Is GeV emission from Gamma-Ray Bursts of external shock origin?

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Accepted 2011 March 4. Received 2011 February 22; in original form 2010 December 30

ABSTRACT

Recent observations of Gamma-Ray Bursts (GRBs) by the Fermi Large Area Telescope (LAT) revealed a power-law decay feature of the high-energy emission (above 100 MeV), which led to the suggestion that it originates from an external shock. We analyse four GRBs (080916C, 090510, 090902B and 090926A) jointly detected by Fermi LAT and Gamma-ray Burst Monitor (GBM), which have high-quality light curves in both instrument energy bands. Using the MeV prompt emission (GBM) data, we can record the energy output from the central engine as a function of time. Assuming a constant radiative efficiency, we are able to track energy accumulation in the external shock using our internal/external shell model code. By solving for the early evolution of both an adiabatic and a radiative blastwave, we calculate the high-energy emission light curve in the LAT band and compare it with the observed one for each burst. The late time LAT light curves after $T_{90}$ can be well fitted by the model. However, due to continuous energy injection into the blastwave during the prompt emission phase, the early external shock emission cannot account for the observed GeV flux level. The high-energy emission during the prompt phase (before $T_{90}$) is most likely a superposition of a gradually enhancing external shock component and a dominant emission component that is of an internal origin.


1 INTRODUCTION

The Large Area Telescope (LAT; Atwood et al. 2009) aboard the Fermi Gamma Ray Space Telescope (Fermi) has recently detected nearly 20 Gamma-Ray Bursts (GRBs, e.g. Abdo et al. 2009a,b; Ackermann et al. 2010, 2011; see Zhang et al. 2011 for a synthetic study). Among them, several bright GRBs (e.g. GRBs 080916C, 090510, 090902B and 090926A) have well sampled long-term LAT-band light curves. In logarithmic space, these GRBs have count rates that rise, peak and begin decaying before the MeV prompt emission is over, i.e. peaking at a time smaller than $T_{90}$ defined in the Gamma-ray Burst Monitor (GBM; Meegan et al. 2009) detector energy band. The post peak light curve typically has a decay slope steeper than $-1$ (e.g. ranging from $-1.3$ to $-2$, Ghisellini et al. 2009; Zhang et al. 2011). The simple temporal behaviour (a broken power-law light curve) of LAT emission led to the suggestion that GRB GeV emission is of an external forward shock origin (Kumar & Barniol Duran 2009, 2010), possibly from a highly radiative blastwave (Ghisellini et al. 2009) or a Klein–Nishina cooling dominated adiabatic blastwave (Wang et al. 2010). A simple broken power-law light curve is expected from the blastwave evolution of an instantaneously injected fireball with fixed explosion energy. Such an approximation is valid if the analysed time-scale is much longer than $T_{90}$, the duration of the prompt gamma-ray emission itself. However, for the early blastwave evolution, especially during the epoch when the central engine is still active (as is the case for the LAT GRBs discussed in this paper), one would not expect a simple light-curve evolution, since the energy output from the central engine is continuously injected into the blastwave.

The high-quality spectral and temporal data of GRBs codetected by Fermi LAT and GBM allow us to track the energy output from the central engine as a function of time. Recently we have developed a shell code to model the internal and external shock development for arbitrary central engine activities (Maxham & Zhang 2009). By processing the spectral and temporal evolution data of Fermi GRBs using the method described in Zhang et al. (2011), we can model the early development of the external shock based on first hand data.

2 DATA ANALYSIS

We study four bright LAT GRBs (080916C, 090510, 090902B and 090926A). GBM and LAT data reduction was carried out using the data analysis script introduced in Zhang et al. (2011). This
the range of steeper than the fully radiative condition. With \( \rho = 0 \) representing the purely adiabatic case and \( \rho = 1 \) representing where the value of \( \rho \) is the initial mass of the ejecta. As a result, one has another differential equation, \( \frac{dM}{dt} = \rho c = (\sqrt{\gamma^2 - 1}/\gamma)c \), a statement of conservation of energy and momentum across the blastwave. For an instantaneous explosion with constant energy, the motion of this decelerating ejecta along with the medium collected along the way, known as the ‘blastwave’, is governed by three differential equations (Chiang & Dermer 1999; Huang et al. 2000): 

\[
d\gamma/d\tau = -\frac{\rho}{\gamma}m/R^2\gamma(1 + \gamma^n) + \frac{8\pi^2\rho^2 R^6}{9M_0^3}(1 + \gamma^n),
\]

where \( \gamma \) is the Lorentz factor and \( m \) is the density of the ambient medium, \( R \) is the distance from the central engine, \( \rho \) is the density of the ambient medium, \( \gamma \) is the Lorentz factor of the shell, \( M \) is the swept-up mass and \( M = M_0 + \gamma m \) is the total effective mass including the internal energy of the blastwave, where \( M_0 \) is the initial mass of the ejecta. As a result, one has another differential equation, 

\[
\frac{dM}{d\tau} = \frac{1}{(1 - \epsilon)\gamma + \epsilon}.
\]

3 EXTERNAL SHOCK MODELLING

3.1 Blastwave evolution

We model a GRB as an explosion of many matter shells with some mass and Lorentz factor (Rees & Mészáros 1994). As the first matter shell moves outward into the ambient medium, it slows down when sweeping up this medium (Mészaros & Rees 1993). As time goes by, more and more trailing shells pile up on to the leading decelerating shell (Rees & Mészáros 1998).

