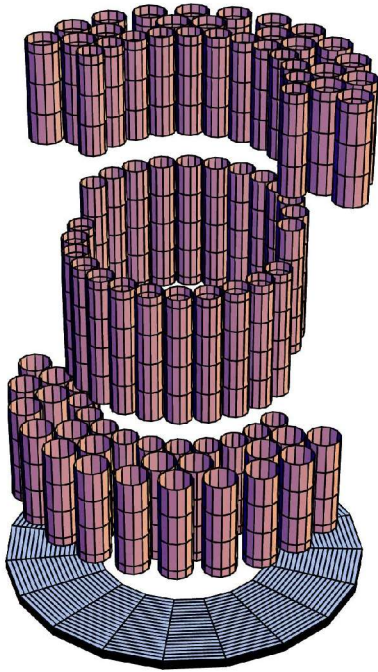
small unwanted gravitational field



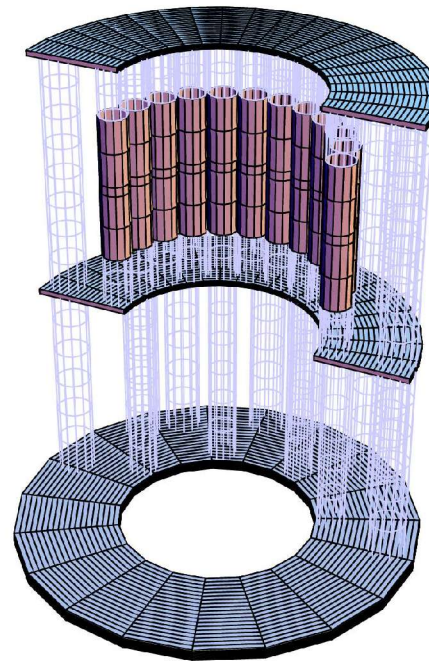
small unwanted mass moment

Minimizing the Leading Systematic Effect

