

6. the variance of velocity for 1 of the 3 perpendicular directions

6052

directions  $P = \frac{2}{3} \int_0^\infty \frac{1}{2} m v^2 n(v) dv$   
 ~~$\int_0^\infty \frac{1}{2} m v^2 n(v) dv$~~   $= \frac{1}{3} m n \int_0^\infty v^2 f(v) dv = \frac{1}{3} m n \frac{3kT}{m} = n k T$

e.g., Maxwell Boltzmann distribution  
 $P_i = n_i k T$  partial pressure

For 3 directions  $\rightarrow$   
 ~~$\frac{3kT}{m}$~~   $= \frac{3kT}{m}$

Max: Max-Boltz distribution function

$3eV - 53$   
 ~~$P = \sum \frac{m_i n_i k T}{m_i} = \sum n_i k T$~~   
 ~~$= \sum n_i k T$~~

dimensional correct  $\left[ \frac{N}{m^3} \right] \cdot \left[ \frac{m^2}{s^2} \right] = \frac{N}{m^2}$   
 $P = n k T$  ideal gas law  
 No dependence on particle mass. Add up the pa

c) the Hydrostatic Equilibrium equation for gas

$\frac{P}{A_{amp}} = \sum \frac{x_i P}{A_{amp}} = n_i$   
 $n = \sum n_i$

in this context call the isotropic Jeans equation  
 Ci-197, 182  
 becomes

contains the particle mass concept at all times  
 $P = n k T$   
 ideal gas law for one species

$kT \frac{dn}{dr} = - \frac{GM(r)}{r^2} \rho$

For gas divide this by particle mass  $m$   
 ~~$\frac{kT}{m} \frac{dn}{dr} = - \frac{GM(r)}{r^2} \frac{\rho}{m}$~~   
 which we have implicitly assume is the same for all particles.

$\frac{kT}{m m_0} \frac{dn}{dr} = - \frac{GM}{r^2} \frac{\rho}{m m_0} = - \frac{GM}{r^2} n$   
 $\frac{P}{A_{amp}} = \sum_i \frac{x_i P}{A_i m_i} = \sum_i n_i = n$

6052

Dark matter particles decoupled except in their global mass effect - assumed spherically symmetric

$$\frac{d v_{\text{circ}}^2}{d r} = - \frac{GM}{r^2}$$

separately?  
 The pressure of the two species are decoupled. They do not feel each other. Gas holds up gas - galaxies hold up galaxies  
 pressure non zero  
 flow to either kind of particle has to interact even with itself  
 of course gas interacts with gas particles and galaxies interact gravitationally with galaxies  
 similarly dark matter particles are decoupled at they

and now assume isothermal for both gas and galaxies - very roughly true

$\sigma_v$  independent of  $r$

$$\frac{m}{n} \frac{dn}{dr} = - \frac{GM}{r}$$

$$\sigma^2 \frac{d \ln(n)}{d \ln(r)} = - \frac{GM}{r}$$

$$\sigma^2 = \frac{kT}{m m_p} \text{ for gas}$$

$$\sigma_{\text{los}}^2 \text{ for galaxy}$$

MB distribution  $\mu$  is mean atomic weight of proton mass - universe made of protons

$$\mu = \frac{kT}{m_p} \sum \frac{x_i}{A_i}$$

Deltons =  $A m_p$   
 $= \frac{1}{2} m_p c^2$

$$\frac{kT}{m_p} \frac{d \ln n}{d \ln r} = - \frac{GM}{r} \quad \sigma_{\text{los}}^2 \frac{d \ln v_{\text{los}}}{d \ln r}$$

but for gas particles

with Maxwell Boltzmann distribution

6053

~~$d(A_i) \propto e^{-\frac{E_i}{kT}}$~~

~~$d(\rho) = -\frac{GM(r)}{r^2} \sum_i m_i n_i$~~

Unit  $\rightarrow$  correct but pointless  $\frac{kT}{m_i} \frac{dn}{dr} = -\frac{GM(r)}{r^2} \left(\frac{\rho}{A_i m_p}\right)$  and for  $\rho = \sum_i \frac{X_i \rho}{A_i m_p}$

$\sum_i f_i = 1$   
leave explicit

let  $f_i = \frac{n_i}{n}$  total particles = density  
number fraction

~~$kT \frac{dn}{dr} = -\frac{GM(r)}{r^2} n \sum_i f_i m_i$~~

and  $f_i$  is assumed constant with radius.

For too since we assume that the system is Boltzmann

~~$\left(\sum_i f_i kT\right) \frac{dn}{dr} = -\frac{GM(r)}{r^2} n$~~

Now  $f_i = \frac{n_i}{n} = \frac{X_i \rho}{m_i} n$  where  $X_i$  is mass fraction

$\frac{1}{\sum_i f_i m_i} = \frac{1}{\rho \sum_i \frac{X_i m_i}{m_p}}$   
so  $\mu = \frac{\rho}{\rho \sum_i \frac{X_i m_i}{m_p}}$  at max I should know

$\frac{\sum_i f_i}{\sum_i f_i m_i} = \frac{\sum_i X_i m_i}{\sum_i X_i m_i} = \frac{\sum_i X_i m_i}{\sum_i X_i m_i} = \sum_i X_i \frac{m_i}{m_i}$

mean atomic weight  $\mu = \frac{1}{\sum_i \frac{X_i}{A_i m_p}} = \frac{1}{\sum_i \frac{X_i}{A_i m_p}}$

The math uses proton mass as the standard mass since the reverse is used of protons not dalton =  $AMU = \frac{1}{2} m_p$

6054)

$$\therefore \frac{kT}{\mu n_p} \frac{dn}{dr} = - \frac{GM}{r^2} n \text{ from p 6051}$$

But unlike the earlier occasion where we used mean atomic mass, it now includes free electrons since our gas is nearly entirely ionized and free electrons contribute to the pressure of an ideal gas as much as any other particle, but for less mass.