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To evaluate \( \gamma \)-ray energy \( E_{\gamma} \) as a function of time, we divide the light curve into multiple time bins for each burst. For each time bin (with uneven duration denoted as \( \Delta T \)), we record its average flux \( F \) in the GBM band, along with other useful information such as spectral parameters and the maximum photon energy.

The total gamma-ray energy released in this time bin (ith) is therefore

\[
E_{\gamma,i} = \frac{4\pi d_k^2 F_i \Delta T_i}{1 + z},
\]

where \( z \) is the redshift (see Table 1 for values of each burst), \( d_k \) is the luminosity distance of the source, and the concordance cosmology with \( \Omega_m = 0.7 \) and \( \Omega_\Lambda = 0.3 \) is adopted in the calculation.

Adopting \( E_{\gamma,i} = \xi E_{\gamma,i} \), we then progressively increase the total energy in the blastwave \( E_{\gamma} = \sum E_{\gamma,i} \) by adding \( E_{\gamma,i} \) in each step. For each time step, we calculate the light curve giving the available \( E_{\gamma} \). This results in a series of light-curve solutions. The final light curve is then derived by jumping to progressively higher levels due to additional energy injections in each time step (see also Maxham & Zhang 2009). This would result in a series of ‘glitches’ in the light curves, each representing injection of energy from ith shell into the blastwave.

Besides the energy, we also derive the (lower limit) Lorentz factor \( \gamma_{\gamma,i} \) of each shell. This parameter is important, especially for early shells, since it determines the deceleration time of a certain shell. This is particularly relevant for the first shell. The Lorentz factors of later shells are also relevant for two reasons. First, they can be
used to calculate the effective Lorentz factor of a ‘merged’ shell after adding energy to an existing shell. This is needed to calculate the deceleration time of the blastwave solutions. Secondly, since the observed time for a late energy injection is defined by (Maxham & Zhang 2009)

\[ t_{\text{col}} = t_{\text{ej}} + \frac{(t_{\text{col}} - t_{\text{ej}})}{2\gamma^2}, \]  

where \( t_{\text{ej}} \) and \( t_{\text{col}} \) are the times of ejection and collision measured in the rest frame of the central engine. The effect of \( \gamma \) becomes progressively less important, since at large \( t_{\text{ej}} \)'s, the second term in equation (4) becomes negligible so that the observed collision time is essentially defined by the ejection time. In any case, we derive the constraints on \( \gamma \) for each time bin using the pair opacity argument as described below.

To derive a constraint on the Lorentz factor, we have collected the spectral parameters and the observed maximum photon energy \( E_{\text{max},i} \) for each time bin. One can then derive the maximum photon energy in the cosmological local frame, i.e. \( E_{\text{max},i} = E_{\text{max},i}(1+z) \). Requiring the pair production optical depth to be less than unity for \( E = E_{\text{max},i} \), we can write a general constraint in the parameter space of \( R \) and \( \gamma \) (where \( R \) is the distance of the emission region from the central engine, Gupta & Zhang 2007; Zhang & Pe’er 2009), i.e.

\[ R(\gamma) > \sqrt{\frac{C(\beta)\sigma_T d^2}{1 - \beta f_0}} \left( \frac{E_{\text{max}}}{511 \text{keV}} \right)^{1 - \beta} \left( \frac{\gamma}{1 + z} \right)^{2+2\beta}, \]  