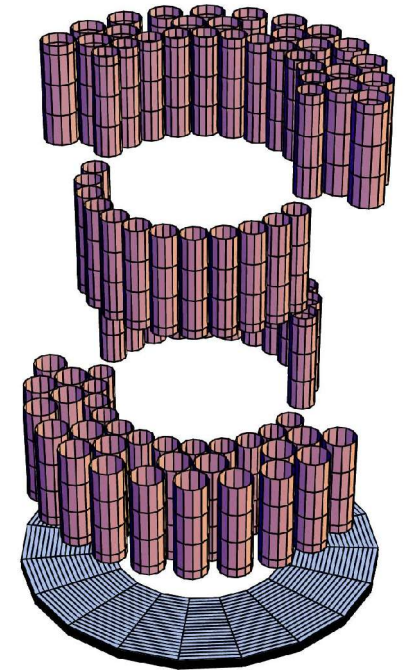
Exaggerated Source Mass Configurations



221



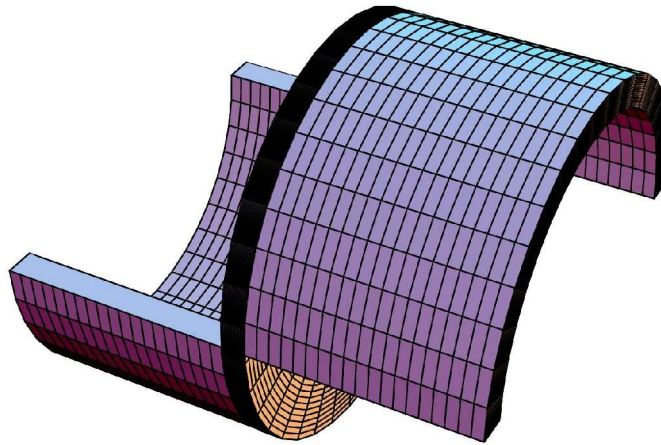
331



441

Minimizing the Leading Systematic Effect