So

$$\mu^{-1} = \sum_i \frac{X_i}{A_i} \Rightarrow$$

$$A_p = 1$$

$$A_e = \frac{m_e}{m_p}$$

example  
pure  
ionized  
Hydrogen

$$X_p = \frac{n_p}{n_p + n_e}$$

$$X_e = \frac{n_e}{n_p + n_e}$$

$$\Rightarrow = \frac{n_p}{n_p + n_e} + \frac{n_e}{n_p + n_e} \frac{m_e}{m_p}$$

$$= \frac{2 n_p}{n_p + n_e} \approx 2$$

$$\mu = \frac{1}{2} \text{ which is consistent}$$

$$\mu = \frac{\rho}{n m_p}$$

$$\approx \frac{n_p \cdot m_p}{n_p + n_e} \frac{1}{m_p}$$

$$= \frac{1}{2}$$

d) Hydrostatic Equilibrium for galaxies and dark matter

galaxies  
and

$$\frac{d(n_{gal} G_{105}^2)}{dr} = - \frac{GM(r)}{r^2} n_{gal}$$

$$P_{gal} = \frac{2}{3} \frac{1}{2} m_{gal} \int_0^{R_0} 4\pi r^2 n(r) dr$$

assuming all galaxies are some mass

$$= m_{gal} \frac{1}{3} G_{gal}^2$$

$$= m_{gal} G_{105}^2 \quad \text{and} \quad \rho_g = n_{gal} m_g$$

dark matter

and we assume  $G_{105}^2$  as a simplifying approximation

$$\frac{d(n_{DM} \frac{1}{2} G_{DM}^2)}{dr} = - \frac{GM(r)}{r^2} n_{DM}$$

e) Combining Hydrostatic equilibrium

We assume ~~galaxies~~ gas, galaxies and dark matter are all decoupled in a pressure sense  
 - their mutual interactions are only through bulk gravity which is spherically symmetric

~~$\frac{kT}{m_p n} \frac{dn}{dr} = - \frac{GM(r)}{r^2} n$~~

$$\therefore \frac{kT}{m_p n} \frac{dn}{dr} = - \frac{GM(r)}{r} = G_{105}^2 \frac{r}{n_{gal}} \frac{dn_{gal}}{dr} = \frac{r}{n_p n} \frac{dn_{DM}}{dr}$$

we assume  $G_{105}^2$  for galaxies can be approximated as a constant

But we are interested in dark matter

6056

$$\frac{kT}{\mu m_p} \frac{d \ln n}{d \ln r} = \sigma_{100}^2 \frac{d \ln n_{gal}}{d \ln r}$$

$$\frac{d \ln n}{d \ln r} = \beta \frac{d \ln n_{gal}}{d \ln r}$$

$$d \ln n = \beta d \ln n_{gal}$$

$$n \propto n_{gal}^\beta$$

where  $\beta = \frac{\mu m_p \sigma_{100}^2}{\cancel{\mu m_p} kT}$  is the  $\beta$  parameter of the  $\beta$  model and not the speed parameter  $\beta$  of relativity  $= \frac{v}{c}$  (Not at work but Wilkinson conference)

ratio of "galaxy temperature" to gas temperature

~~$\frac{kT}{m_p v^2} \approx \frac{d \ln n}{d \ln r_g}$~~   
 ~~$\beta$  is not  $\frac{kT}{m_p v^2}$~~   
~~and not the anisotropy parameter of~~  
 ~~$\frac{d \ln n}{d \ln r_g} = \beta$~~   
 ~~$n \propto n_g$~~   
 ~~$\frac{kT}{m_p v^2} \approx \frac{d \ln n}{d \ln r_g}$~~   
~~ratio of galaxy temperature to gas temperature~~

d) Now if we assume King Profile which is not so good really but again is a reference profile we have

$n_{gal} = n_{gal}$

$\left[ 1 + \left( \frac{v}{v_c} \right)^2 \right]^{3/2}$

but Ci-179, 182 gives no standard  $v_{c,eff}$  for  $v_c$

$\therefore n = n_0 \left[ 1 + \left( \frac{v}{v_c} \right)^2 \right]^{-(3/2)\beta}$

And then can be used to find

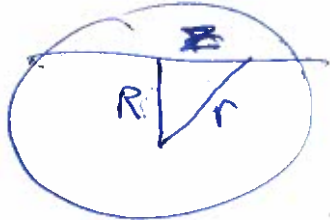
$I_x(R)$

the surface brightness in X-ray

King 1972 for com of cluster  $n_c = 0.13 \text{ Mpc}$   
 (King 1962 was thinking of globular clusters and elliptical galaxies not galaxy clusters)  
 $n_c \in [0.07, .4] \text{ Mpc}$   
 Ciamele 1996  $\alpha 1997$  (in ApJ)

6058

$$I_x(R) = 2 \int_R^{\infty} \frac{j_x(r) r dr}{\sqrt{r^2 - R^2}} \quad (Cr-172)$$



$$j_x \propto n_e n_{ion} \quad (Cr-172)$$

$$\approx n^3$$

$$I_x(R) \propto 2 \int_R^{\infty} \frac{1}{\sqrt{r^2 - R^2}} \frac{n_0^2 r}{\left[1 + \left(\frac{r}{r_c}\right)^2\right]^{3/2}} dr$$

~~$$\approx 2 \int_R^{\infty} \frac{n^2 r}{\sqrt{r^2 - R^2}} dr$$~~

Doesn't  
look  
analytically  
~~tractable~~  
tractable to me

~~$$\propto \frac{2 n_c n_0^2}{r_c} \int_{R/r_c}^{\infty} \frac{1}{\sqrt{x^2 - \left(\frac{R}{r_c}\right)^2}} \frac{x dx}{(1+x^2)^{3/2}}$$~~

$$2 n_c n_0^2 \int_0^{\infty} \frac{dx}{(1+x^2)^{3/2}}$$

still  
not  
tractable

$R=0$

Just  
an order  
of  
magnitude  
approximation  
- some  
behavior.

My guess is they ansatz =  $\phi$

Seems  
pretty  
hell  
to me.

$$\sqrt{x^2 - \left(\frac{R}{r_c}\right)^2} \triangleq \sqrt{x^2 + 1}$$

or

somehow an  $\infty$  approximation



$$\begin{aligned}
 \Sigma_{\lambda}(R) &\propto 2v_c n_0^2 \int_{\frac{R}{v_c}}^{\infty} \frac{x dx}{(1+x^2)^{3\beta+\frac{1}{2}}} \\
 &= 2v_c n_0^2 \frac{(1+x^2)^{-3\beta+\frac{1}{2}}}{-3\beta+\frac{1}{2}} \Bigg|_{\frac{R}{v_c}}^{\infty} \\
 &= 2v_c n_0^2 \frac{(1+(\frac{R}{v_c})^2)^{-3\beta+\frac{1}{2}}}{3\beta-\frac{1}{2}}
 \end{aligned}$$

which is valid if  $3\beta - \frac{1}{2} > 0$

$$\beta > \frac{1}{6}$$

and  $\beta \in [\frac{1}{2}, 1]$

and  $\beta = \frac{2}{3}$  is the reference value (Ci-182)

