

Detecting Terrestrial Planets in Transiting Planetary Systems



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Planet Formation

How massive is the protoplanetary disk?

How long does it take to make a planet?

What is the lifetime of a disk?

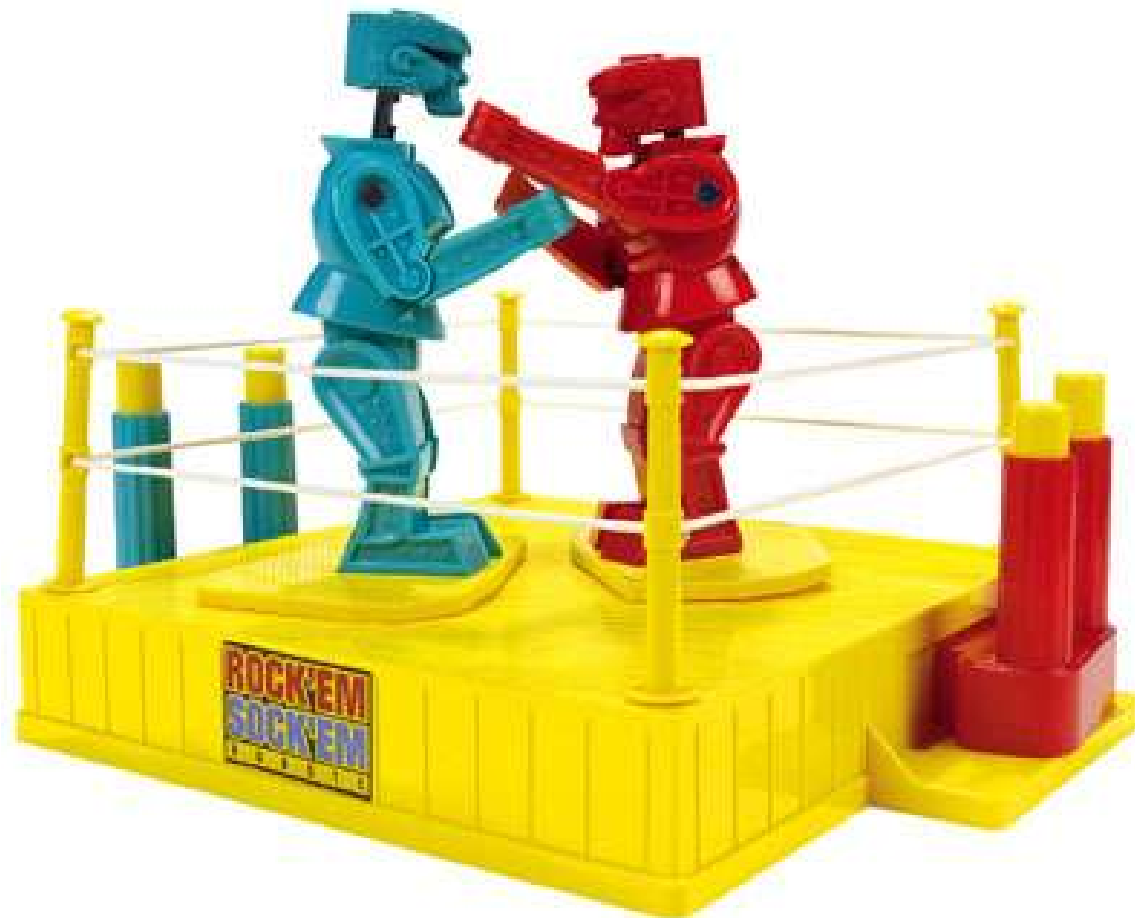
Why are there hot Jupiters?

How can I make hot Jupiters?

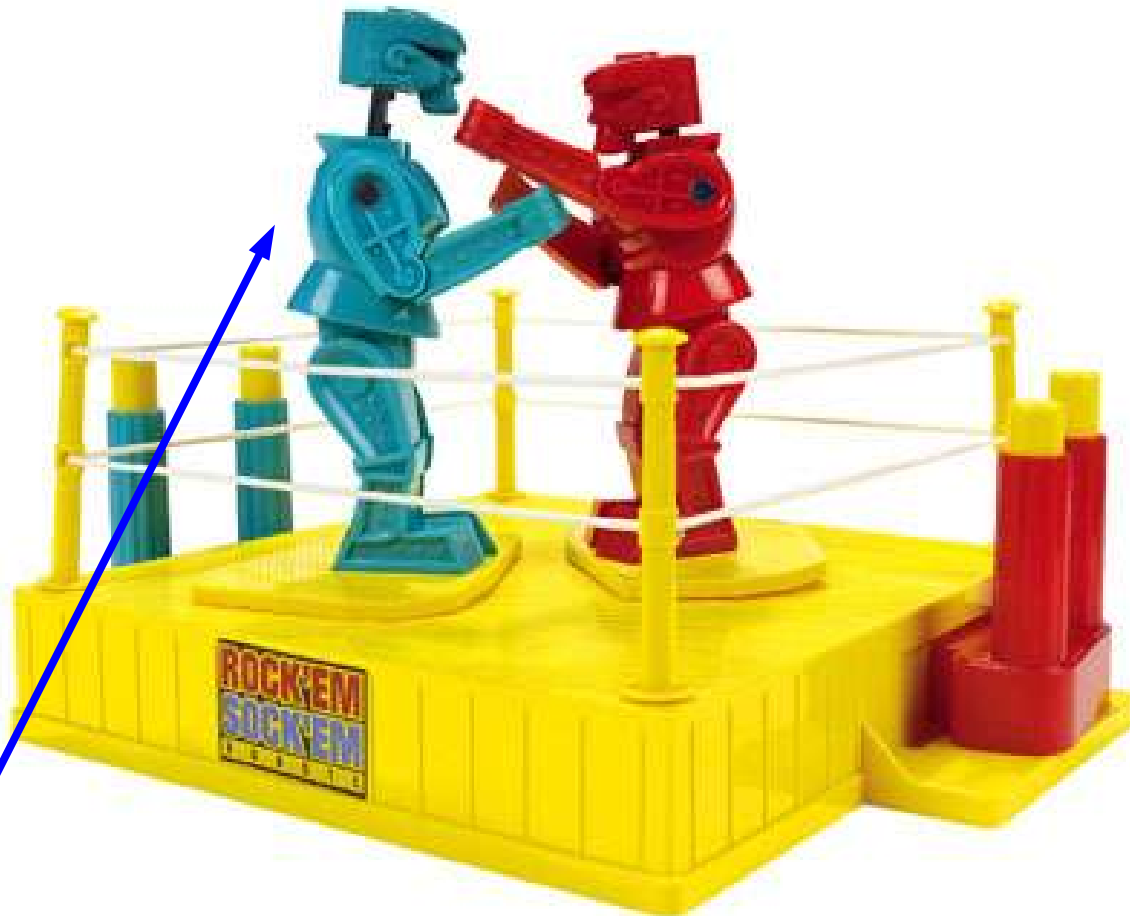
What is going to happen to Anna Nicole's baby?

Why are some of the eccentricities of distant planets so big?

Planet Formation

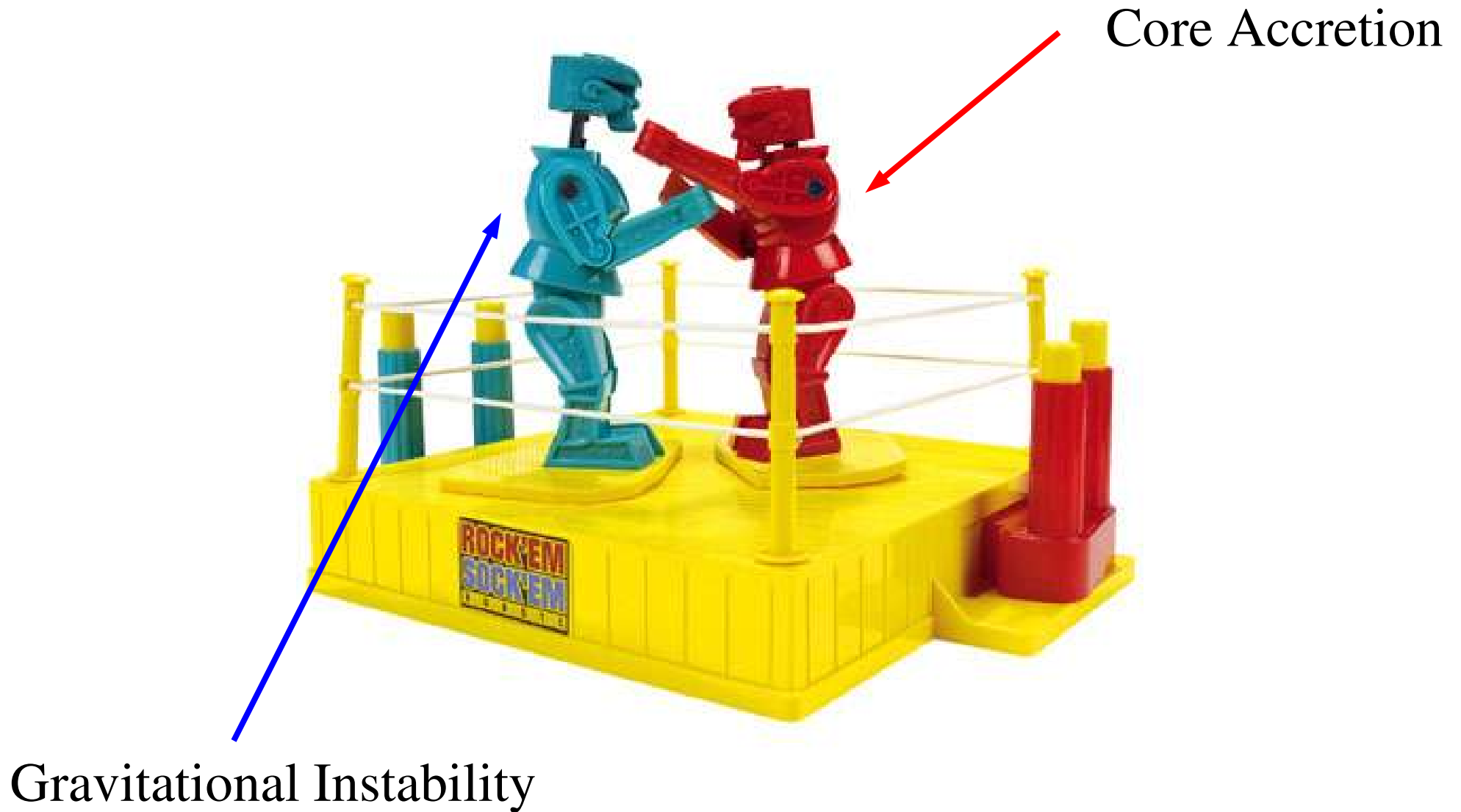


Planet Formation

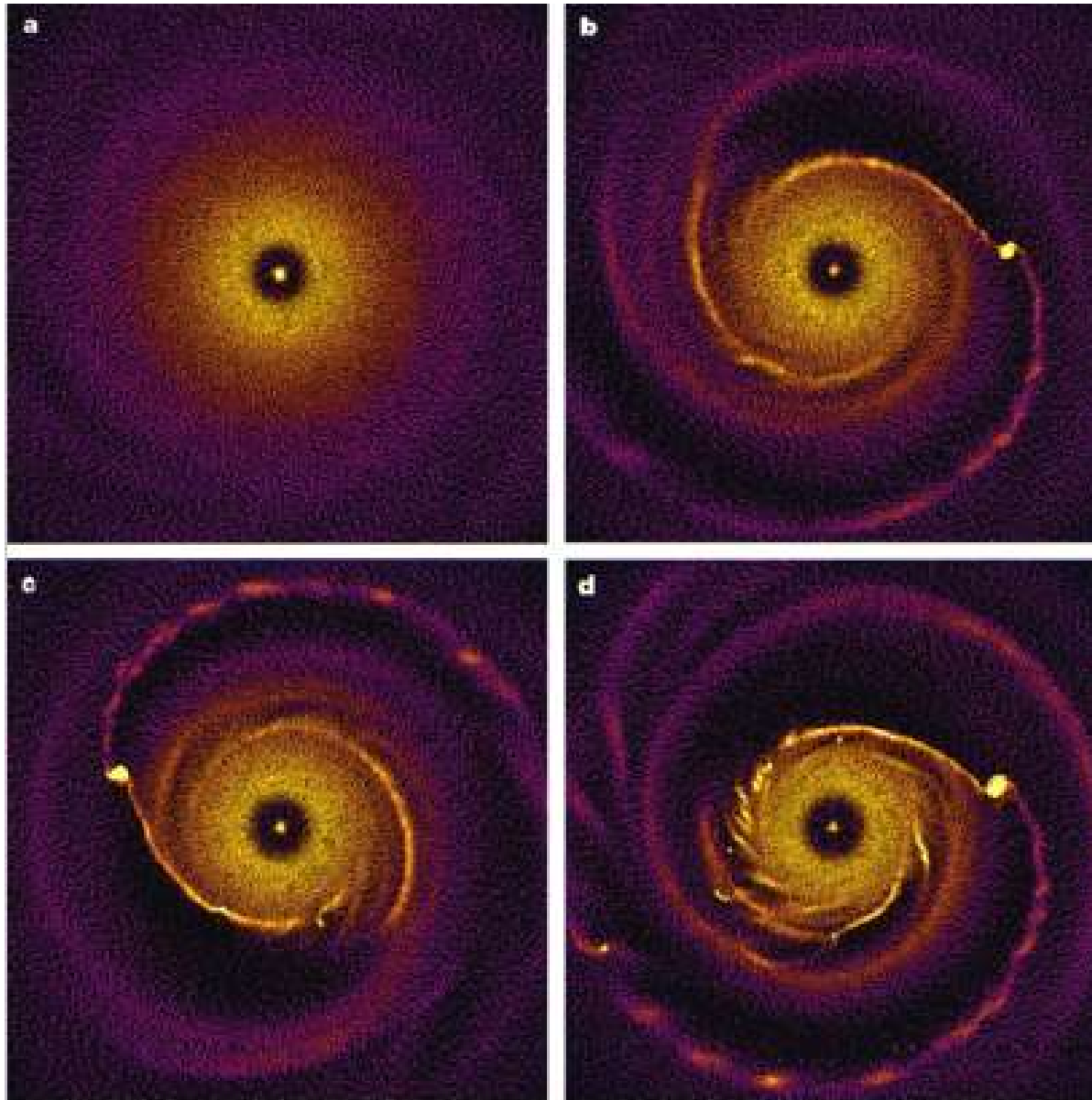


Gravitational Instability

Planet Formation



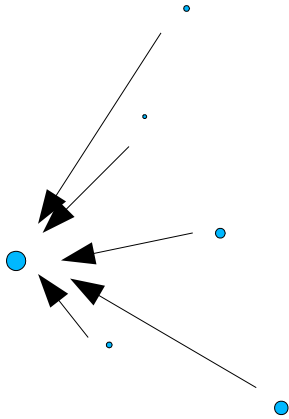
Gravitational Instability



Start with initial disturbances.