where \( \sigma_T \) is the Thompson cross-section, \( \beta \) represents the slope of the power-law component for GRBs 090902B and 090510 and the Band function high-energy spectral parameter for GRBs 080916C and 090926A, and \( f_0 = A \cdot \Delta T(E_{\gamma}(\alpha - \beta)/(2 + \alpha))^{\alpha - \beta} \exp(\beta - \alpha)(100 \text{keV})^{-\beta} \) for the Band function model, and \( f_0 = K \cdot \Delta T(100 \text{keV})^{-\beta} \) for the simple power-law model, where \( A \) and \( K \) are normalization factors (both normalized to 100 keV). The approximation \( C(\beta) \approx (7/6)(-\beta)^{3/2}(1 - \beta)^{3/2} \) (Svensson 1987) is adopted to perform the calculation. In order to further constrain \( \gamma \), one needs to make an assumption about \( R \). Without other independent constraints, we apply the conventional assumption of internal shocks, so that \( R(\gamma) = \gamma^2 c (\delta t/1 + z) \), where \( \delta t \) is the observed minimum variability timescale. Combining equation (5), the lower limit for \( \gamma \) is derived for each time bin of each burst (see also Lithwick & Sari 2001, Abdo et al. 2009a,b). In our calculation, we generally adopt \( \gamma_i \) as the derived lower limit. This is because the derived Lorentz factors of other GRBs using the afterglow deceleration constraint (Liang et al. 2010) or photosphere constraint (Pe’er et al. 2011) are all below or consistent with these lower limits derived from the opacity constraints (Abdo et al. 2009a,b; Ackermann et al. 2010, 2011).

### 3.3 Model results

Feeding these data into our shell model code, letting each shell be ejected with energy \( E_{\text{ej},i} \) and Lorentz factor \( \gamma_i \) at time equal to that of the beginning of the bin time, we can calculate the early blastwave evolution and LAT band (integrated over \( \gtrsim 100 \text{MeV} \)) light curve for the four GRBs.

To match the observed steep decay (with slope \( \sim -1.5 \)), we adopt a radiative fireball solution or an adiabatic fireball solution with steep electron energy index. Even though each solution (for a fixed kinetic energy) has a steep decay slope, the overall light curve shows a shallower decay due to piling up of successive shells ejected later, with glitches introduced by jumping among the solutions. As an example, the radiative model light curve of GRB 080916C as compared with observation is presented in Fig. 1. The top panel shows the long-term evolution, while the bottom panel is the zoomed-in early light curve. The dotted lines denote the blastwave solutions with progressively increasing total energy. The lowest one corresponds to the first time bin, the second lowest corresponds to adding the energy of the second time bin, etc.

Since the light curve is chopped into discrete time bins, the blastwave energy is added in discrete steps. This introduces some artificial glitches in the light curve. Such an approximation is more realistic for GRBs with distinct emission episodes. For GRB 080916C, the light curve is more appropriately approximated as a continuous wind with variable luminosity. The artificial glitches should appear to be more smeared. For this reason, we have smoothed the glitches to make more natural transitions between solutions. The model afterglow parameters (the fraction of electron energy \( \epsilon_e \), the fraction of magnetic energy \( \epsilon_B \) and the number density \( n \)) are presented in Table 1. These are in general consistent with the parameter constraints derived by Kumar & Barniol Duran (2009, 2010).

In general, the model light curve of GRB 080916C cannot fit the early LAT data. Making the model suitable to fit the late-time steep decay, the early model light curve level is too low to account
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Figure 1. The predicted external shock >100 MeV light curve of GRB 080916C for a radiative blastwave solution (yellow line) as compared with the data (blue points). Successive light curves that correspond to different total blastwave kinetic energy are shown as dashed lines. The top panel shows the global light curve, while the bottom panel shows a zoom view where the flux deficit at early times can be clearly seen.

for the observed data. Alternatively, one can make the early model light curve match the observed flux level. Then inevitably the late time afterglow level exceeds the observed level significantly due to the continuous energy injection. We believe that if the LAT band emission after $T_{90}$ originates from the external shock, then the LAT emission during the prompt emission phase cannot be solely interpreted by the external shock model. The external shock contribution is relatively small, especially during early epochs when energy in the blastwave is small. As a result, the GeV emission during the prompt phase must be of an internal origin. This is consistent with the fact that the entire GBM/LAT emission during the prompt phase can be well fit by a single Band-function spectral model in all the time bins (Abdo et al. 2009a; Zhang et al. 2011). We have also modelled GRBs 090510, 090902B and 090926A. The model parameters (for both radiative and adiabatic solutions) are listed in Table 1, and the results for radiative solution are shown in Fig. 2. In all cases, the slope and flux level of the data are matched in the latter part of the curve only. During the prompt emission phase, the data points rise above the flux prediction of the external shock model, suggesting that GeV emission is a superposition of external and internal components during the prompt emission phase ($T < T_{90}$). This conclusion is valid for both the adiabatic and radiative solutions. The difference between the two is that the adiabatic model invokes a shallower $p$ but a larger $\xi$ (and hence a larger energy budget) to fit the same data.

Figure 2. Model predictions of >100 MeV light curve (for a radiative blastwave solution) versus observed data for GRBs 090510, 090902B and 090926A. The conventions are similar to Fig. 1, but without successive solutions specifically plotted.