For  $\beta = \frac{2}{3}$

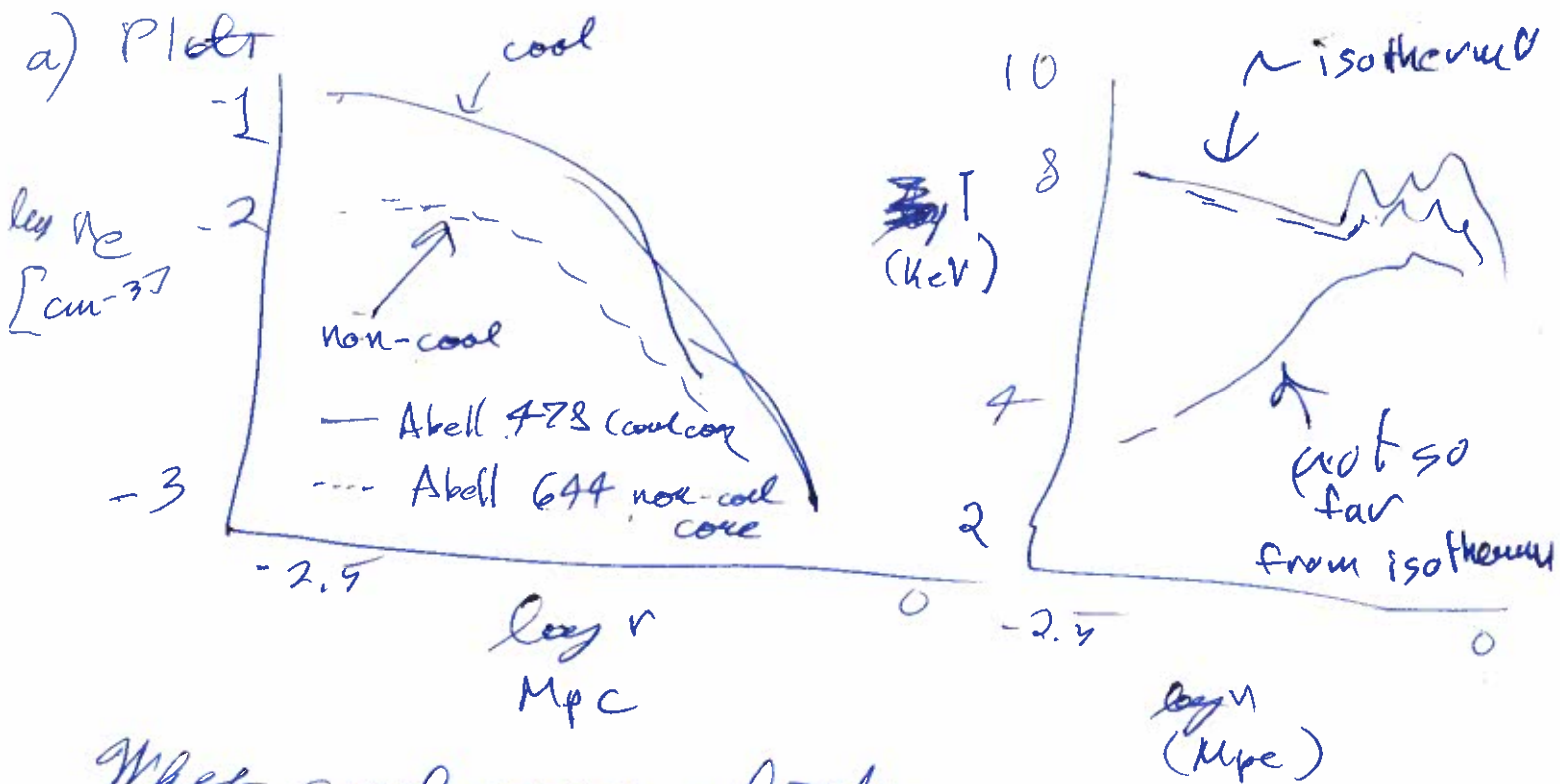
$$\Sigma_{\lambda}(R) \propto \left(\frac{R}{v_c}\right)^{-\frac{1}{2}(2+\frac{1}{2})} = \left(\frac{R}{v_c}\right)^{-\frac{5}{4}}$$

$$n(r \geq v_c) \propto r^{-2} \quad \text{and} \quad n_{gal} \propto \left(\frac{r}{v_c}\right)^{-3}$$

and so the gas distribution is more extended than galaxy distribution.

6060) But the  $\beta$ -model  
 is only a reference  
 model  
 — a standard of comparison  
 for more realistic models  
 which deviate from it  
a lot in general (Ci-182)

11) Cool-Core & Non-Cool Core  
Clusters Ci-182



Why cool core clusters

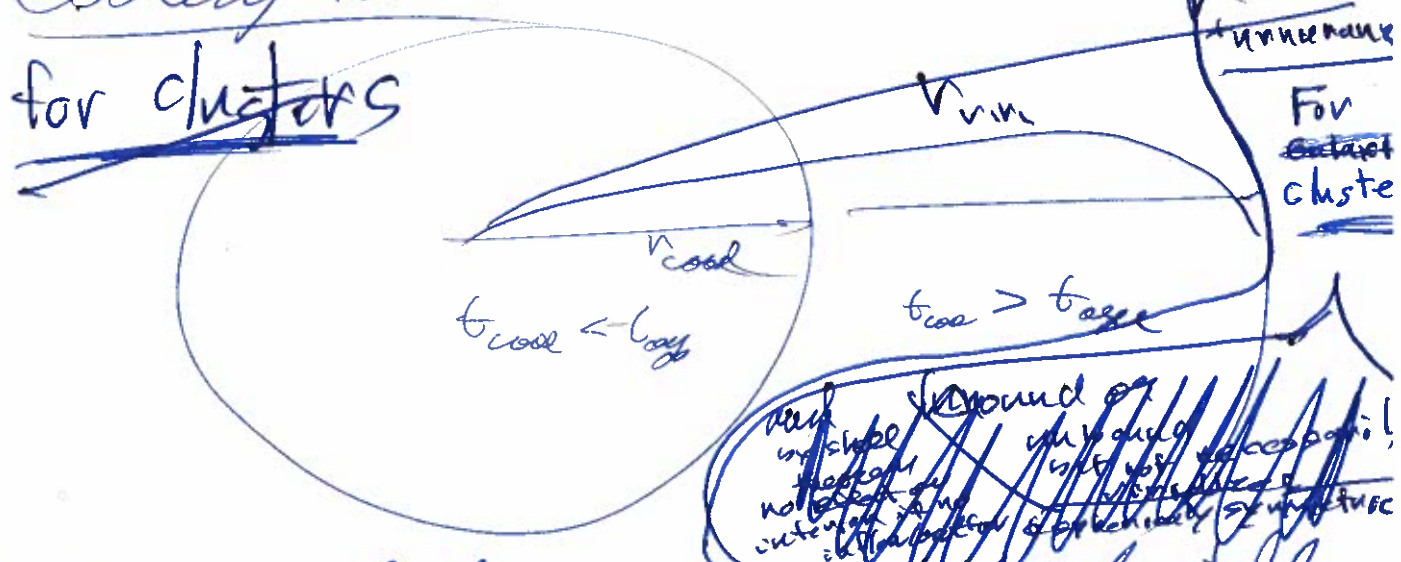
higher density  $j_x \propto n_e n_p \propto n_e^2$  Ci-199  
 $\therefore t_{\text{cool}} \propto \frac{E_{\text{gas}}}{j_x} \propto \frac{1}{n_e^2}$  estimate of time to go to zero T (Ci-228)