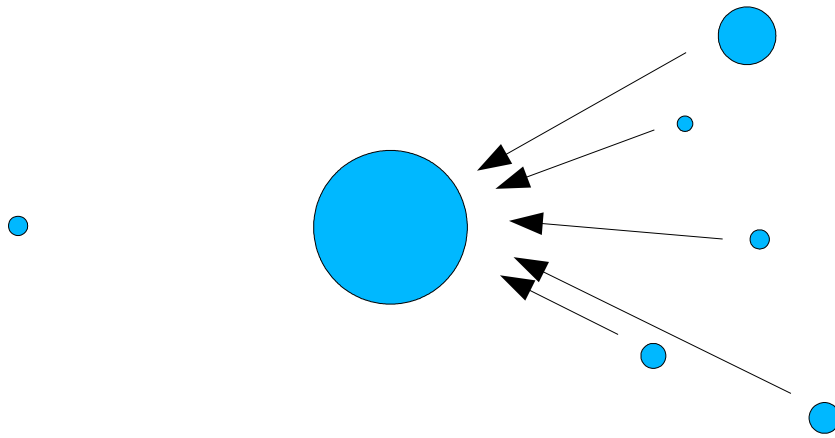
End with gas giant planets.

Core Accretion



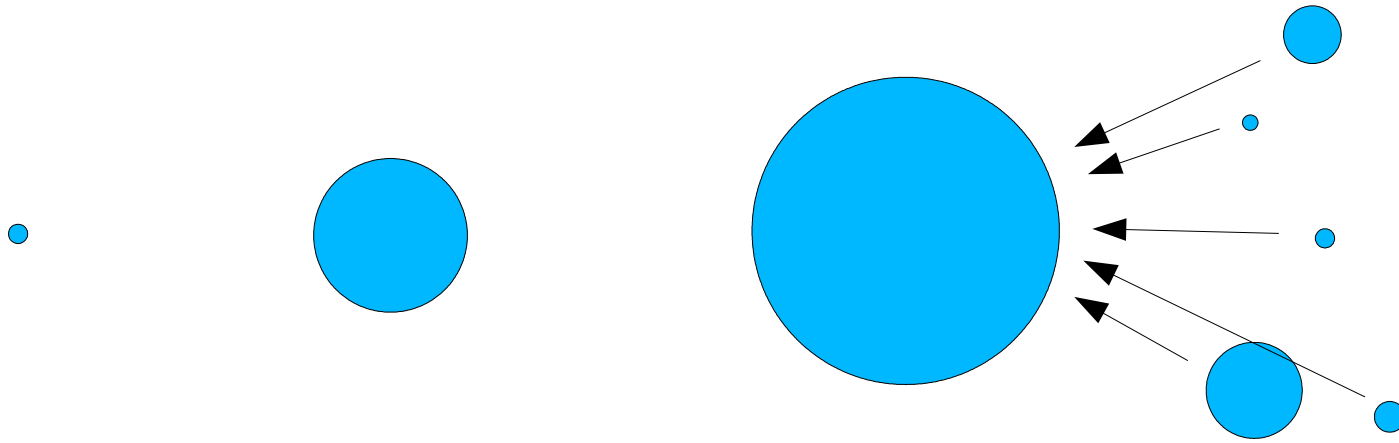
Start with small objects that accrete other small objects.

Core Accretion



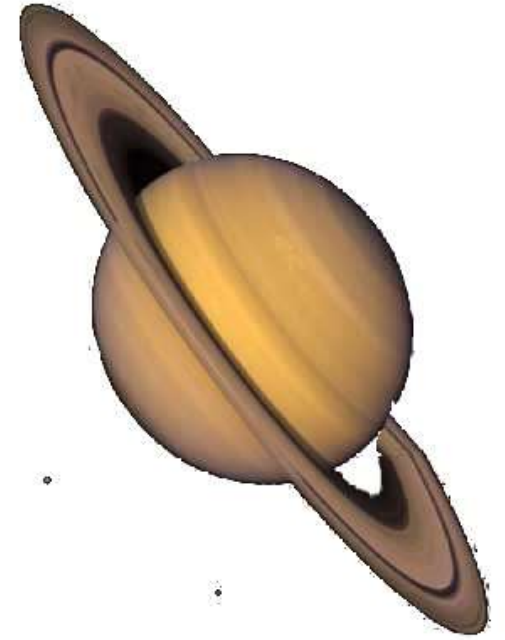
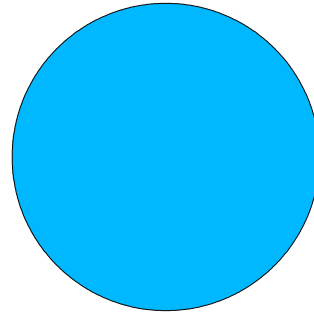
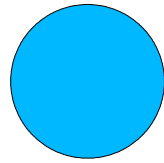
and other small objects.

Core Accretion



and other not so small objects.

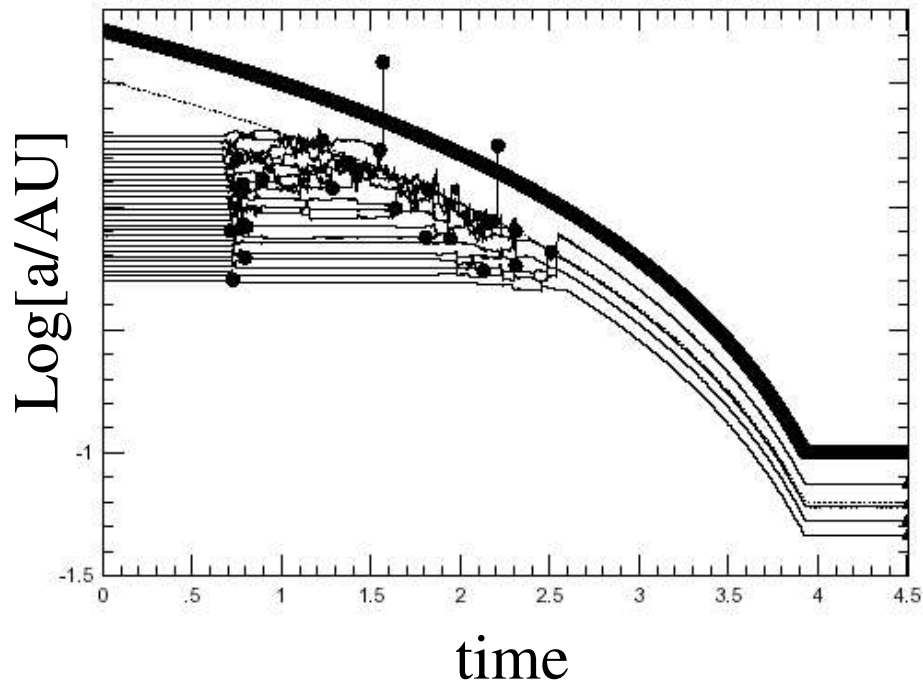
Core Accretion



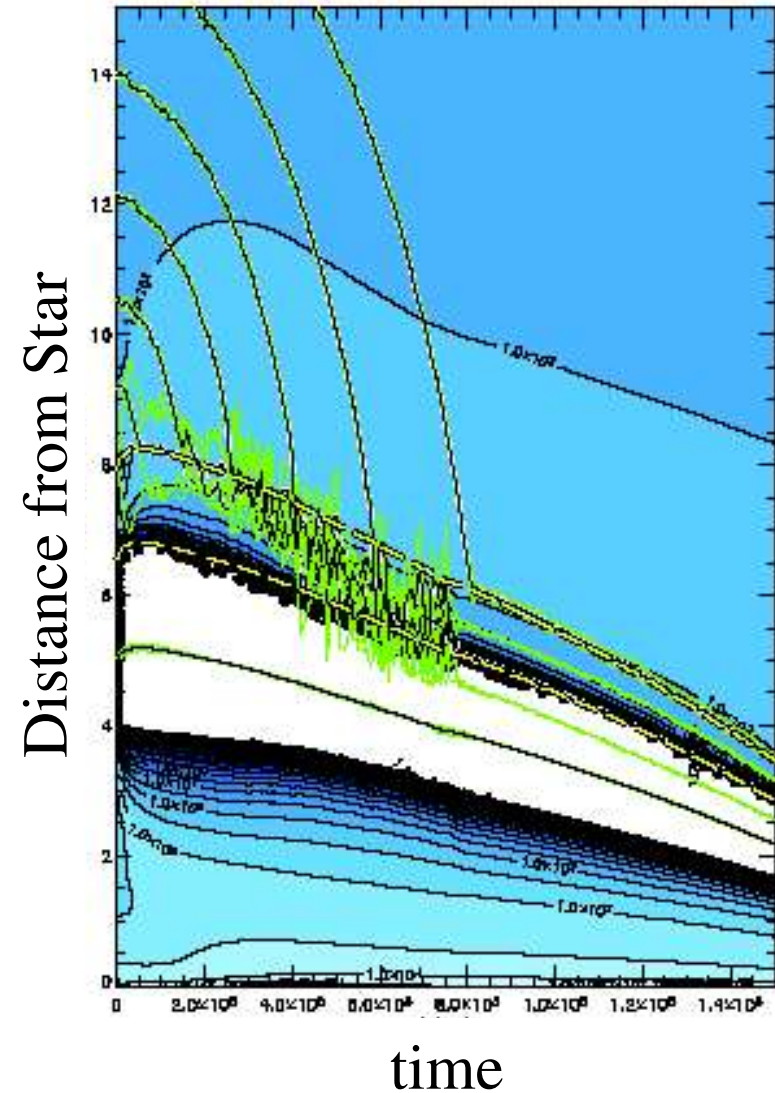
to make a planet

Tell Tale Sign

Core accretion predicts
small, resonant planets.