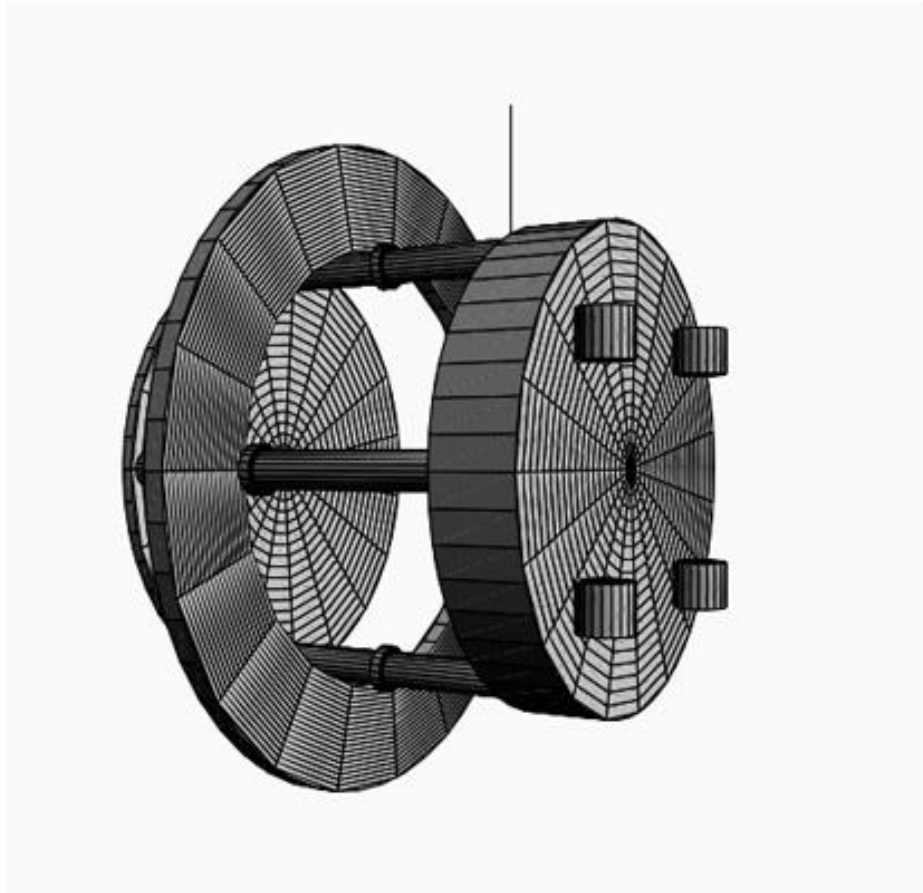
Exaggerated Pendulum



221 pendulum

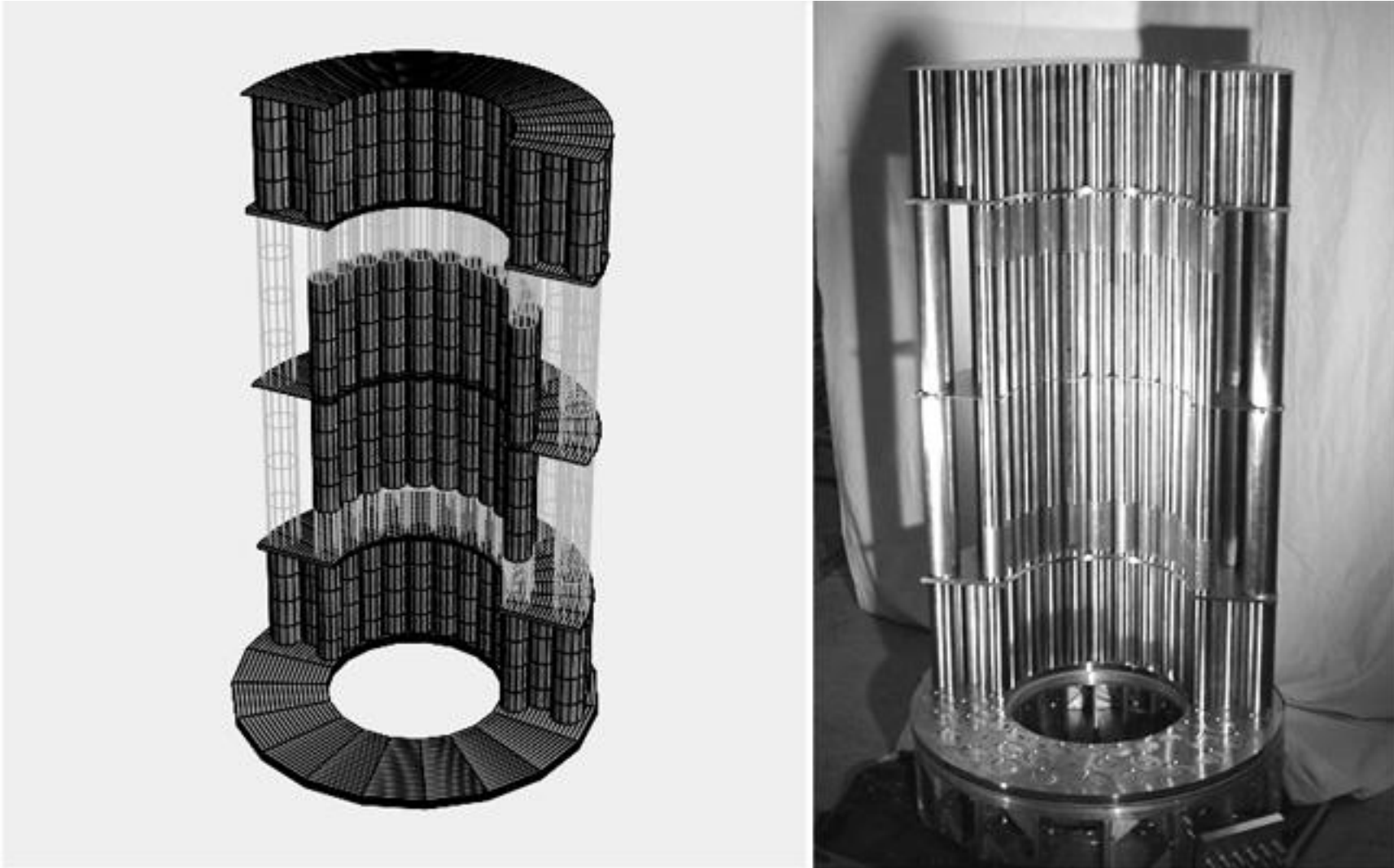
$$V_{441} = \frac{d}{dz} V_{331} = \frac{d^2}{dz^2} V_{221}$$