for cool cores

$$t_{cool} < t_{age\ of\ uneven} = 13.8\ Gyr$$

$$\sim 10^{10}\ yr$$

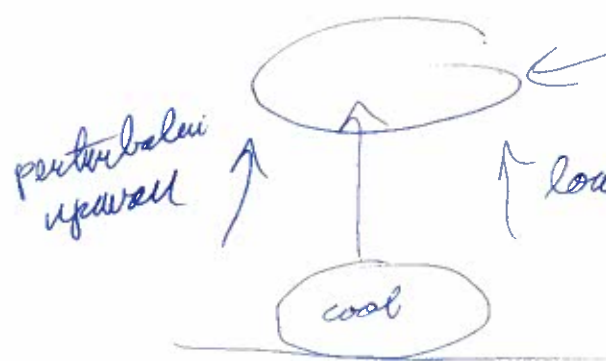
cooling radius  
for clusters



cool core clusters are convectively stable somewhat obviously?

Plausibility argument without understanding

but adiabatic cooling



lower density surroundings but hotter and so pressure can contract it and make it denser and it sinks

- adiabatic heating not enough to counteract.

makes it denser  
suppress it  
to trigger  
to expand  
- NO runaway  
and so sink  
expansion  
and lowering  
of density

6062

But why non-cool core clusters

→ recent cluster merger

- merger has randomized  
the relaxed conditions  
of pre-merger  
clusters

on time scale

$\approx 1 \text{ Gyr}$  I guess

Table of Relative ~~Average~~ <sup>Typical</sup> Behaviors Ci-184

Cool Core

non-cool core

- outward increasing profile

blurred temperature profile

- higher central density

lower central density

- regular  
→ i.e. spherically symmetric

irregular  
→ less spherically symmetric

- has BCG

- tends not to  
but Virgo

Cluster  
is irregular Ci-186  
but M87 is Super Giant elliptical (with  
near center has a BCG,

little substructure -  
No diffuse radio halo  
central radio galaxy

substructure  
diffuse radio halo  
no central radio galaxy  
but ~~but~~ M87 has radio lobes  
and so is a radio galaxy

# 12) Cluster <sup>virial</sup> Mass

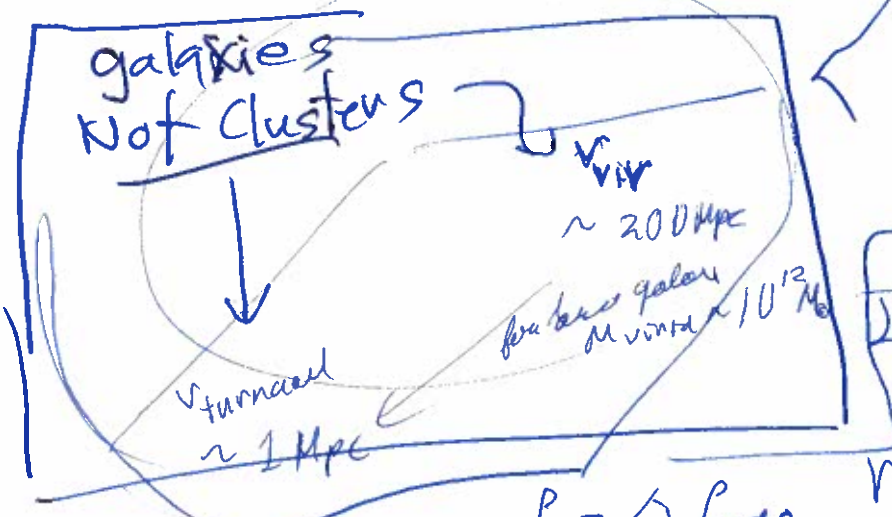
6063

Mass Density Profile (Dark matter mainly)

& Scaling relations

King Profile for Galaxy number density

a)  $M_{vir} \approx 10^{14} - 10^{15} M_{\odot}$  (Ci-165)  
 from velocities &  $r_{vir}$   
 Probably  $M_{200}$  (i.e.  $M_{vir}$  for  $\Delta_c = 200$ )



$r_{vir}$  the radius out to which the interior has been virialized

In spherical collapse model Ci-200-20

$r_{vir}$  is set by an overdensity ratio to  $\rho_{crit}$

$$\rho = \Delta_c \rho_{crit 0}$$

defines the  ~~$r_{vir}$~~

$$\Delta_c = \frac{\rho}{\rho_{crit 0}} = 200$$

Ci-203  
Fiducial value but better to expect  $\rho_{crit}$  value

For  $\Delta_c = 200$

$$r_{vir} = r_{200}$$

Spherical collapse model of dark matter halos  
 Ci-201

Ci-19

$$\begin{aligned} \text{ISM density} &\approx 1 \text{ atom/cm}^3 \\ &= \frac{1}{\text{cm}^3} \left( \frac{10^2 \text{ cm}}{\text{m}} \right)^3 \\ &= 10^6 \frac{\text{atom}}{\text{m}^3} \end{aligned}$$