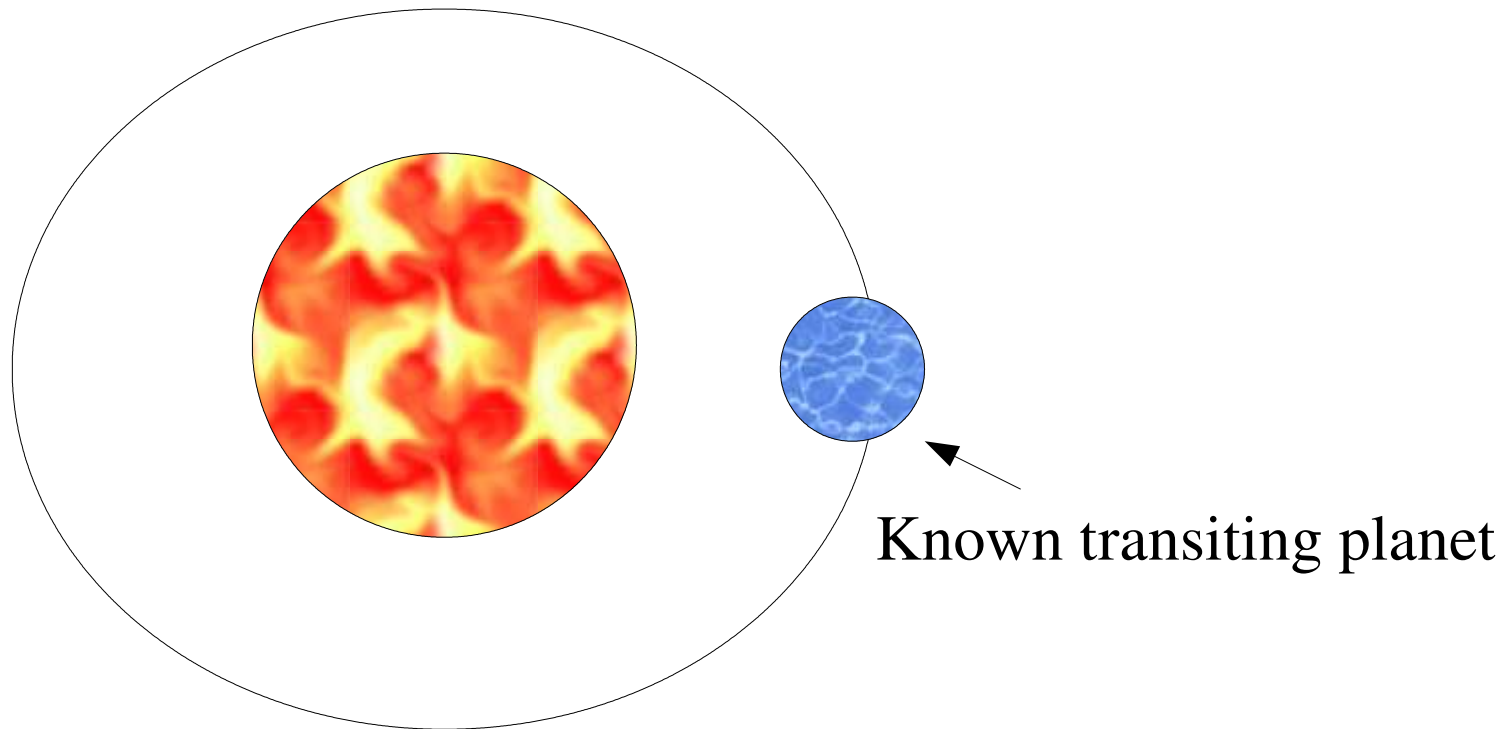


Zhou et al 2005



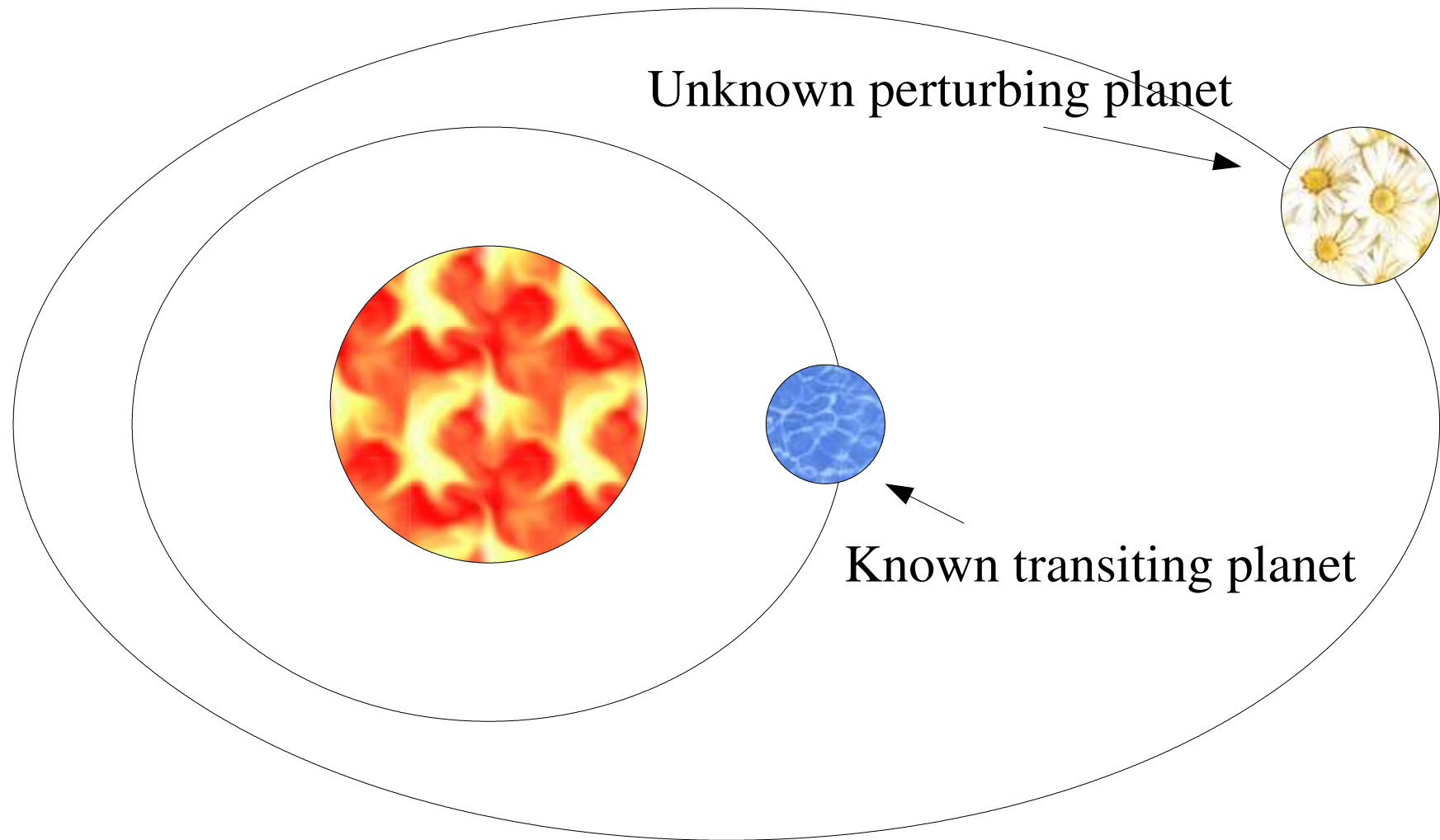
Thommes 2005

Transit Timing Variations



Transit times are equally spaced.

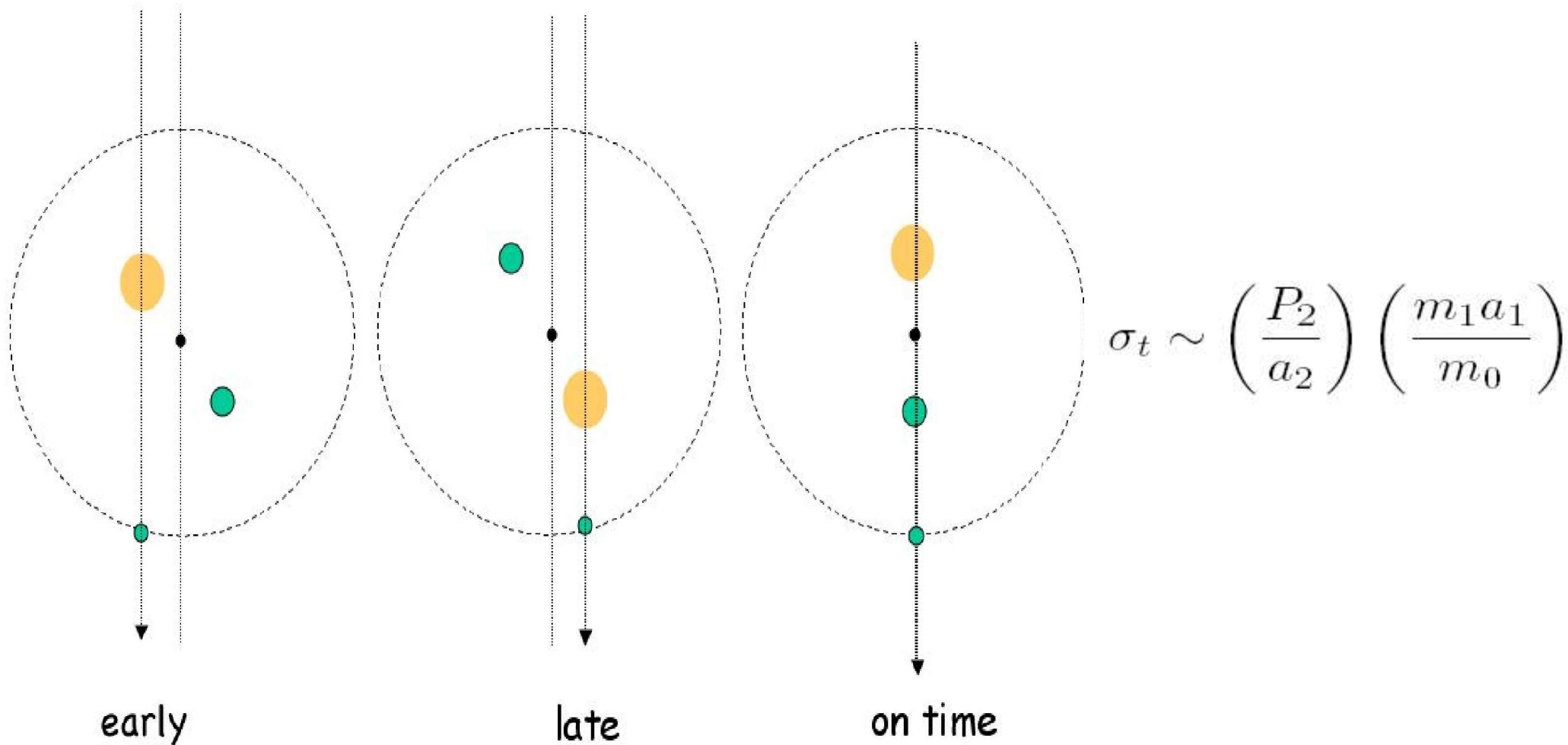
Transit Timing Variations



Transit times are NOT equally spaced.