4 CONCLUSIONS AND DISCUSSION

Using the first-hand Fermi data, we have tracked the energy output from the central engine and modelled the early blastwave evolution of four bright LAT GRBs. The predicted >100 MeV light curve is found unable to account for the observed LAT emission during the prompt emission phase. The main reason is that during the phase when the central engine is still active, the forward shock is continuously refreshed by late energy injection, so that the afterglow decays much slower than the case predicted by an instantaneously ejected constant energy fireball. This suggests that at least during the prompt emission phase, the LAT band emission is not of external forward shock origin. This is in contrast to the suggestion of
Ghisellini et al. (2009), Kumar & Barniol Duran (2009), who did not consider the energy accumulation during the prompt emission phase and interpreted the entire GeV emission as of the external shock origin of an instantaneously ejected fireball. Feng & Dai (2010) considered this energy-accumulation process, but made the assumption that the central engine ejects shells with progressively increasing Lorentz factors. This model can reproduce a steep rising light curve before the afterglow peak time, but would still have difficulty accounting for the observed simple power-law decay after the peak, since the energy injection process discussed in this paper still plays an important role before the end of GBM-band prompt emission.

Our conclusion is based on the assumption that GRB radiative efficiency is essentially a constant throughout the burst. In order to interpret the entire afterglow as due to the external forward shock origin, one needs to ‘artificially’ assume that the GRB efficiency increases with time, so that the late-time central engine activity, even though producing bright γ-ray emission, adds little kinetic energy into the blastwave. Another possibility would be to assume that the initial energy of the blastwave does not produce MeV gamma-rays, and this dark component contributes to the majority of the afterglow energy. We believe that both such assumptions are unnatural and contrived.

Our conclusion is consistent with some independent arguments. From data analysis, Zhang et al. (2011) showed that during the prompt emission phase the GeV emission has rapid variability and traces the MeV emission well1. For GRB 080916C, the entire GBM/LAT emission can be modelled by a single Band function component in all the time bins (see also Abdo et al. 2009a). For GRB 090902B, even though GeV emission belongs to a distinct spectral component, its flux seems to track the flux of the MeV component nicely, suggesting a connection in the physical origin (see Pe’er et al. 2011 for modelling). A more definite argument in favour of an internal origin of GeV emission in GRB 080916C is that the GeV light-curve peak coincides the second peak in the GBM light curve, suggesting that GeV emission is the spectral extension of MeV emission to higher energies (Zhang et al. 2011). Also individual case studies of GRB 090902B (Pe’er et al. 2011; Liu & Wang 2011) and GRB 090510 (He et al. 2011) all suggest that the external shock model cannot interpret the prompt GeV data. In general, our modelling suggests that it is possible to use the external shock model to interpret GeV emission after the prompt emission phase, but not during the prompt emission phase (see also Kumar & Barniol Duran 2010).

Since the observed GeV light curve is consistent with a simple power-law decay after the peak time, one requires a coincidence in the current picture so that the external shock emission light curve appears as a natural extension of the early GeV light curve that is of an internal origin. We note, however, that the external shock energy parameter (ξ) and other parameters (e.g. εe, εb) adopted in our calculations are all within the reasonable range, suggesting that the calculated external shock GeV emission can be indeed at the expected level. Parameter space explorations suggest that there is a good range of parameters that can reasonably reproduce the late light curve, without needing to fine-tune the parameters. Furthermore, according to our data analysis, the derived GeV light curves are not strict power laws. Some possible features (e.g. wiggles in GRB 080916C and GRB 090902B and a flattening feature in GRB 090510 and GRB 090926A) that may be related to the merging of the external shock component are observed. The coincidence problem is therefore not as severe as it appears.

On the other hand, the model that interprets the prompt GeV emission as due to an external shock origin also demands a coincidence in the spectral domain, so that the internal and the external shock components would conspire to mimic a single Band function in GRB 080916C (Kumar & Barniol Duran 2009). Since the Band function perseveres in the time-resolved spectra of several time bins (Abdo et al. 2009a; Zhang et al. 2011), that model demands coincidence in all the time bins. This coincidence problem may be more demanding than the model discussed in this paper.

Our conclusion also has implications for understanding GRB prompt emission physics, in particular, the composition of the GRB outflow. The internal origin of the GeV emission in GRB 080916C makes it essentially impossible to interpret the entire Band spectrum with the photosphere model (e.g. Beloborodov 2010; Lazzati & Begelman 2010). The lack of photosphere emission then demands a Poynting flux dominated outflow at least for this burst (Zhang & Pe’er 2009; Fan 2010). This argument, along with other evidence uncovered in other GRBs (e.g. Narayan & Kumar 2009), calls for new models of GRB prompt emission in the Poynting flux dominated regime (e.g. Zhang & Yan 2011).

ACKNOWLEDGMENTS

This work is partially supported by NSF AST-0908362 and NASA NNX09AT66G, NNX10AD48G. We thank Xue-Feng Wu for helpful discussion.

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