$$\rho_{crit 0} = \frac{3H^2}{8\pi G} = 1.9 \times 10^{-29} \text{ g/cm}^3$$

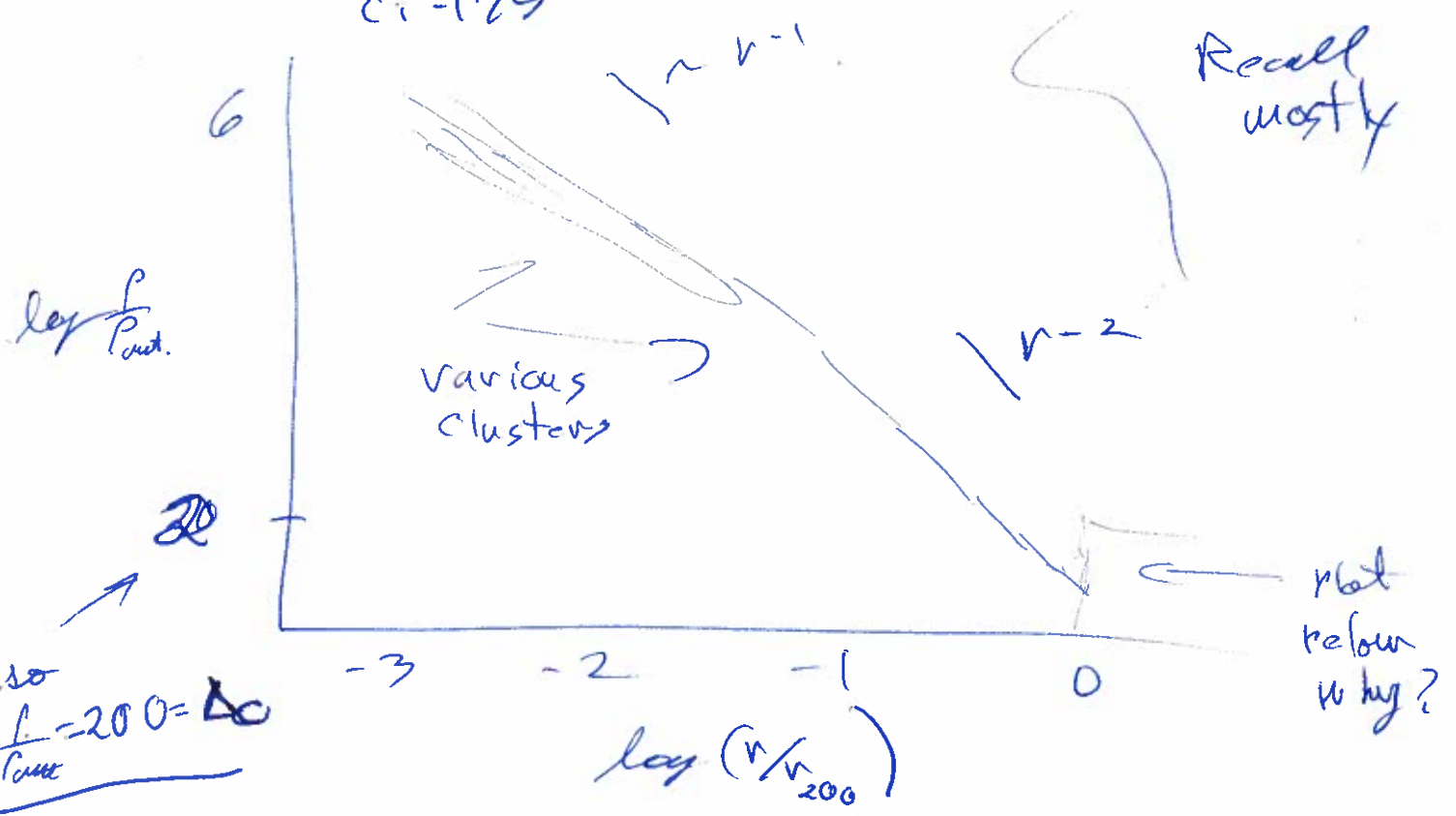
$$\begin{aligned} h &= \frac{H_0}{100} = \frac{H_0}{70} \frac{70}{100} = h_{70} (?) \\ h^2 &= h_{70}^2 (1.5) \end{aligned}$$

$$\begin{aligned} \rho_{crit 0} &= 10^{-29} h_{70}^2 \text{ g/cm}^3 \\ &\approx 6 \text{ proton/cm}^3 \end{aligned}$$

6064] b) Somehow density is measured (Cr-18+194)  
 84 - 90% dark matter

biggest clusters      smallest

$C_i - 174$   
 $C_i - 175$



The profile is NFW-like,

- No surprise: ~~best~~ best fit N-body simulation  $10^{-6} M_{\odot} < M_{halo} < 10^{11} M_{\odot}$   
 J. Wang 2020

gave NFW profile fits

$(0 \rightarrow 30) \times V_s$   
 mostly within 10%, but systematic deviations suggest some improvement possible

$$\rho_{\text{NFW}} = \frac{4\rho_s}{x + 2x^2 + x^3} \quad \boxed{6065}$$

$$x = \frac{r}{r_s} \left\{ \begin{array}{l} r_s \text{ is scale radius} \\ \rho_s \text{ is scale density} \end{array} \right.$$

$$\frac{4\rho_s}{x}$$

$$x < 1$$

$$\rho_s$$

$$x = 1$$

$$\frac{4\rho_s}{x^3}$$

$$x \gg 1$$

logarithmic slope

$$\frac{d \ln \rho}{d \ln r} = \frac{d \ln \rho}{d \ln x} = \frac{x}{\rho} \frac{d\rho}{dx} = \frac{x}{\rho} \left[ \frac{-4\rho_s (1+2x+3x^2)}{(x+2x^2+x^3)^2} \right]$$

$$= -x \frac{(1+4x+3x^2)}{(x+2x^2+x^3)} = -\frac{(1+4x+3x^2)}{(1+2x+x^2)}$$

$$\left. \begin{array}{l} \\ \\ \end{array} \right\} -\frac{8}{4} = -2$$

6066) a)