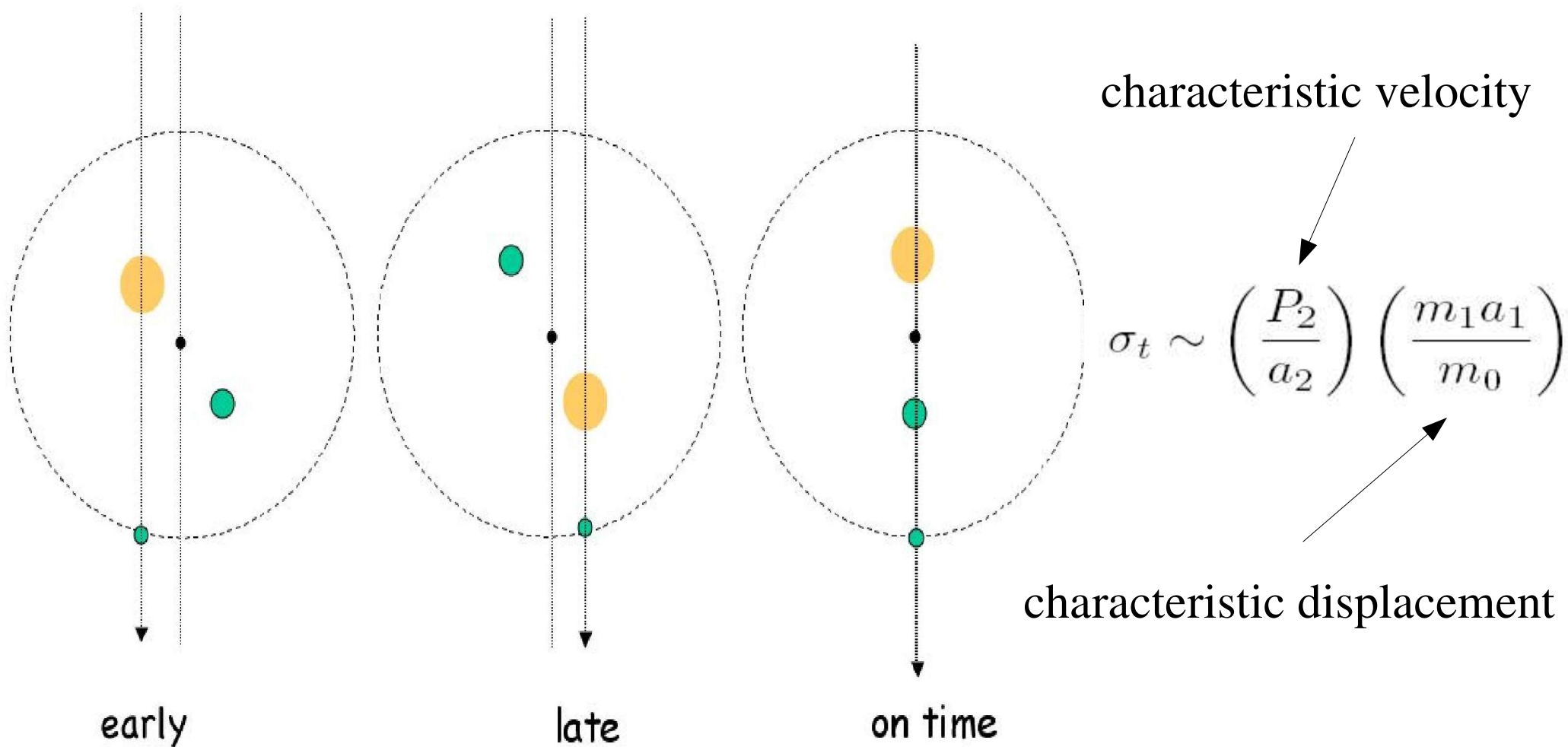
Transit Timing Variations

The TTV Poster Child



Transit Timing Variations

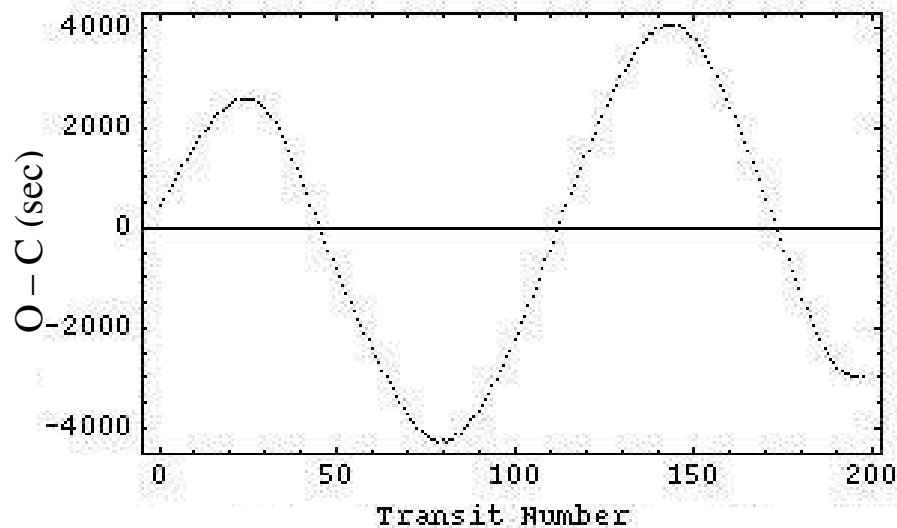
The TTV Poster Child



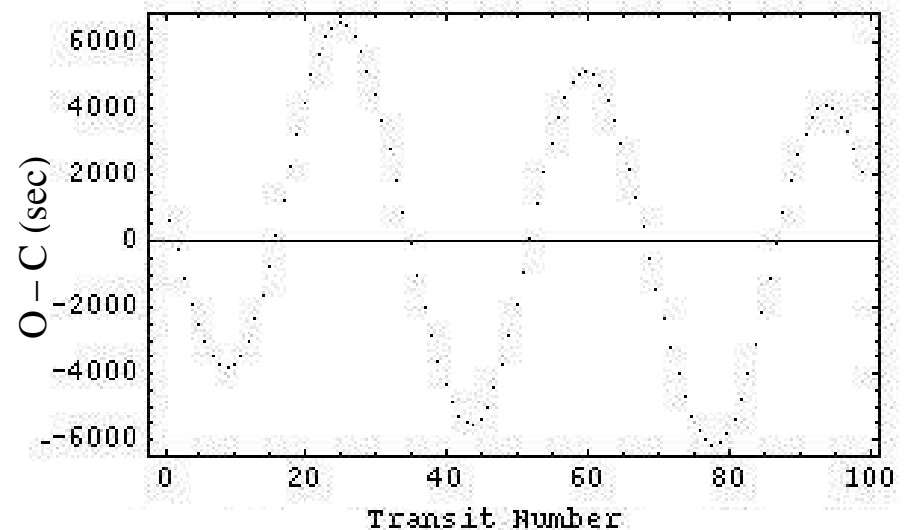
Transit Timing Variations

Sample signal for a resonant, 0.1 Jupiter-mass planet perturbing a Jupiter-mass planet that is on a 3-day orbit.

2:1 – outer resonance



2:1 – inner resonance

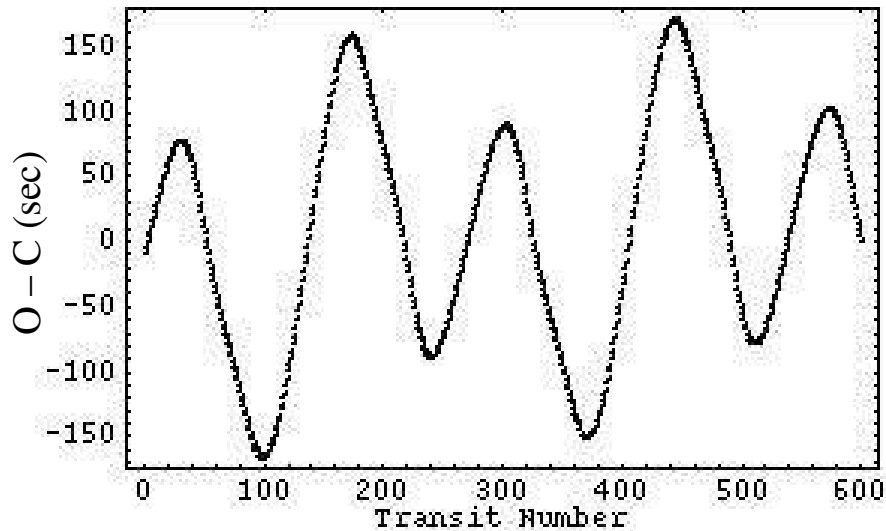


$$\delta t_{max} \sim \frac{P}{4.5j} \frac{m_{pert}}{m_{pert} + m_{trans}}$$

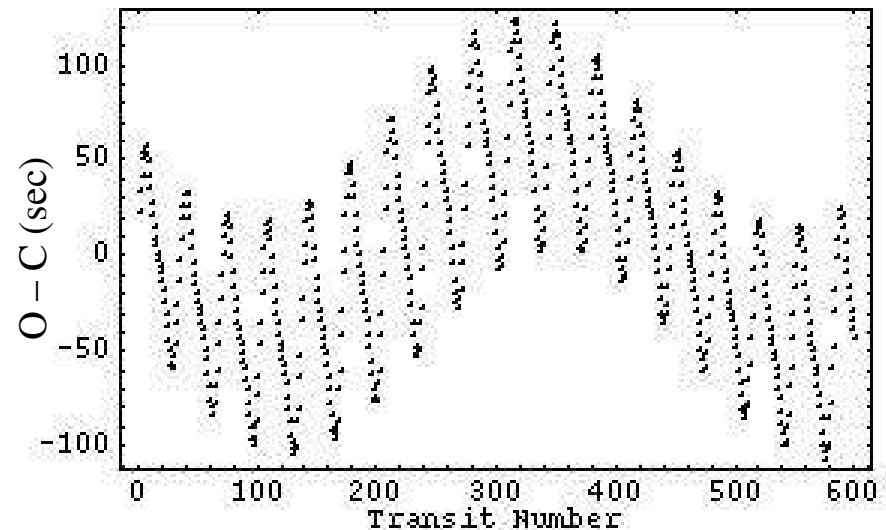
Transit Timing Variations

Sample signal for a resonant, Earth-mass planet perturbing a Jupiter-mass planet that is on a 3-day orbit.

2:1 – low eccentricity



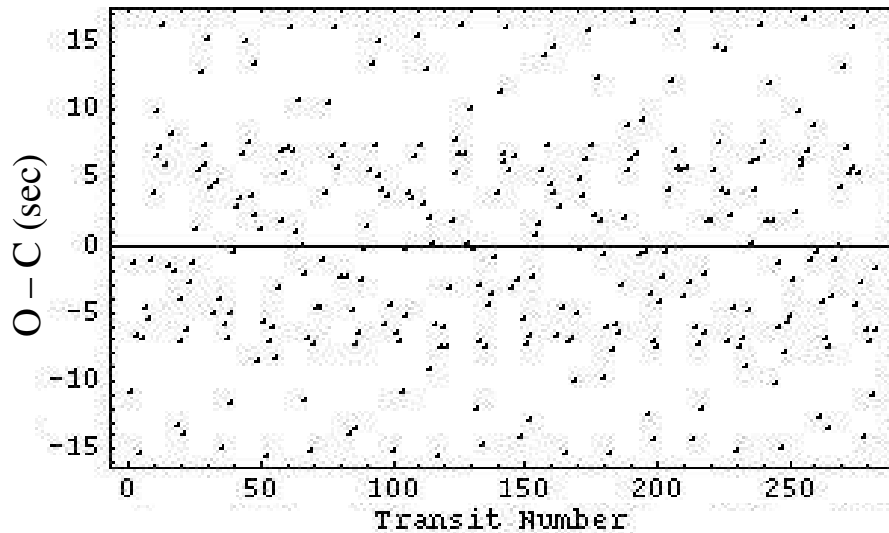
2:1 – high eccentricity



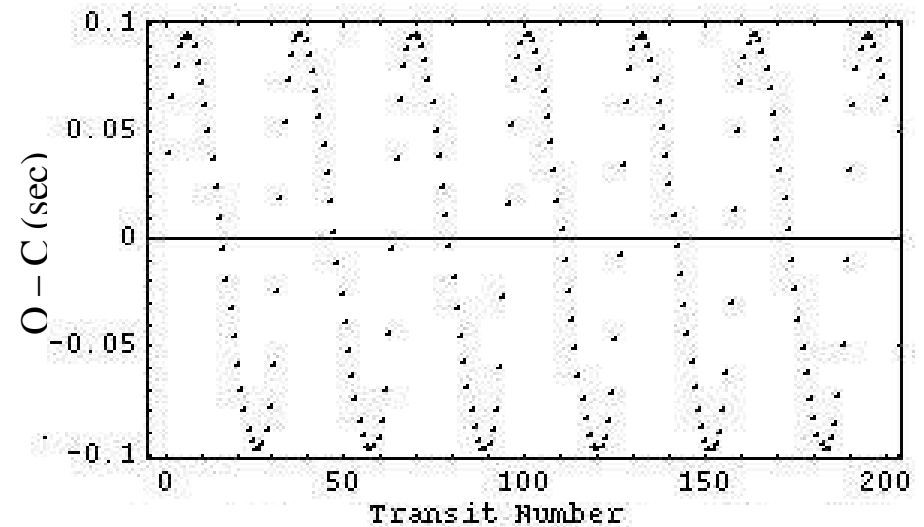
Transit Timing Variations

Sample signal for a non-resonant, 0.1 Jupiter-mass planet perturbing a Jupiter-mass planet that is on a 3-day orbit.

2:1 – semi-major axis ratio



10:1 axis ratio, high eccentricity

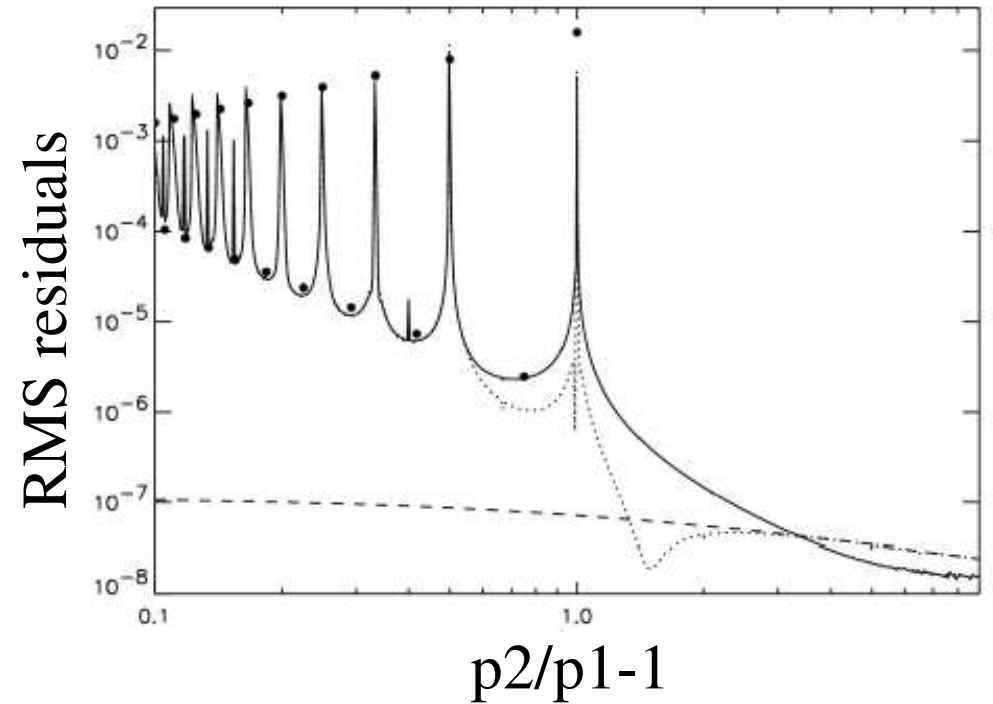
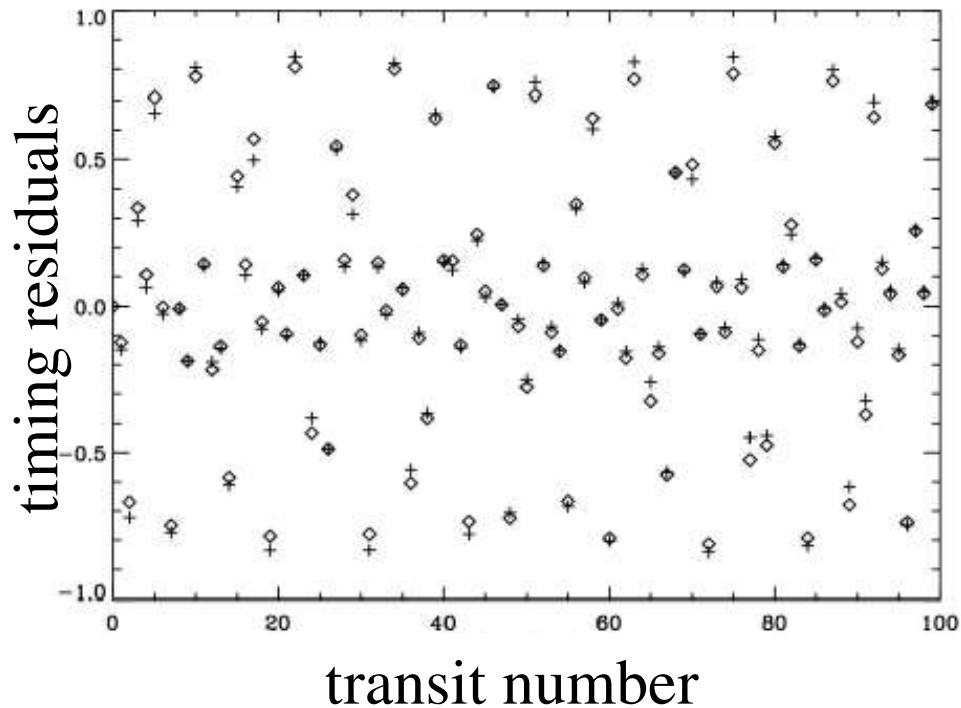


$$\sigma_t \sim (\text{Big, Messy Expression})$$

$$\sigma_1 \sim e_2 P_2 \left(\frac{m_2}{m_0} \right) \left(\frac{a_1}{a_2} \right)^3$$