Parts List: ISLV Pendulum



gold coated, fused silica, 240 grams

Parts List: ISLV Source Mass



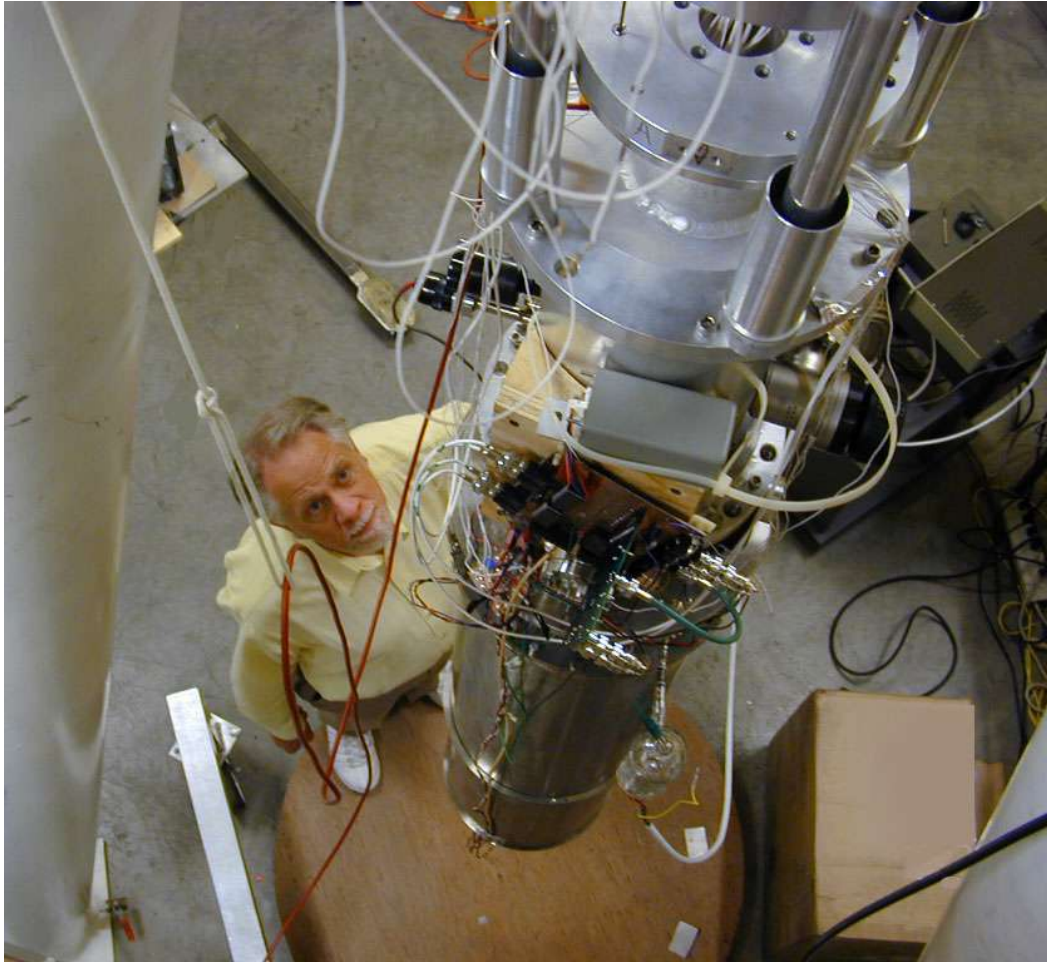
stainless steel, 1500 kg

Parts List: Exaggerated 221 Pendulum



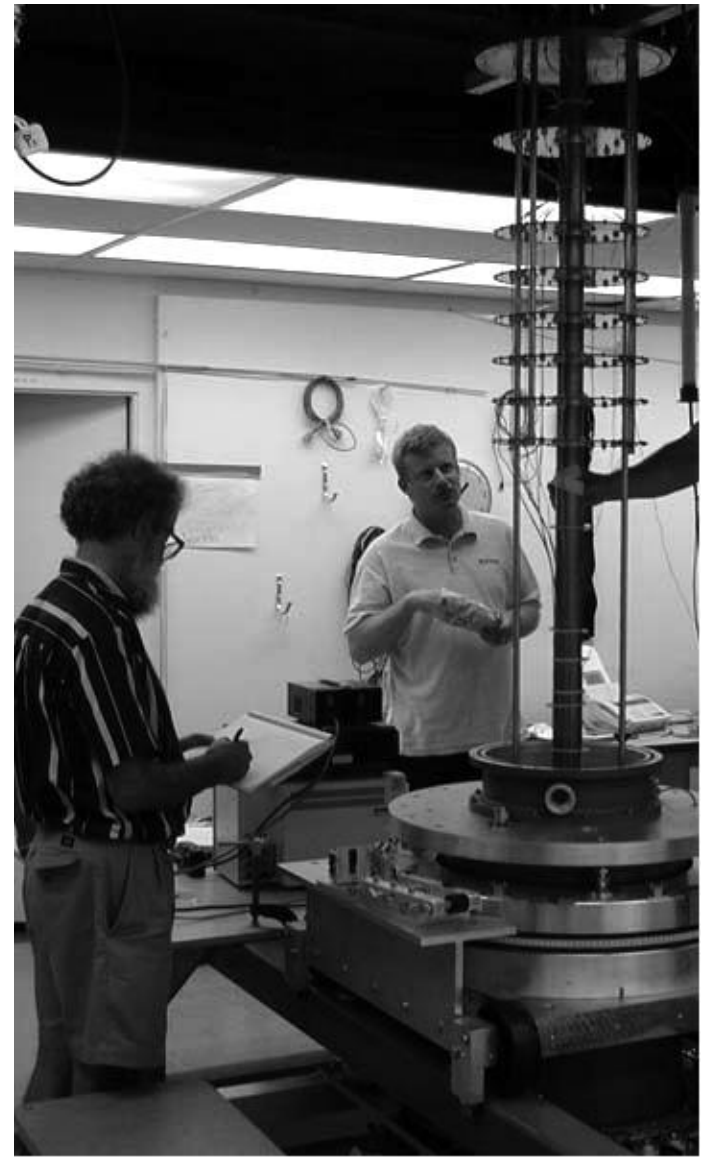
aluminum, 240 grams

Parts List: Instrumentation



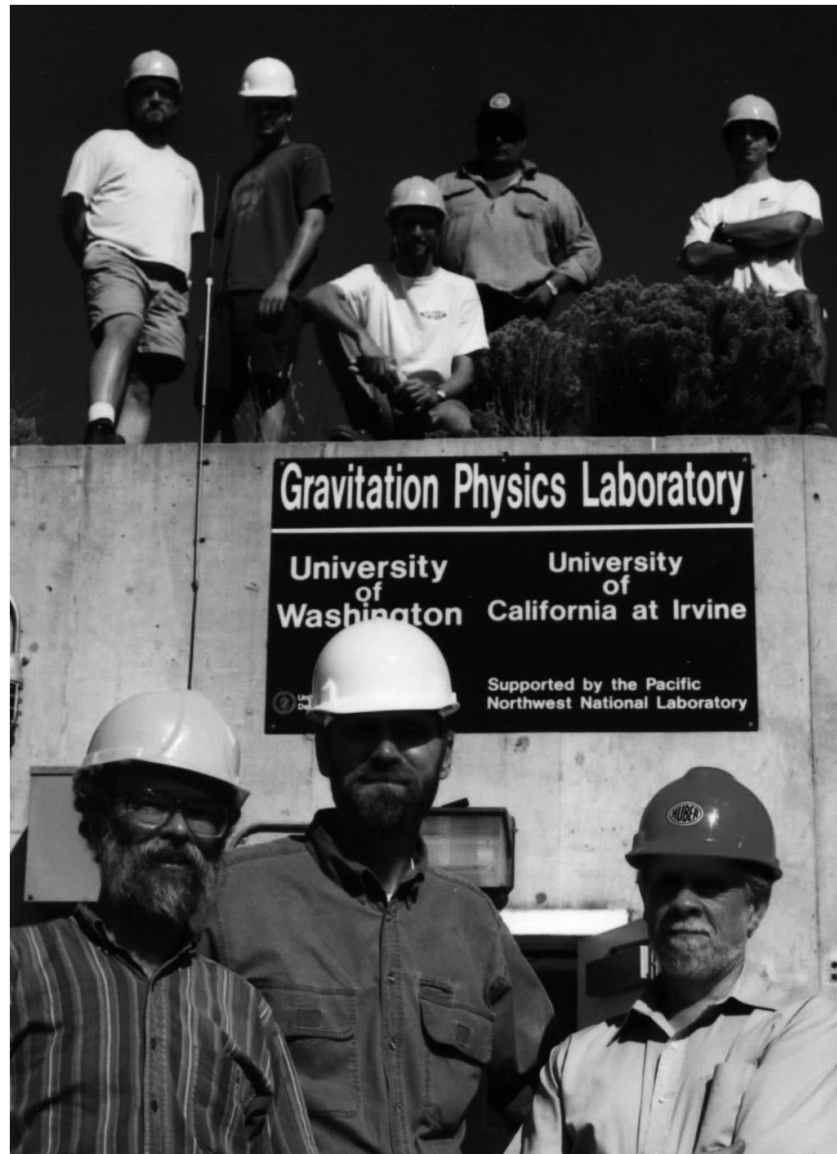
Room Temperature Apparatus

Parts List: Instrumentation



Cryogenic Apparatus

Parts List: Batelle Facility



Nike Missile Bunker

State of the System

- Both cryogenic and ambient temperature instruments are operating at BGPL
- Optimization and calibration will require another 3 to 4 months
- ISLV measurement tasks will begin in the summer of 2007
- Completion expected by spring of 2009

Conclusions

- Second-order sensitive to fabrication errors
- Source mass produces no low-order Newtonian fields by design
- Pendulum is not sensitive to low-order Newtonian fields by design
- Both pendulum and source are maximally sensitive to a gradient of the Laplacian of the non-Newtonian potential
- Cryogenic apparatus to reduce thermal noise and improve magnetic shielding
- Quiet both geologically and anthropogenically