Scaling relations

$$M_{vir} \propto T^{3/2}$$

$$L_x \propto T^3$$

average temperature

measure by exponential cutoff of free emission

$C_i = 524$   
 $C_i = 142$

useful for estimating  $M_{vir}$  and  $L_x$

# Influence of Environment on Galaxy Properties

Large scale structure (LSS) cosmic web

layers of in cosmic voids, clusters of voids and filaments

Above groups and clusters of galaxies are

superclusters, filaments, sheets, walls

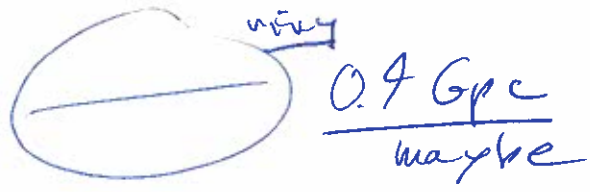
$C_i = 186$  etc. doesn't use this term for superclusters unboundly irregular defining edge in eye-d behavior

size scale 50-100 Mpc

voids (size scale 10-100 Mpc)

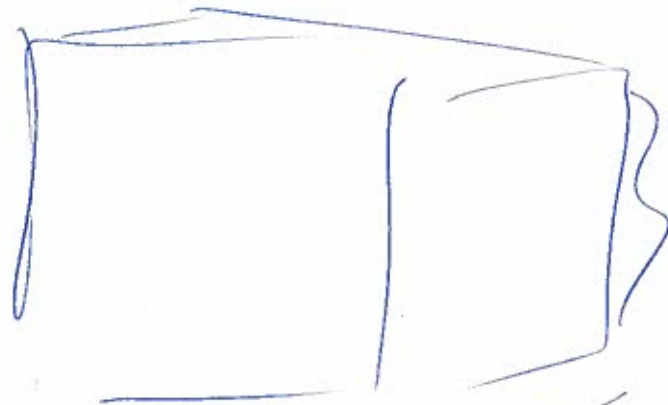
voids upto  $\sim 1$  Gpc (?)

Supervoid  $R = 220(50)$  Mpc





Particular large-scale structure  
realized ~~is now~~  
in the observable universe  
is now called cosmic web



Cosmic Present

400 Mpc (WIK)

- cubes of this size  
seem to  
have same properties

- size scale  
of cosmological  
principle

Observable  
universe

homogeneous  
and isotropic

on large  
enough scale

Einstein introduced idea  
in mathematical cosmology  
for universe of stars  
he had little idea  
of the scale  
size

but there are  
some ~~some~~ structures  
larger  $\approx 1$  Gpc?

- are there just  
fluctuations

or is the  
cosmological  
principle  
failing

If seems  
every month  
or so there  
are at least two papers  
coming to the opposite  
conclusion on the issue

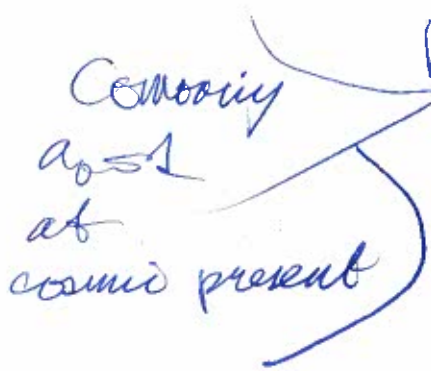
E.A. Milne  
introduced  
name  
cosmological  
principle  
in 1930s

6068) Obviously if the cosmological principle is failing, it is doing so very inconspicuously  
 - strong evidence for it is the CMB

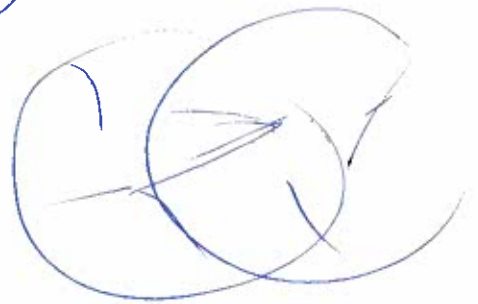
↳ departures are tiny

$$\frac{\Delta I_{\text{CMB}}}{I} \approx 10^{-5} \quad (\text{w. h. CMB features})$$

Also Baryonic Acoustic Oscillations (BAOs)



$$r = 490 \text{ Mpc} \approx 150 \text{ Mpc}$$



The cosmological principle doesn't have to hold.

- hierarchical universe considered before 1960s

- ↳ structures on larger scales forever
- ↳ No end of greatness
- ↳ perhaps fractal → some on all scales after a point.

# (4) Influence of Environment on Galaxies

6069

Denser the galaxy environment  
the larger the  
ratio of EFGs/SFGs (%)

$R = 10 - 20$  in voids  
 $R = 80 - 90$  in densest cluster  
or nodes of filaments.

Morphology  
CSFR  
Density  
Relation  
- a bit  
qualitative

galaxies in voids are called

void galaxies

interesting because they  
perhaps evolved mostly  
in isolation since earlier universe