Transit Timing Variations

Comparison of Analytic and Numerical Results



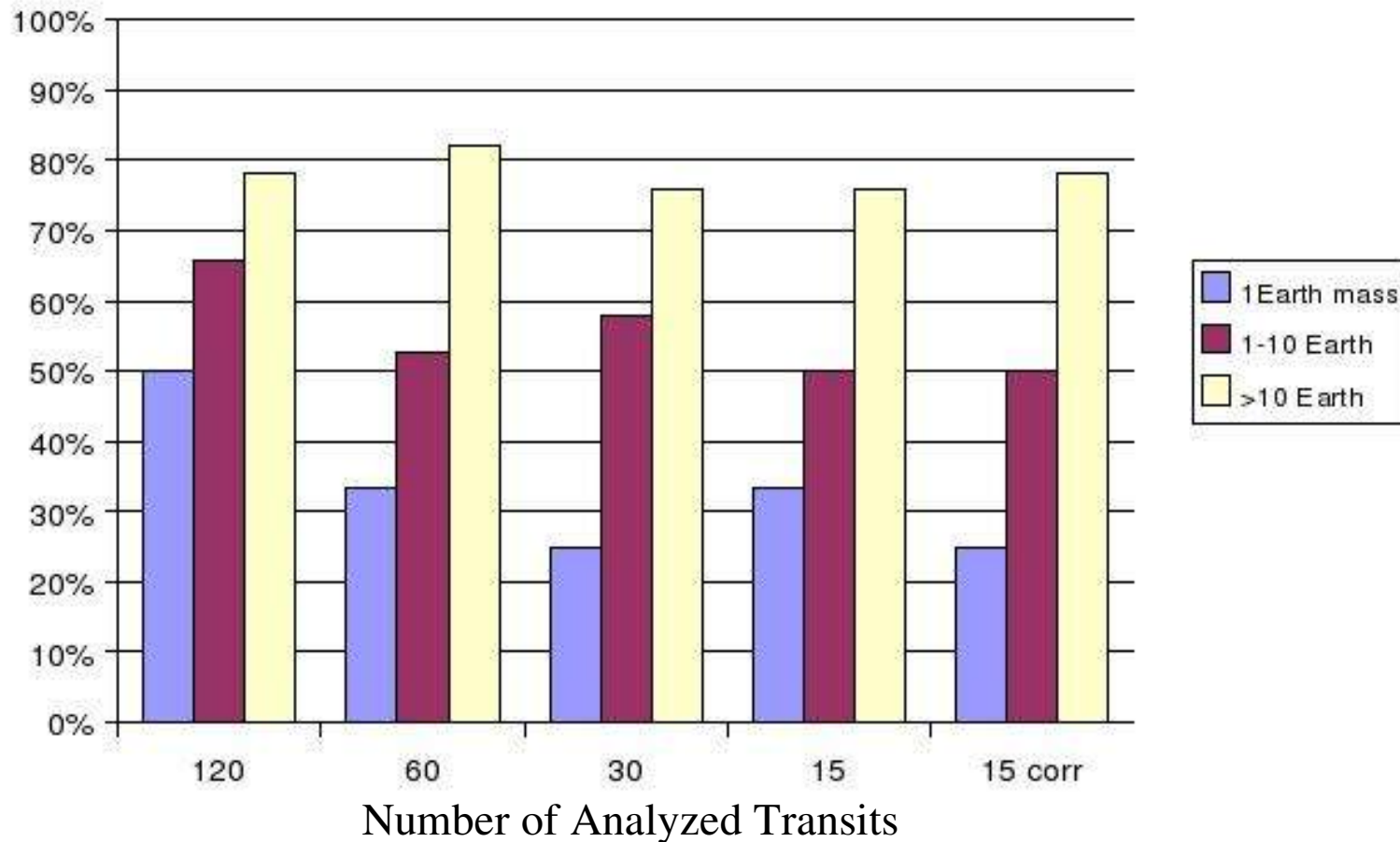
Signal increases with period of transiting planet, mass of perturber, and, particularly, proximity to mean-motion resonance.

Finding Simulated Planets

- 100 random systems
 - Transiting Jupiter on a 3-day orbit
 - Perturbing planet with mass between 0.3 and 300 Earth-masses
 - Eccentricities between 0.001 and 1
 - Coplanar orbits of random orientation
- All systems near the 2:1 exterior resonance
- Data spans 120 orbits – broken into 4 subsets of 120, 60, 30, and 15 random transits, and one of 15 correlated transits.
- White, Gaussian timing noise added equal to 5 seconds per day of the transiting planet period

Finding Simulated Planets

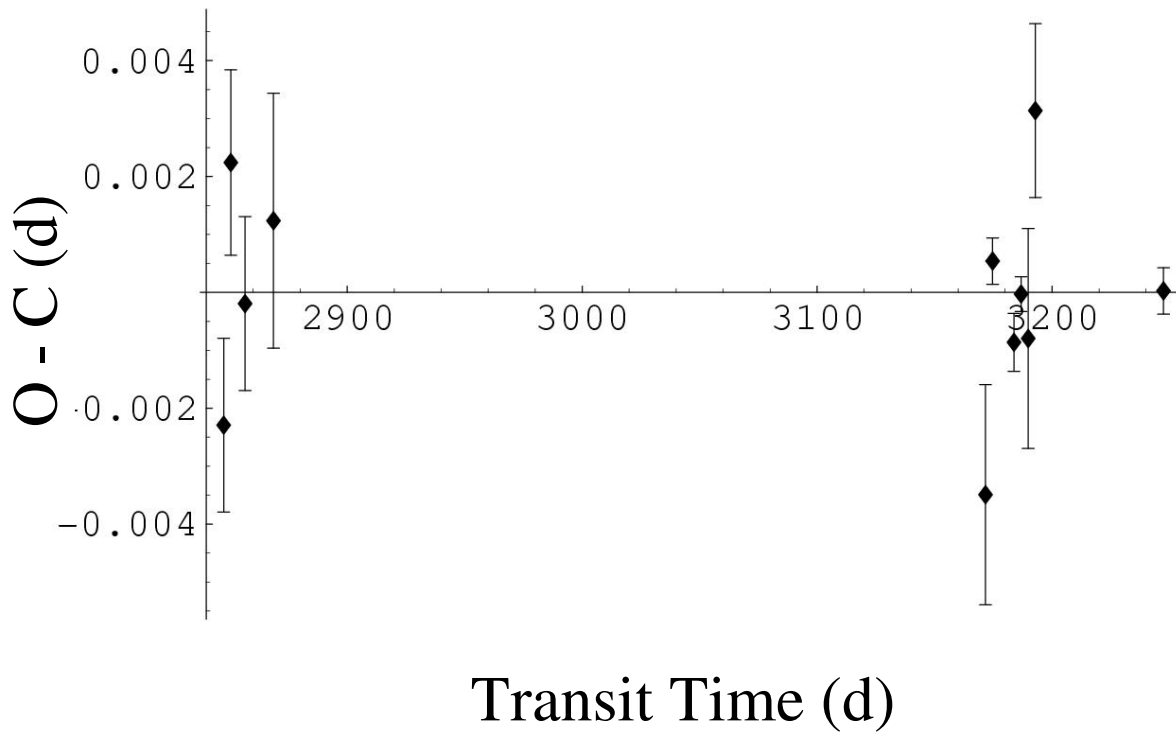
Correct Identifications in 2:1 Exterior Resonance



These results are for a coarse search with a no frills minimization algorithm.

Analyzing Real Data, Part 1

11 ground-based transits of the TrES-1 system

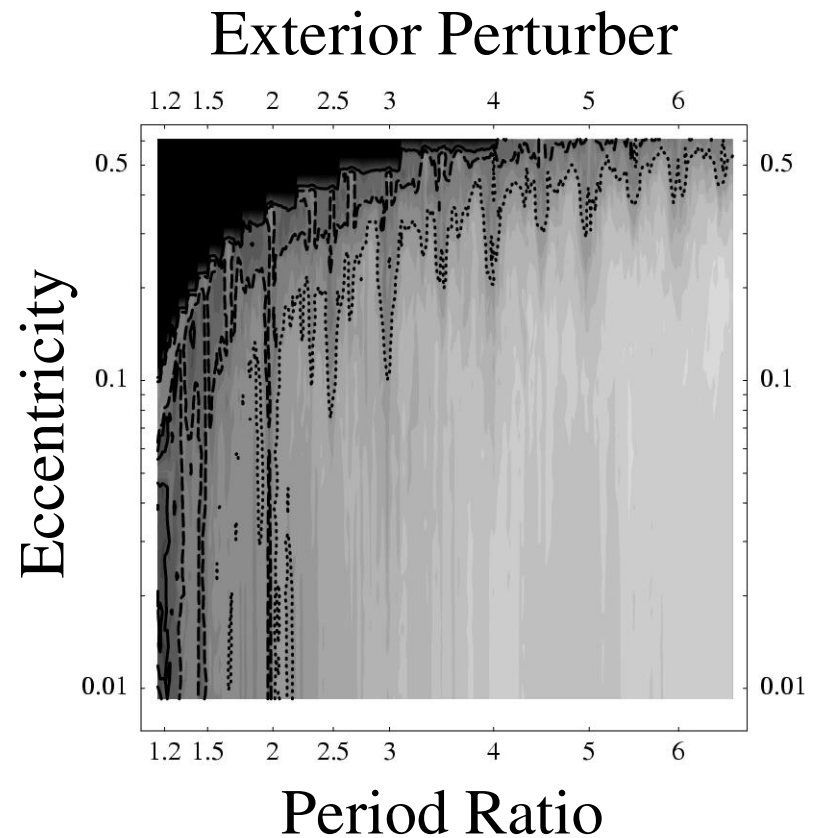
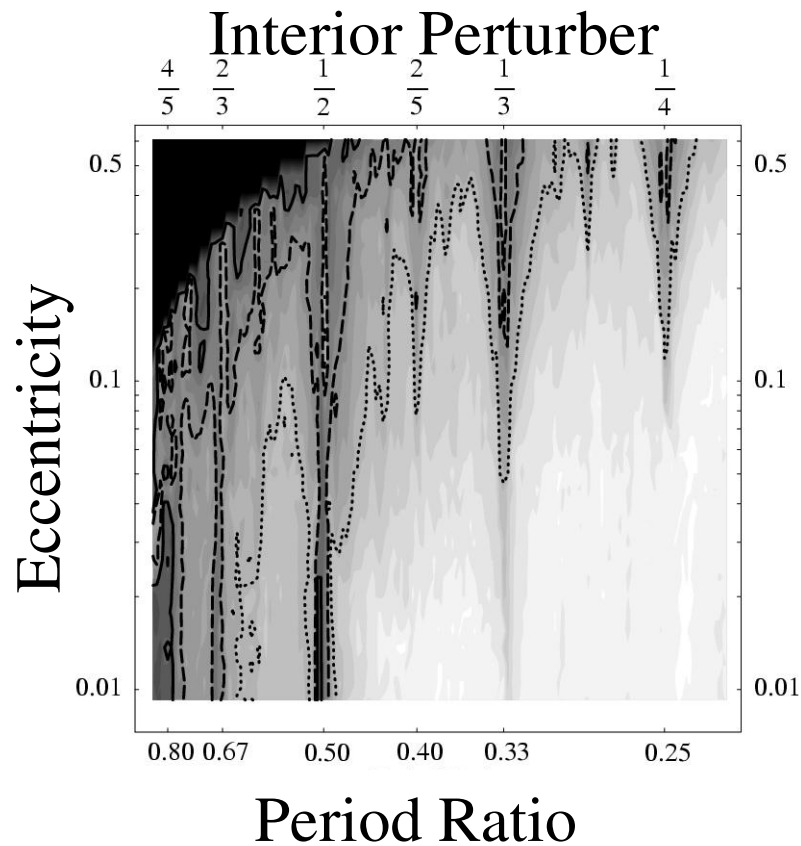


reduced $\chi^2 = 1.93$
mean $\sigma = 107.6\text{s}$
minimum $\sigma = 25.9\text{s}$
(1.2m Whipple)

Data from Charbonneau et al. 2005
Results from Steffen & Agol 2005

The TrES-1 System

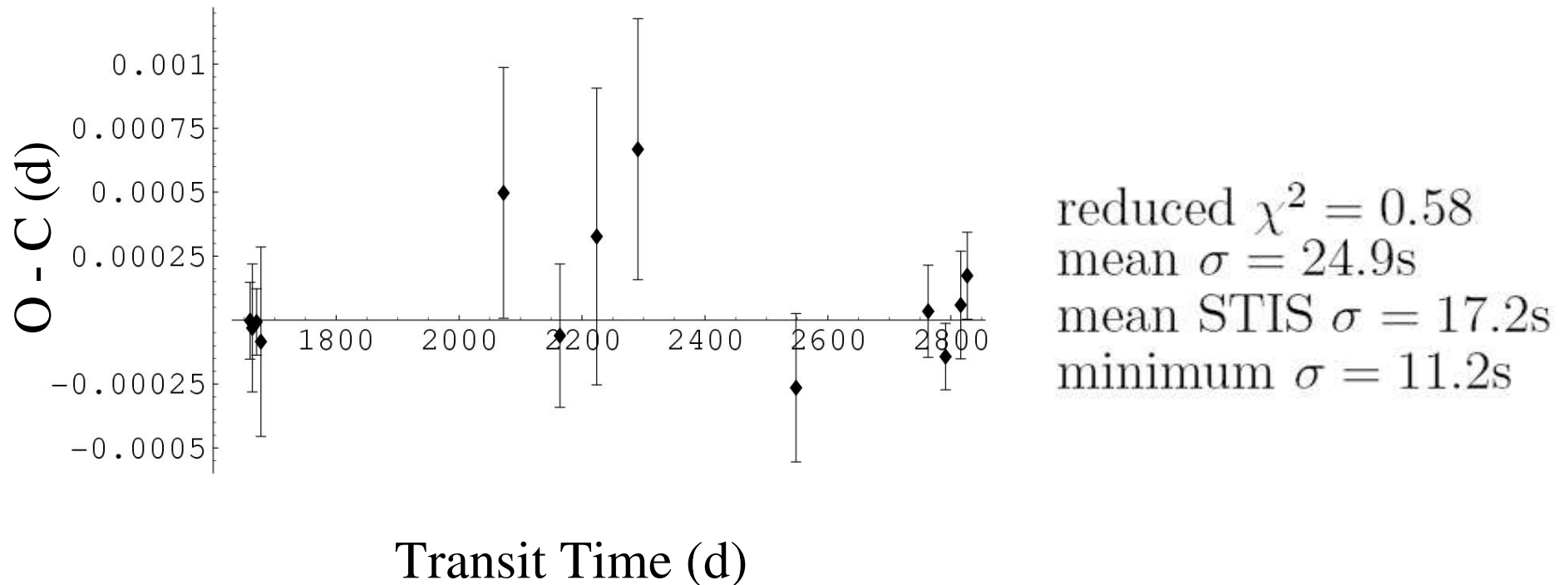
Constraints on the Mass of a Secondary Planet



Contours: 100, 10, and 1 Earth mass

Analyzing Real Data, Part 2

13 HST transits of the HD 209458 system

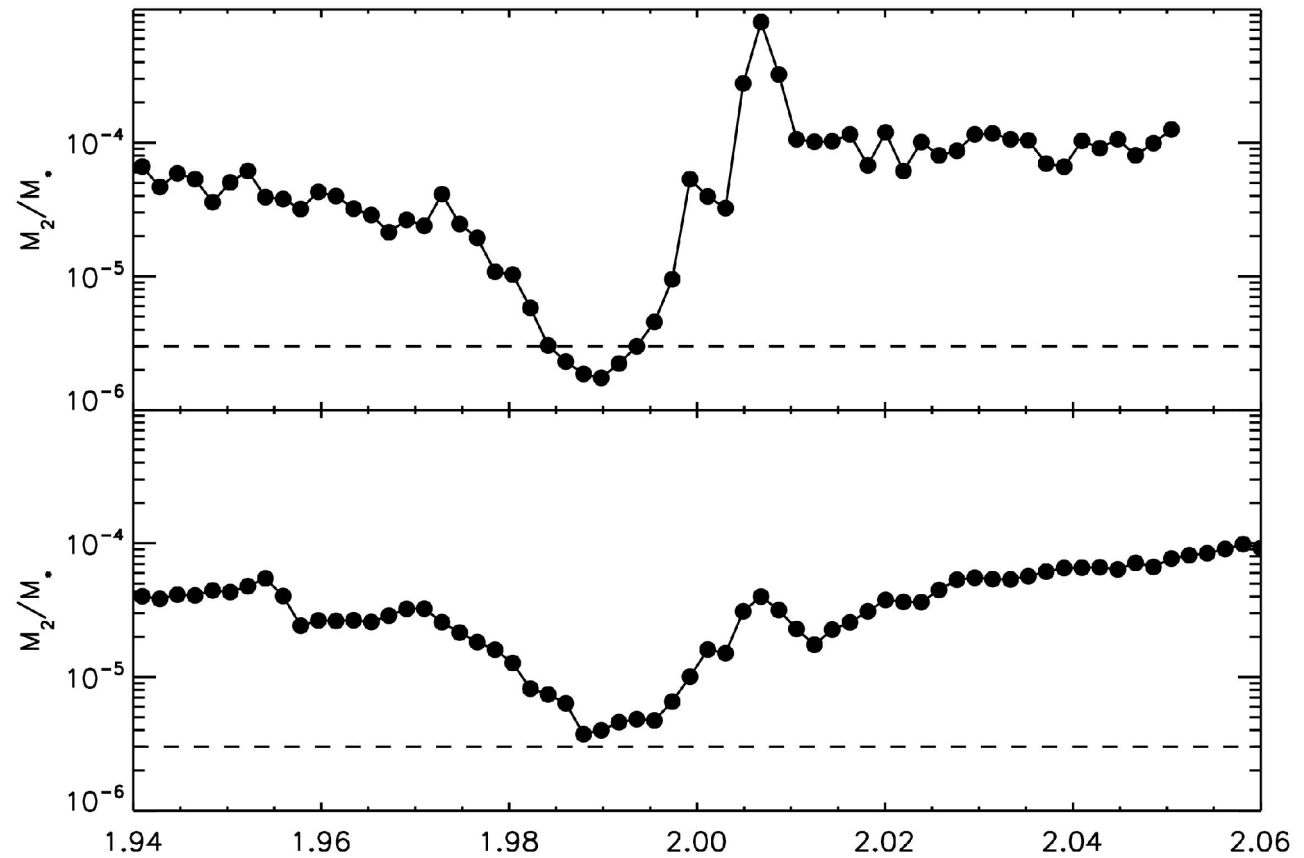


Data from Charbonneau et al. 2001, Brown et al. 2001, Schultz et al. 2004
Re-reduced and analyzed in Agol & Steffen 2007

The HD 209458 System

Maximum allowed mass of companion
in 2:1 resonance with any eccentricity

Interior Perturber

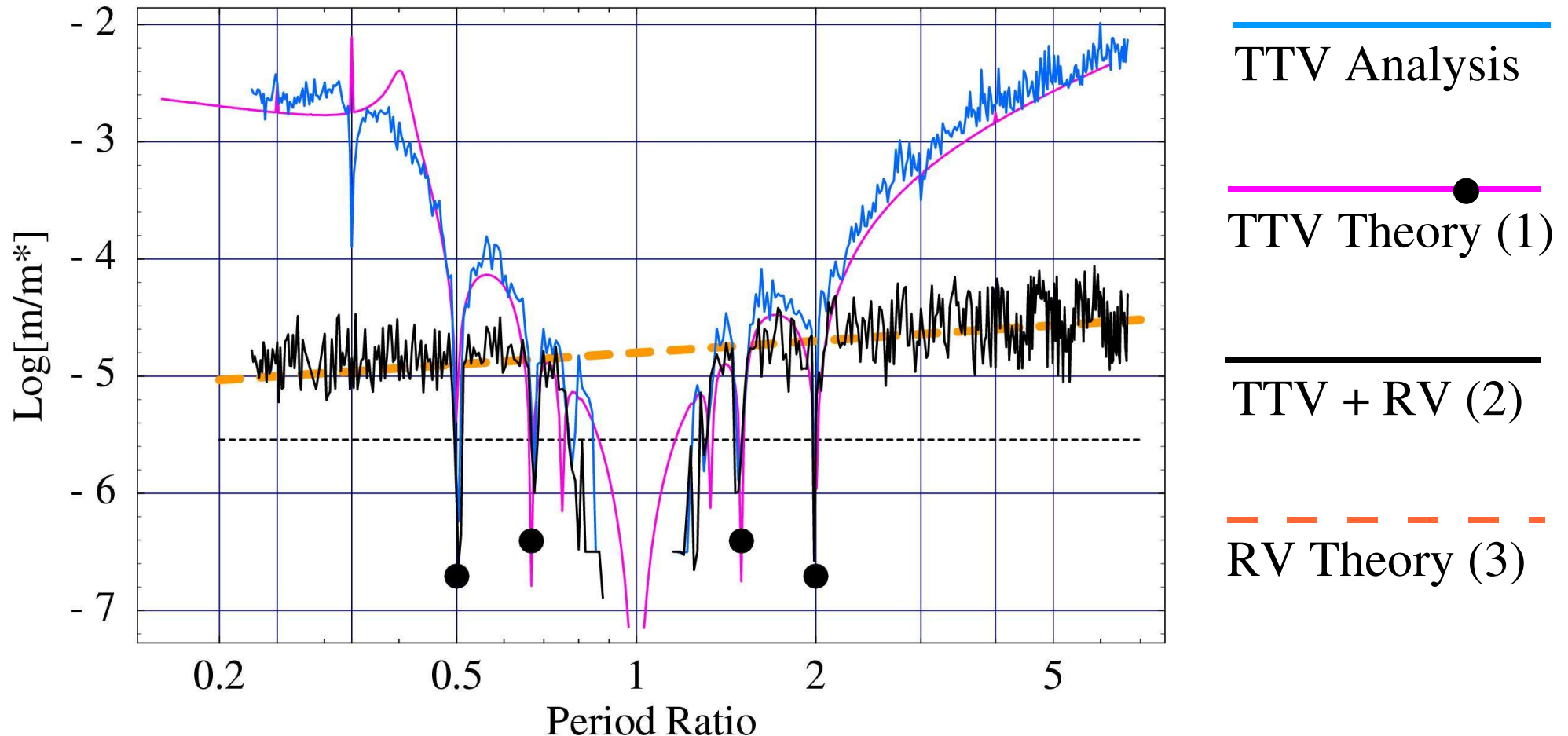


Exterior Perturber

Period Ratio

The HD 209458 System

Maximum allowed mass for companion in initially circular orbit



- (1) Eqns. (A7-8) & (33) from Agol, Steffen, Sari, & Clarkson MNRAS 359, 567 (2005)
- (2) RV measurements from Laughlin et al. ApJ 629, L121 (2005)
- (3) Eqn. (2) from Steffen & Agol MNRAS 364, L96 (2005)

The Future of TTV

PASS, WASP0, ASAS-3, RAPTOR, TrES,
XO, HATnet, SWASP, Vulcan, RAPTOR-F,
BEST, Vulcan-S, SSO/APT, RATS, TeMPEST,
EXPLORE-OC, PISCES, ASP, OGLE-III,
STEPSS, INT, ONC, EXPLORE-N, EXPLORE-S,
KELT, ASEPS, Pan-Planets, MOST

The Future of TTV

PASS, WASP0, ASAS-3, RAPTOR, TrES,
XO, HATnet, SWASP, Vulcan, RAPTOR-F,
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STEPSS, INT, ONC, EXPLORE-N, EXPLORE-S,
KELT, ASEPS, Pan-Planets, MOST