Do NOT seem odd in obvious features

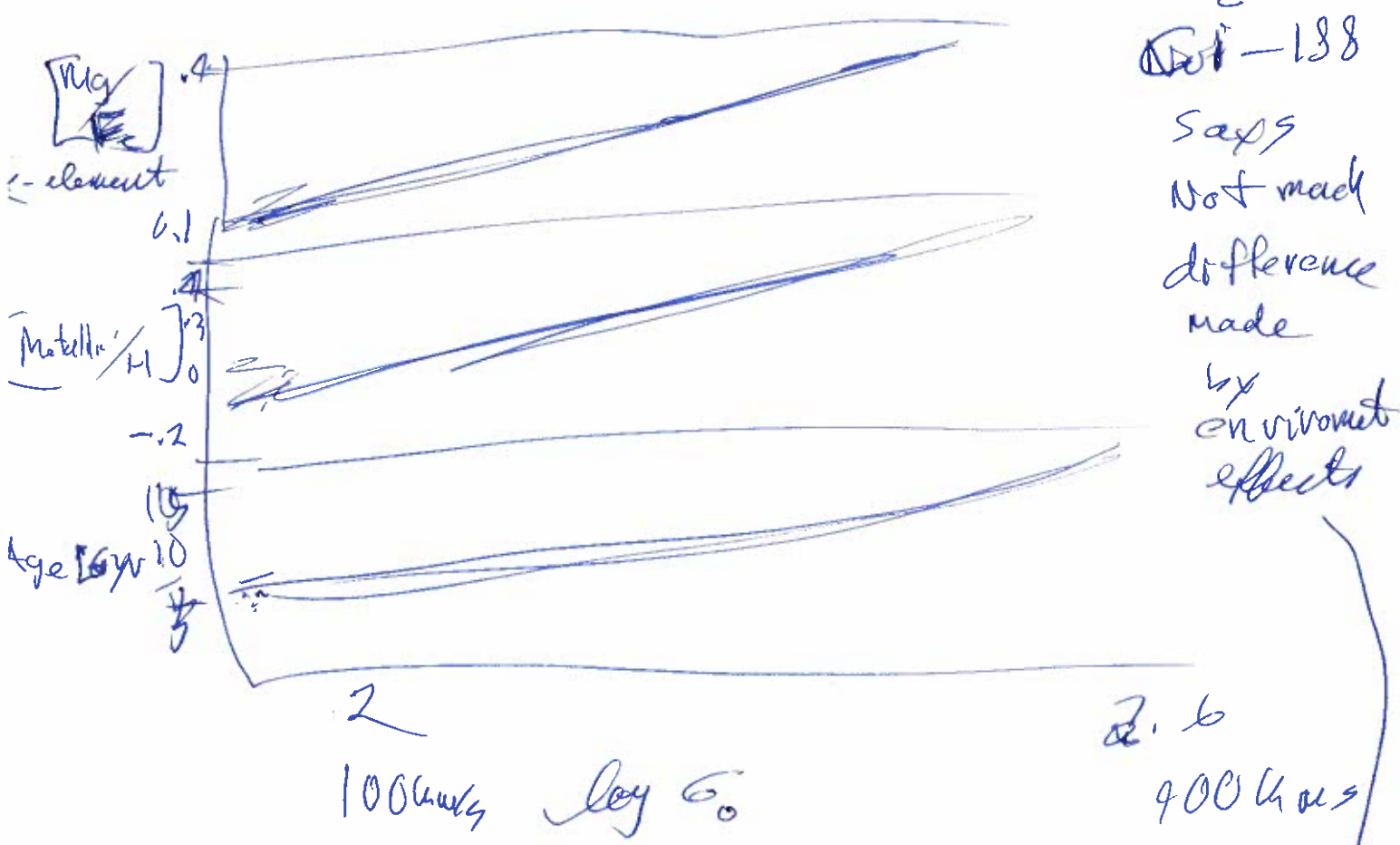
Typically Somewhat smaller SFGs with  
disks, spiral arms not much  
different galaxies in moderate density  
environment

6070

Other than morphology ~~Does~~ <sup>FSF</sup>  
does environment have an effect?

— Seems subdominant  $C_i - 188$

~~For Example~~ <sup>For Example</sup> Scaling relations for  $EIGs$   
 $C_i - 139$   
with (star) central dispersion  $\sigma_c$



But environment can still have a subtle influence,

SO stellar mass and dynamical mass more important than environments for some things

# 15) Large-Scale Structure (LSS) & Galaxy Clustering

6071

Distance  $r$  between galaxies

$\sim 1 \text{ Mpc}$  (fiducial value  
not highly accurate)

and galaxy size

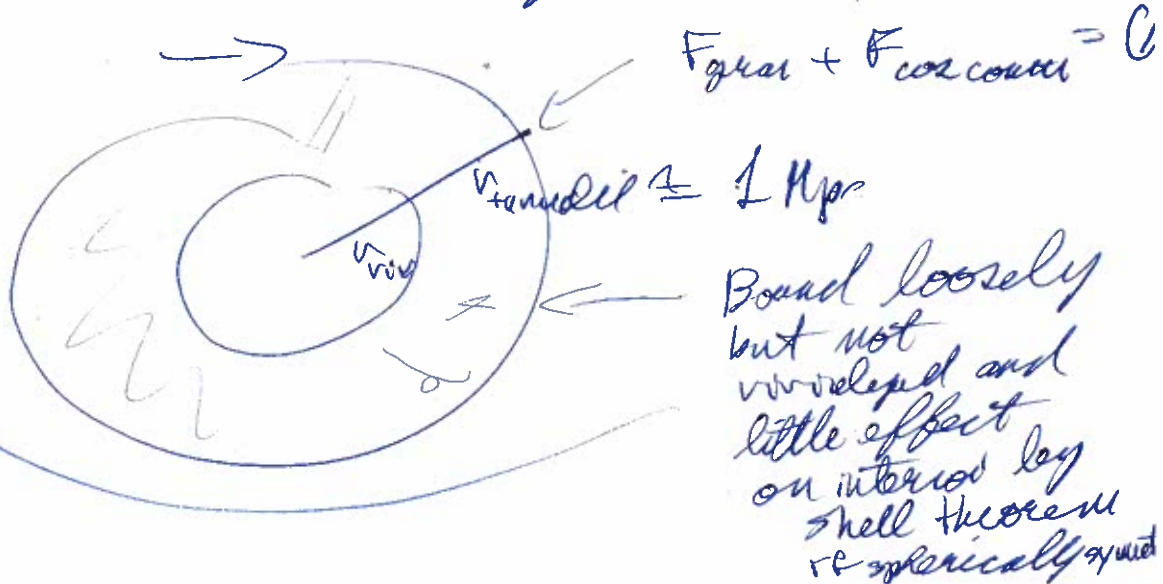
- well disk diameter  $\sim 30 \text{ kpc}$   
 for Milky Way  
 and roughly that  
 order for most  
 spirals.

$$- r_{200} \sim 206.3 \left( \frac{M_{200}}{10^{12} M_{\odot}} \right)^{1/3} \left( \frac{h}{0.7} \right)^{-2/3} \text{ kpc} \quad (1-205)$$

$\frac{r}{r_{\text{vir}}} \approx 200$  consider a fiducial  
 virialization requirement

There is some interest in the dark matter and baryonic matter between  $r_{\text{virial}}$  and  $r_{\text{turnaround}}$

$r_{\text{turnaround}}$



Bound loosely but not virialized and little effect on interior by shell theorem if spherically symmetric

6072

LSS can extend

$\sim 400$  Mpc or maybe more.

So one needs large mapping survey

SDSS-III for example

$\sim 10^6$  galaxies  $\left\{ \begin{array}{l} t_c = 13.7 - 13.7 \text{ Gyr} \\ t_{100h \text{ back}} = 0.3 - 6.3 \text{ Gyr} \end{array} \right.$   
 $z \in [0.2, 0.7]$

of obs. Univ  
 $\frac{4}{3}\pi (14 \text{ Gpc})^3$   
 $\approx 10^4 \text{ Gpc}^3$

on  $8500$  square degrees  $\sim (90 \text{ deg})^2$   
of sky

and volume  $\approx 13 \text{ Gpc}^3 = (2.35 \text{ Gpc})^3$

Qualitatively the cosmic web emerges.