and

CoRoT and Kepler

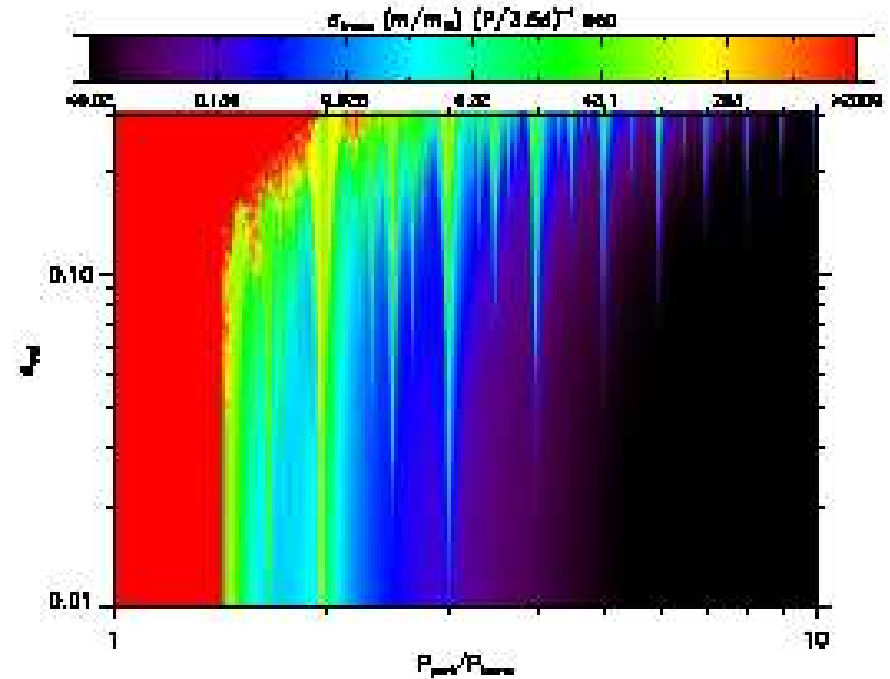
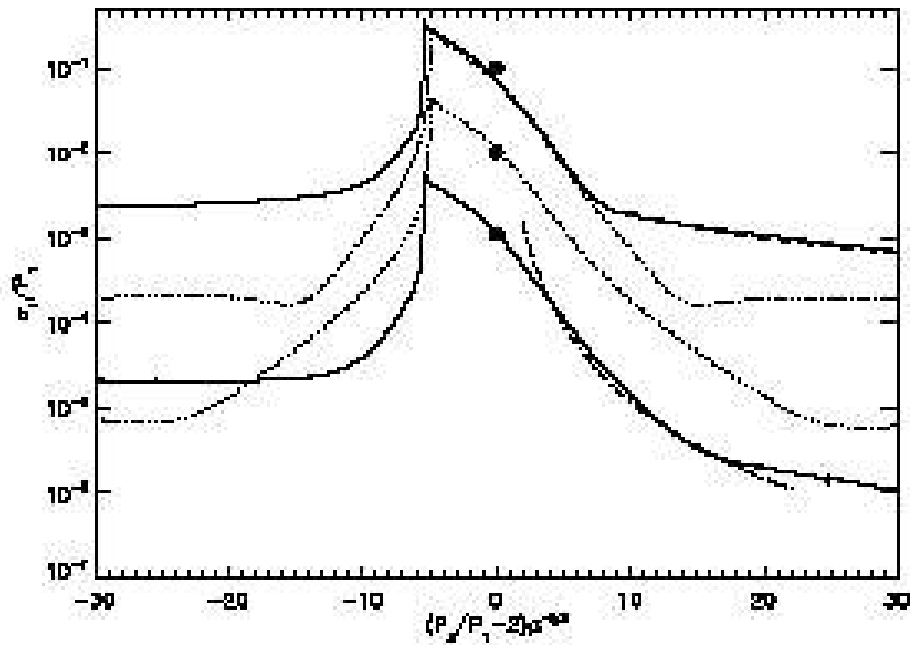
Science from TTV

- 1) Detect additional planets in transiting systems and determine the masses and radii of all bodies in them.
- 2) Determine the relative importance of Gravitational Instability and Core Accretion models of planet formation.
- 3) Constrain planetesimal masses and parameters of protoplanetary disk
- 4) Study the evolution of planetary systems, e.g. the effects of planet-planet scattering on eccentricity and inclination.
- 5) Interesting dynamical scenarios with strongly interacting systems.

Conclusions

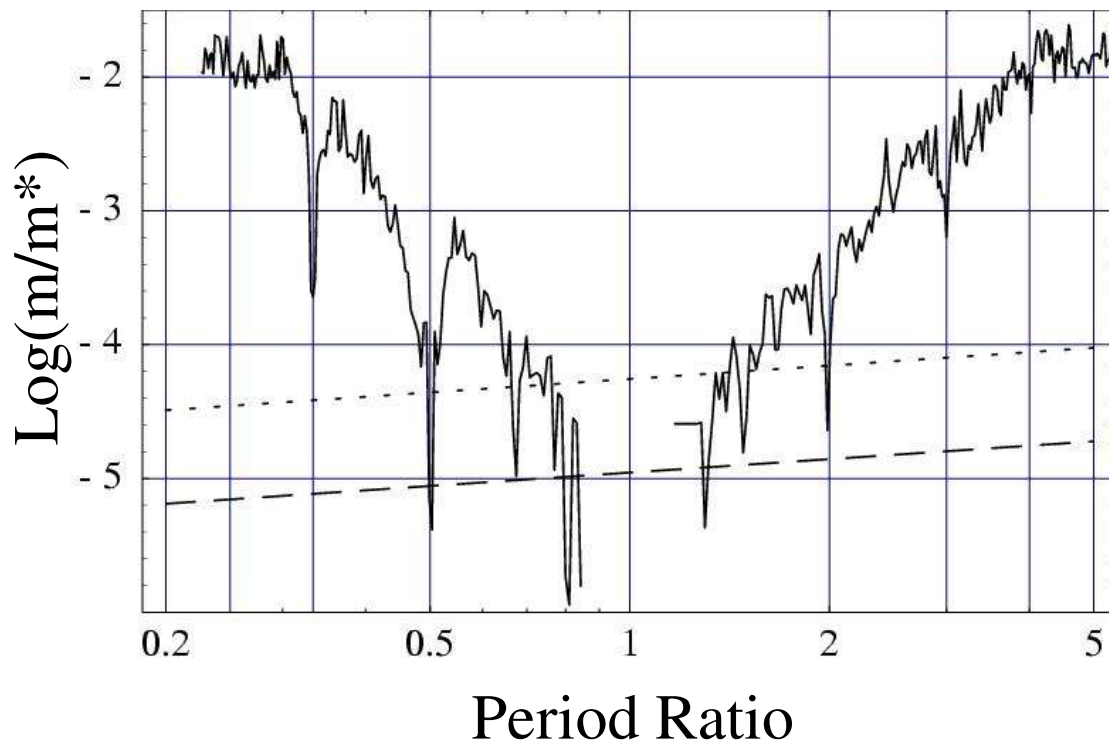
- 1) No low-order resonant ~Earth-mass planets in HD 209458 or TrES-1
 - Sensitivity to 0.2 Earth-masses in low-eccentricity orbits for HD 209458 and 0.7 Earth-masses in TrES-1
 - No comment on planet formation at this time.
- 2) Most resonant systems are detectable with TTV
 - at least 2/3 of systems identified with as few as 15 transits
- 3) Many transit surveys are running and planned.
 - precursor science for larger missions (e.g. TPF)
 - additional science for each new system
- 4) TTV's sensitivity to resonant planets can test planet formation theories

Bonus Feature: More on the Signal



Bonus Feature: TrES-1

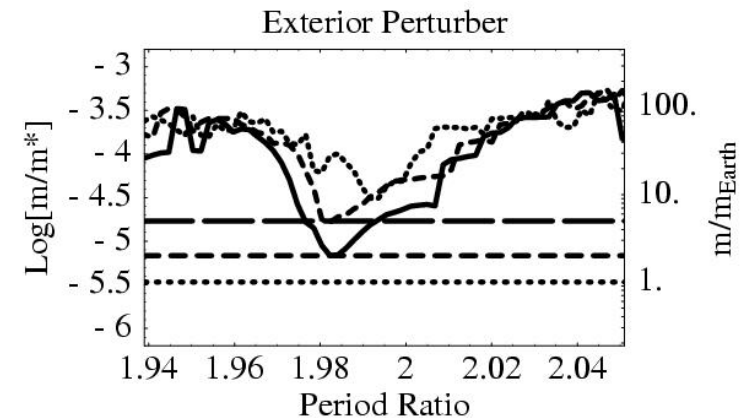
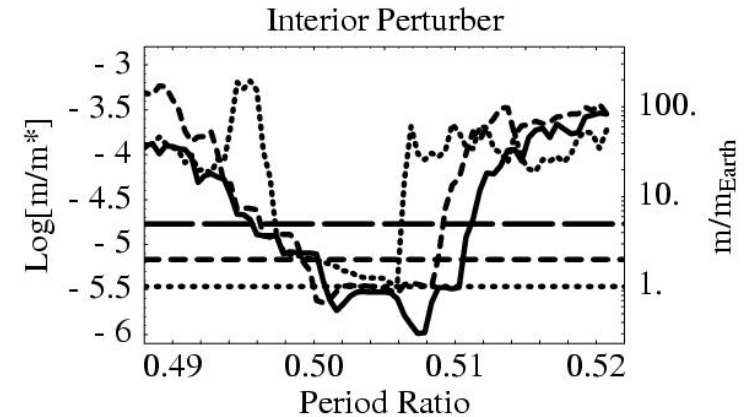
Maximum Mass of Secondary Planet



Dotted: 5 m/s RV limit

Dashed: 1 m/s RV limit

Eccentricity: 0.05



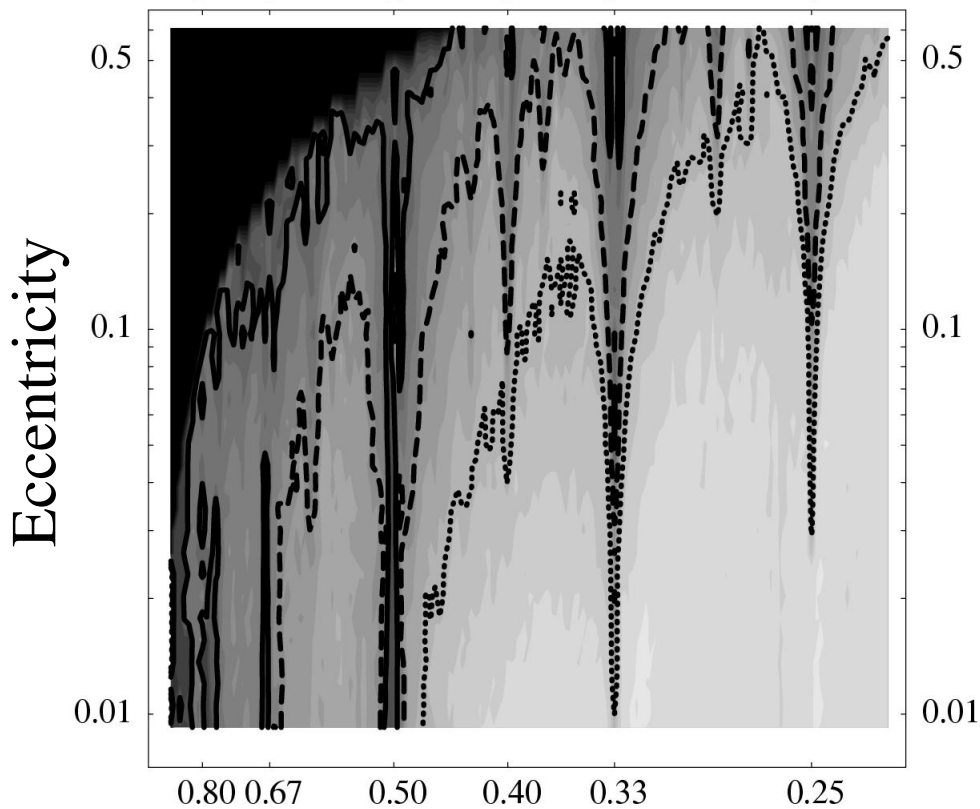
Horizontal Lines: 1, 2, 5 Earth mass

Bonus Feature: HD 209458

Maximum allowed mass of companion for HD 209458

Interior Perturber

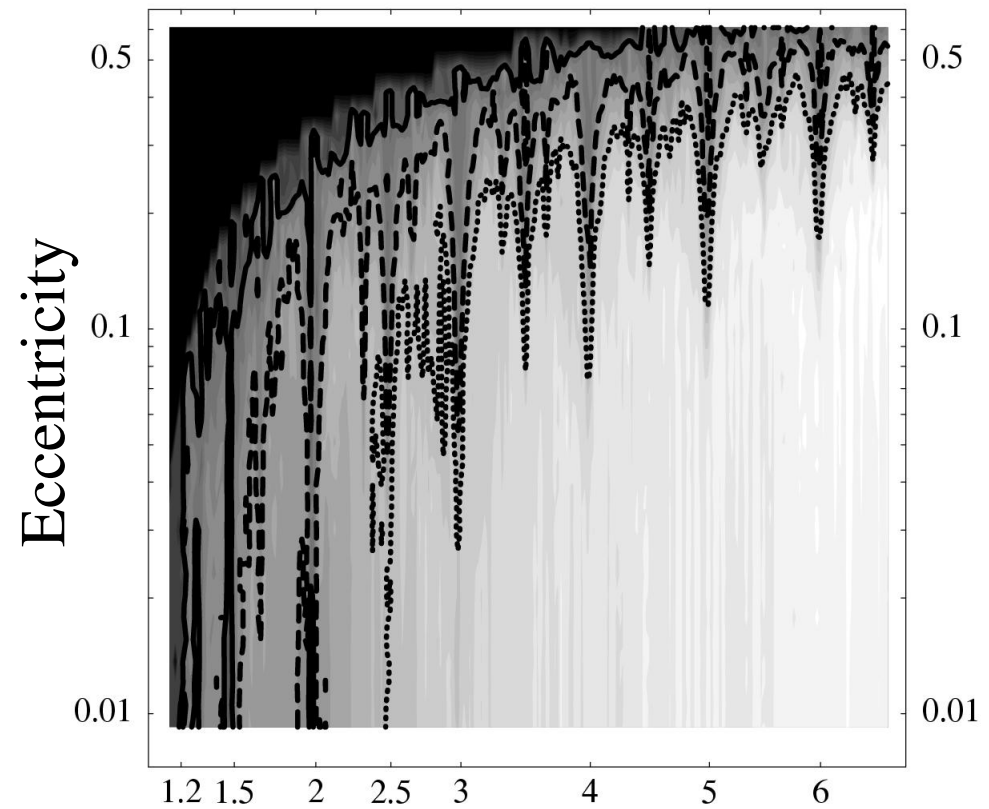
$\frac{4}{5}$ $\frac{2}{3}$ $\frac{1}{2}$ $\frac{2}{5}$ $\frac{1}{3}$ $\frac{1}{4}$



Period Ratio

Exterior Perturber

1.2 1.5 2 2.5 3 4 5 6

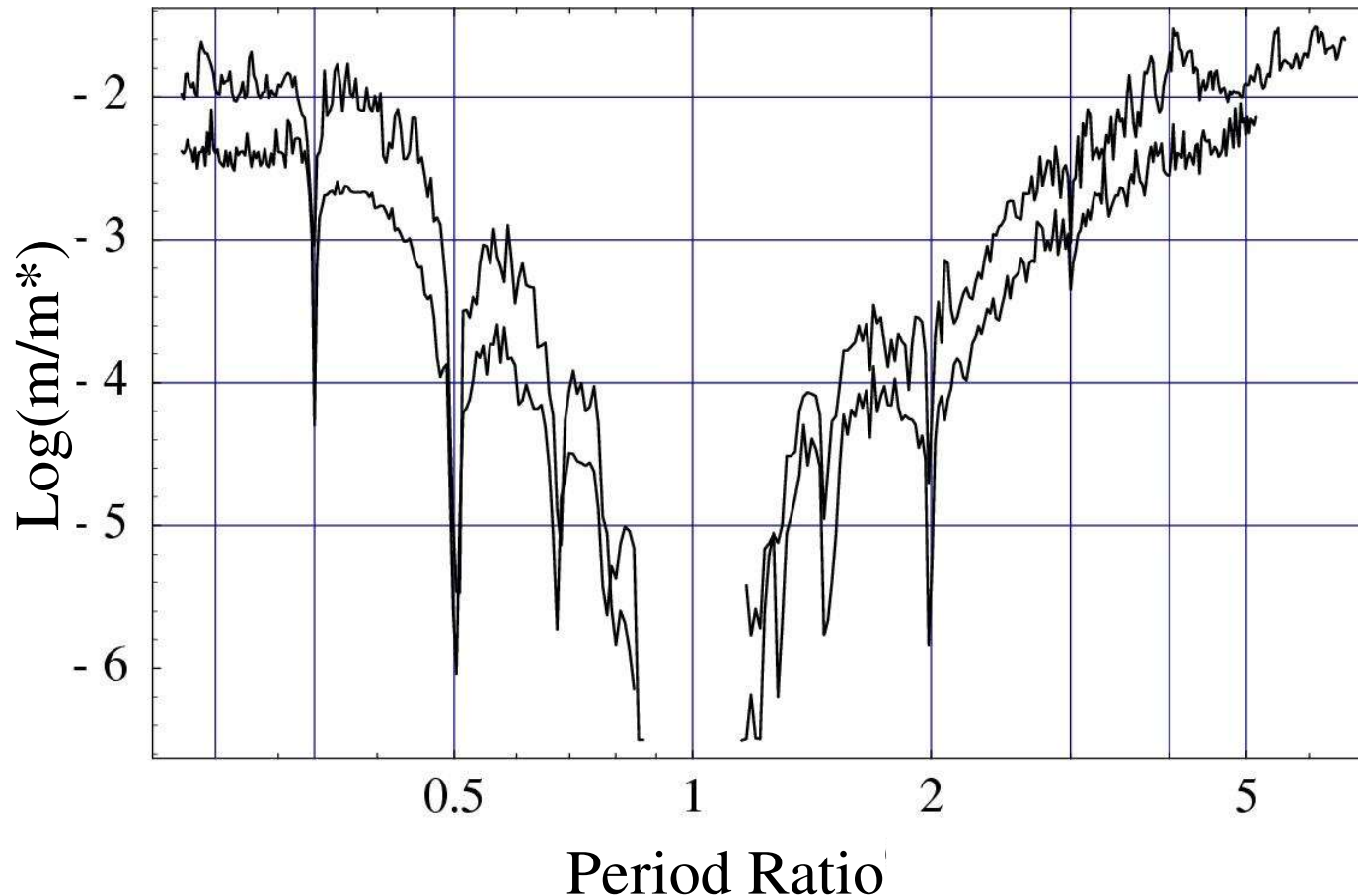


Period Ratio

Contours: 100, 10, and 1 Earth mass

Bonus Feature: Ground vs. Space

Maximum Mass of Secondary Planet ($e_2 = 0.02$)



Upper curve:

TrES-1

11 transits

108s mean timing error

26s smallest error

Lower curve:

HD209458

13 transits

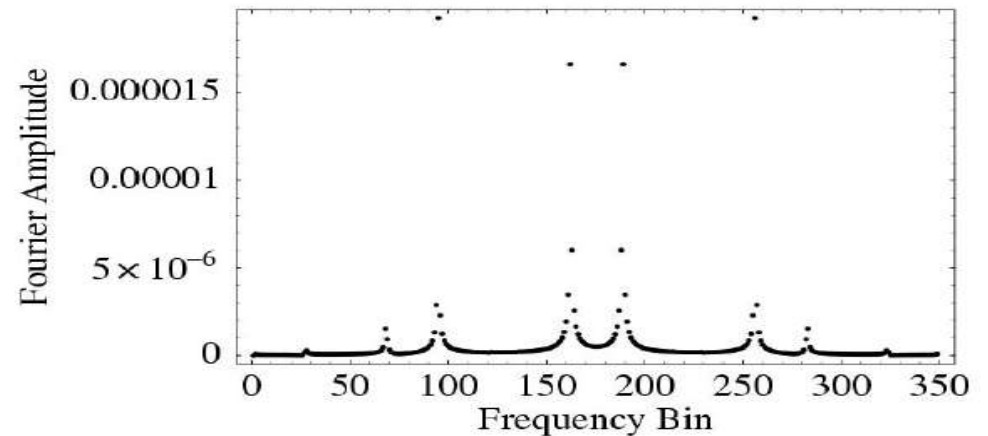
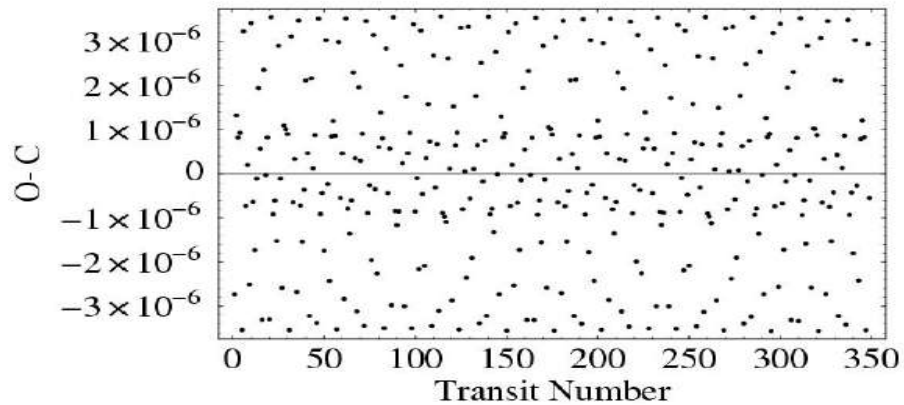
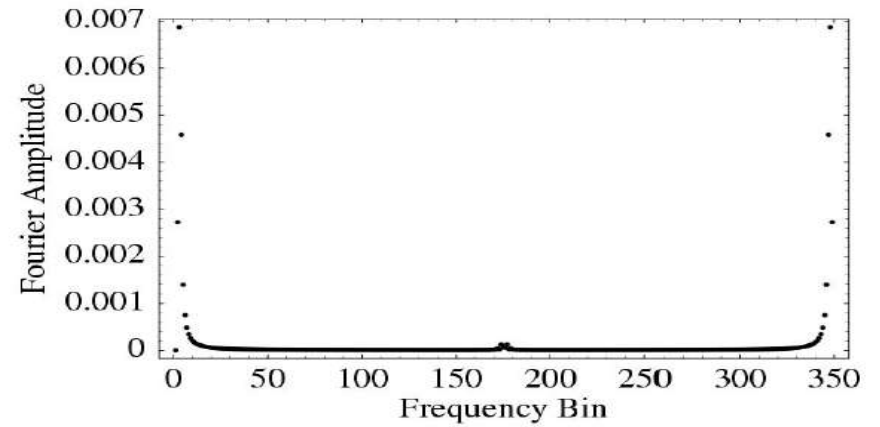
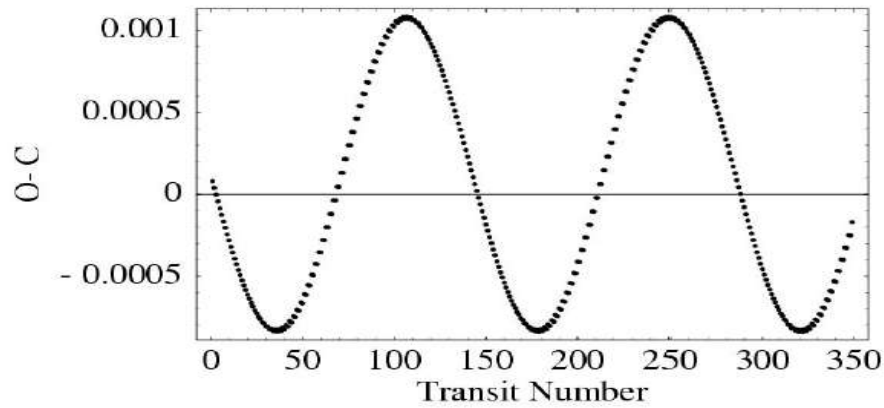
25s mean timing error

17s STIS mean error

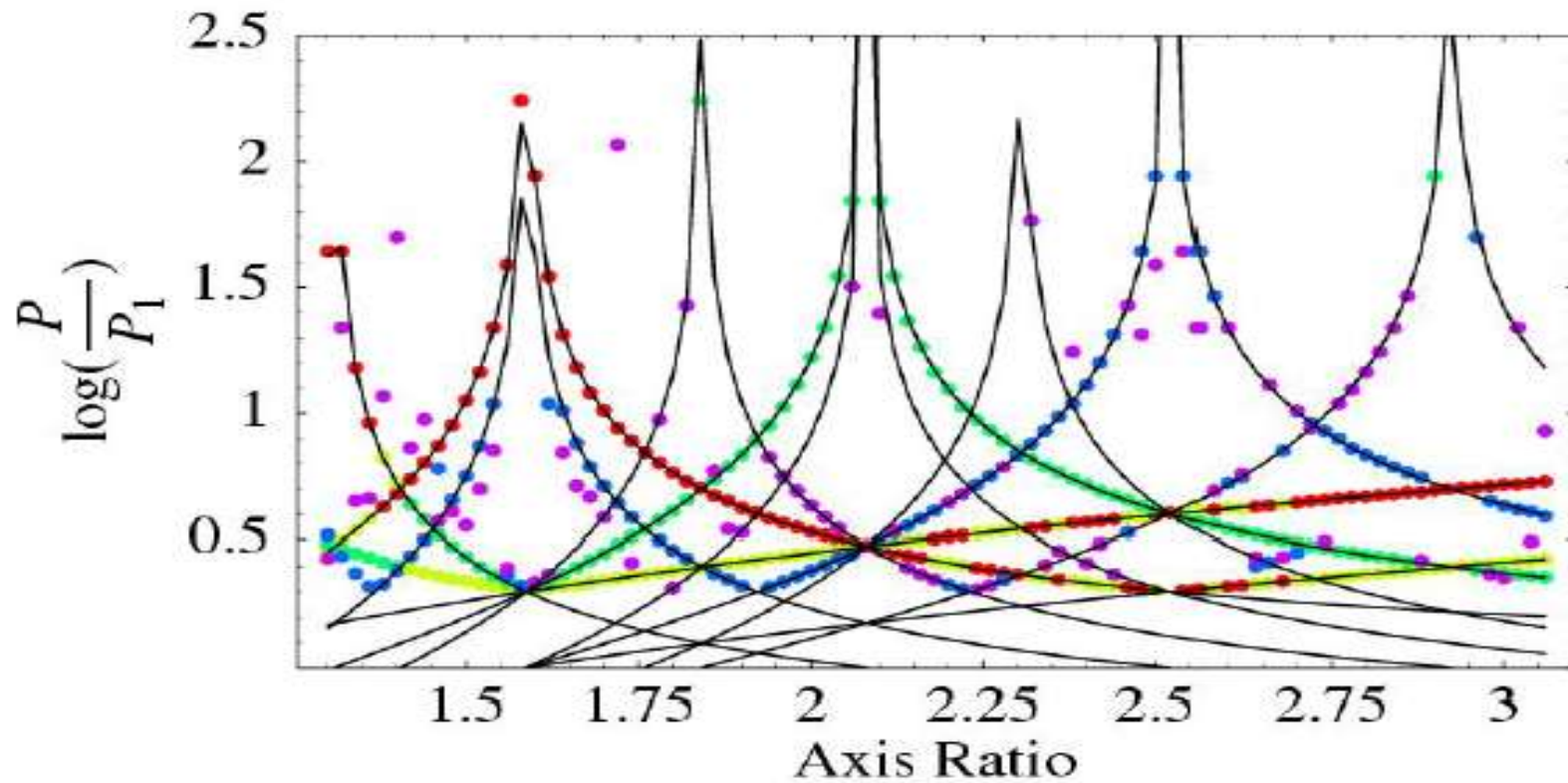
10s smallest error

TrES-1 results from Steffen & Agol, MNRAS 364, L96 (2005)

Bonus Feature: Fourier Space



Bonus Feature: Fourier Space



$$\frac{P_{\text{peak}}}{P_{\text{trans}}} = \frac{P_{\text{pert}}}{iP_{\text{trans}} - jP_{\text{pert}}}$$