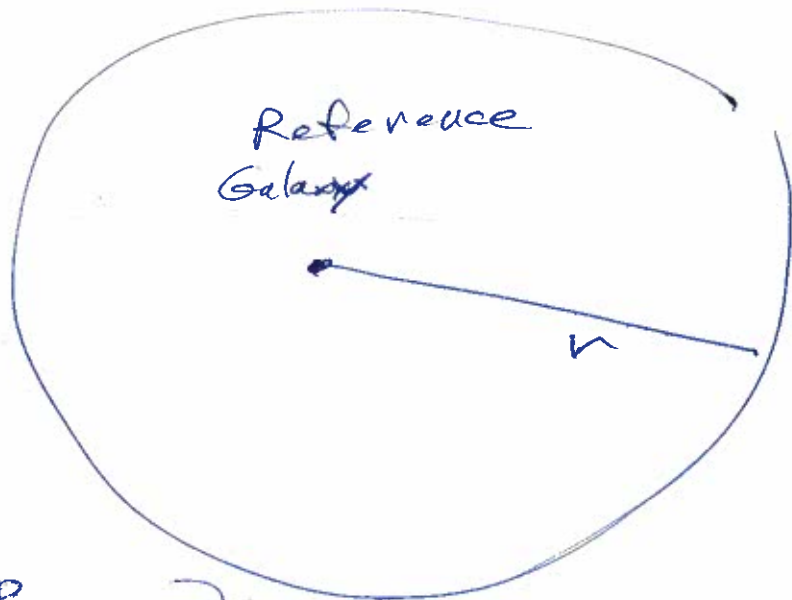
But statistics  $\Rightarrow$  quantitative analysis

- There are many ways to study clustering or clumping of galaxies.

- We can only glance at a very simple analysis  
Statistic - The 2-point correlation function

CI-188 is just a bit too 6073  
 abbreviated for  
 understanding and

used CL-340, see also  
 CL-283  
 CL-344-~~345~~



2-Point  
 correlation  
 function

$$dN = n [1 + \xi(r)] dV$$

Number of galaxies in dV  
on average

Poisson  
 moments

$n$  is the mean number of galaxies  
 per unit volume

$$n = \frac{N}{V}$$

If galaxies were strictly  
Poissonian — just  
 randomly scattered in space  
 they'd obey the Poisson distribution

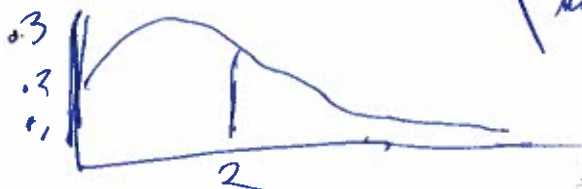
Probability  
 of  $N$  galaxies  
 in volume  $V$   
 given  $n$

$$P(N) = \frac{n^N}{N!} e^{-n} \quad \text{where } \mu = nV$$

Dev-53

mean  
 number in volume  $V$

Poisson distribution  
 is a limiting  
 asymmetric  
 Gaussian distribution



for  $\mu \approx 1.67$   
 $\sigma = 1.29$

6074

However the mean number with a two-point correlation function

$$dN = d\langle N \rangle = n [1 + \xi(r)] dV$$

for galaxy matter at radius  $r$  from the reference galaxy

Corresponding number density not errors in my textbook

has an excess and it is ~~negative~~

positive  $\xi > 0$   
negative  $\xi < 0$

$$\langle N(r) \rangle = n \left[ \frac{4\pi}{3} r^3 + 4\pi \int_0^r \xi(r') r'^2 dr' \right]$$

$$= n 4\pi n^2 \left[ \frac{r^3}{3} + \frac{r^{3-\delta}}{3-\delta} \right] \quad \text{for } r \lesssim 10 \text{ Mpc}$$

However for small  $r$   $\xi > 0$

$$\frac{1}{3} + \frac{1}{2-\delta} = 1.1$$

$$\frac{2}{3} + \frac{2}{1.2} = 2.67$$

as  $r \rightarrow \infty$  this excess goes to zero.

i.e. the galaxies do cluster rather than avoid each other

For  $r \lesssim 10 \text{ Mpc}$

$$\xi = \left(\frac{r}{r_s}\right)^{-\delta} = \left(\frac{r}{r_s}\right)^{-\delta} = n^{-\delta}$$

where  $r_s = 5 \text{ Mpc}$   
 $\delta = 1.8$  } fiducial values

$\xi \approx 30 \rightarrow 50 \text{ Mpc } \xi > 0$   
at  $\xi = 30 \rightarrow 50 \text{ Mpc } \xi$  oscillates around 0.



$$\text{at } r \sim 100 h^{-1} = \frac{100}{0.7} h_{70}^{-1} = 130 h_{70}^{-2} \text{ Mpc} \quad (6079)$$

$$h = \frac{H_0}{100} = \frac{H_0}{70} \frac{70}{100} = h_{70} (0.7)$$

There is a positive excess again.

the BAO scale  
or maybe more like 150 Mpc

BAO scale

DES has just presented  
the April their first results  
but no where in all the  
papers, blinks, videos  
can I find any place  
where they just spit  
out their value for  
the BAO scale.

Two-point correlation function is just  
one statistic.

There are many others and people keep  
inventing new ones trying to  
capture ~~more~~ more of features of large scale  
structure and use to judge  
the fitness of LSS simulations  
TNG, Boyle, Simba etc.

1.  $\frac{1}{x^2} = x^{-2}$   
2.  $\frac{d}{dx} x^{-2} = -2x^{-3}$   
3.  $= -2x^{-3}$   
4.  $= -\frac{2}{x^3}$

5.  $\frac{d}{dx} \frac{1}{x^3} = \frac{d}{dx} x^{-3}$   
6.  $= -3x^{-4}$   
7.  $= -\frac{3}{x^4}$

8.  $\frac{d}{dx} \frac{1}{x^4}$

9.  $\frac{d}{dx} \frac{1}{x^5} = \frac{d}{dx} x^{-5}$

10.  $= -5x^{-6}$

11.  $= -\frac{5}{x^6}$

12.  $\frac{d}{dx} \frac{1}{x^6} = \frac{d}{dx} x^{-6}$

13.  $= -6x^{-7}$

14.  $= -\frac{6}{x^7}$

15.  $\frac{d}{dx} \frac{1}{x^7} = \frac{d}{dx} x^{-7}$

16.  $= -7x^{-8}$

17.  $= -\frac{7}{x^8}$